
Practice Final Exam

1. A CT LTI system is described by the frequency response

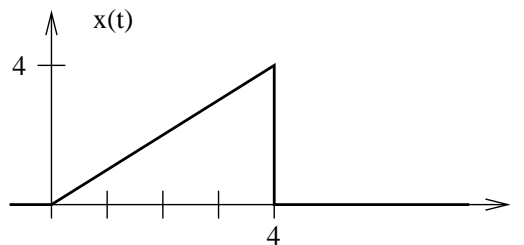
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$$H(j\omega) = \frac{e^{-j\omega}}{3 + \omega^2}.$$

Find the output of this system when the input is $\cos(4t)$.

2. Given $x(t)$,

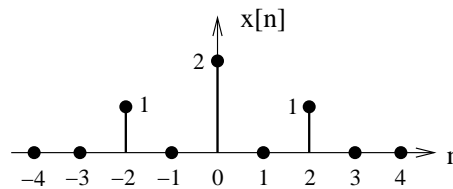
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find $X(j0)$.

3. Give the simplest form possible for $X(e^{j\omega})$ for the signal

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4. A DT system is characterized by the difference equation

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$$y[n] - 0.5y[n - 1] = x[n] + 0.5x[n - 1].$$

Find the frequency response $H(e^{j\omega})$ and the output if the input is $\cos(\pi n)$.

5. An LTI system has the transfer function

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$$H(s) = \frac{s + 1}{s^2 + 7s + 12}$$

with ROC $\text{Re}\{s\} > -3$. Find the impulse response $h(t)$.

6. Given are two DT signals $x[n] = \sin(\pi n/16)$ and $z[n] = \cos(\pi n/2)$.

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(a) Find the DT Fourier series of $z[n]$, when an interval of length $N = 32$ is used.

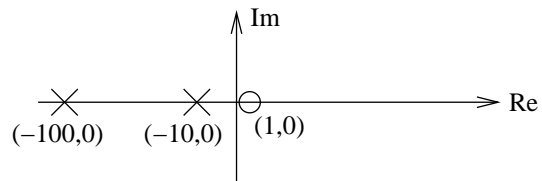
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(b) Write the mathematical form of the DTFT of $w[n] = x[n]z[n]$ and sketch it accurately.

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7. Given is the pole-zero plot of a system function $H(s)$.

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The response of the system to the constant signal $x(t) = 1$ is $y(t) = 2$.

(a) Find $H(s)$.

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(b) Write a differential equation (zero-state response only) describing the relationship between input and output.

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(c) Sketch the magnitude response.

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