

$$1.41. \quad y[n] = x[n] \{ g[n] + g[n-1] \}$$

$$(a). \quad \because g[n] = 1, \quad \forall n$$

$$\therefore g[n] + g[n-1] = 2$$

$$\therefore y[n] = 2x[n]$$

$$\cancel{2x[n+n_0]} \rightarrow y[n+n_0] = 2x[n+n_0]$$

So the system is time invariant

$$(b) \quad \because g[n] = n$$

$$\therefore g[n] + g[n-1] = 2n-1$$

$$\therefore y[n] = (2n-1)x[n]$$

$$\cancel{y[n+n_0]} = (2n_0 + 2n_0 - 1)x[n+n_0]$$

$$= (2n-1)x[n_0+n] + 2n_0x[n+n_0]$$

So the system is not time invariant.

$$(c) \quad \because g[n] = 1 + (-1)^n$$

$$g[n] + g[n-1] = 1 + (-1)^n + 1 + (-1)^{n-1} = 2$$

$$\therefore g[n] = 2[n]$$

$$y[n+n_0] = 2x[n+n_0]$$

So the system is time invariant.