Practice for Quiz 4

1. A signal x(t) is periodic with period T = 8, so it can be represented as

$$x(t) = \sum_{k=-\infty}^{\infty} a_k e^{j(2\pi/8)kt}.$$

It is known that the FS coefficients for this representation of x(t) are given by

$$a_k = \frac{1}{8} \int_{-4}^{0} (4+t) e^{-j(2\pi/8)kt} dt$$

(a) Determine an expression for x(t) that is valid over one period.

(b) Draw a plot of x(t) for $-8 \le t \le 8$. Label carefully.

(c) Determine the DC value of x(t).

2. x[n] is a real, even, and periodic signal. Its Fourier series coefficients for N = 8 are denoted by a_k .

(a) Let $a_0 = 1$, $a_1 = 1/2$, and $a_k = 0$ for 1 < |k| < 7. Sketch the signal and write it as a sum of cosines

$$x[n] = \sum_{k=0}^{\infty} c_k \cos(2\pi kn/N + \phi_k).$$

(*i.e.*, determine c_k and ϕ_k .)

(b) Now, assume $a_{4i} = 1$ for $i \in \mathbb{Z}$, and that all other coefficients are zero. What is the fundamental period of x[n]?

(c) Assume we know that x[n] has fundamental period 8. Is it possible that $a_1 = 0$? Explain.