## CSE 30321 - Lecture 13/14 - In Class Handout

For the sequence of instructions shown below, show how they would progress through the pipeline.

## For all of these problems:

- Stalls are indicated by placing the code of the stage where the hazard would be discovered in the succeeding square
- We will assume a standard 5 stage pipeline
- (IF = Instruction Fetch, ID = Instruction Decode, EX = Execute, M = Memory Access, WB = Write Back)
- Assume that each stage of the pipeline takes just 1 clock cycle to finish.


## Example 1:

- Assume that forwarding HAS NOT been implemented
- Assume that you CANNOT read and write a register in the same clock cycle

| Instruction | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{gathered} \text { Add } \\ \$ 5, \$ 3, \$ 4 \end{gathered}$ | IF | ID | EX | M | WB |  |  |  |  |  |  |  |  |  |  |  |  |
| $\begin{gathered} \text { Add } \\ \$ 6, \$ 5, \$ 7 \end{gathered}$ |  | IF | ID | ID | ID | ID | EX | M | W | Add must wait until $\$ 5$ written by previous add; reads $\$ 5$ in ID stage |  |  |  |  |  |  |  |
| $\begin{gathered} \text { LW } \\ \$ 7,0(\$ 6) \end{gathered}$ |  |  | IF | IF | IF | IF | ID | ID | ID | ID | EX | M | WB | LW stalled by prior add; needs $\$ 6$ too reads in CC \#10 |  |  |  |
| $\begin{gathered} \text { SUB } \\ \$ 1, \$ 2, \$ 3 \end{gathered}$ |  |  |  |  |  |  | IF | IF | IF | IF | ID | EX | M | WB | Pipeline full so SUB can't go |  |  |
| $\begin{gathered} \text { Add } \\ \$ 9, \$ 7, \$ 8 \end{gathered}$ |  |  |  |  |  |  |  |  |  |  | IF | ID | ID | ID | EX | M | WB |

(Last add must wait for $\$ 7$ from LW)

## Example 2:

- Let's do the same problem as before, but now assume that forwarding HAS been implemented
- Assume that you CANNOT read and write from the same register in the register file in the same clock cycle
$\left.\begin{array}{|c|c|c|c|c|c|c|c|c|c|c|c|c|c|c|c|c|c|}\hline \text { Instruction } & 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 & 10 & 11 & 12 & 13 & 14 & 15 & 16 & 17 \\ \hline \begin{array}{c}\text { Add } \\ \$ 5, \$ 3, \$ 4\end{array} & \text { IF } & \text { ID } & \text { EX } & \text { M } & \text { WB } & & & & & & & & & \begin{array}{c}\text { Data to be loaded into \$5 } \\ \text { available at end of CC 3/ } \\ \text { Beginning of CC 4 }\end{array} \\ \hline \begin{array}{c}\text { Add } \\ \$ 6, \$ 5, \$ 7\end{array} & & \text { IF } & \text { ID } & \text { EX } & \text { M } & \text { WB } & & & & & & & \begin{array}{c}\text { Add gets data for \$5 directly } \\ \text { from output of ALU }\end{array} \\ \hline \begin{array}{c}\text { LW } \\ \$ 7,0(\$ 6)\end{array} & & & \text { IF } & \text { ID } & \text { EX } & \text { M } & \text { WB } & & & & & & \begin{array}{c}\text { Lw gets \$6 data directly } \\ \text { from output of ALU }\end{array} \\ \hline \begin{array}{c}\text { SUB } \\ \$ 1, \$ 2, \$ 3\end{array} & & & & \text { IF } & \text { ID } & \text { EX } & \text { M } & \text { WB } & & & & & \begin{array}{c}\text { No dependencies on any } \\ \text { other instructions }\end{array} \\ \hline \begin{array}{c}\text { Add } \\ \$ 9, \$ 7, \$ 8\end{array} & & & & & \text { IF } & \text { ID } & \text { EX } & \text { M } & \text { WB } & & & & \begin{array}{c}\text { Add gets \$7 data from latch } \\ \text { between memory and } \\ \text { writeback stage }\end{array} \\ \text { (its an input to ALU) }\end{array}\right]$


## Example 3:

- Like Example 2, assume that forwarding HAS been implemented
- Assume that you CAN read and write a register in the same clock cycle

| Instruction | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{gathered} \text { Add } \\ \$ 1, \$ 6, \$ 9 \end{gathered}$ | IF | ID | EX | M | wB |  |  |  |  |  |  |  |  |  |  |  |  |
| $\begin{gathered} \text { Add } \\ \$ 6, \$ 2, \$ 4 \end{gathered}$ |  | IF | ID | EX | M | WB |  |  |  |  |  |  |  |  |  |  |  |
| $\begin{gathered} \text { LW } \\ \$ 7,0(\$ 6) \end{gathered}$ |  |  | IF | ID | EX | M | WB |  |  |  |  | LW instruction producing result that will be stored in $\$ 7$; even with forwarding must stall; data not available until end of CC \#6 and needed at beginning of CC \#6 |  |  |  |  |  |
| $\begin{gathered} \text { SUB } \\ \$ 1, \$ 7, \$ 8 \end{gathered}$ |  |  |  | IF | ID | ID | EX | M | WB |  |  |  |  |  |  |  |  |
| $\begin{gathered} \text { Add } \\ \$ 9, \$ 1, \$ 8 \end{gathered}$ |  |  |  |  | IF | IF | ID | EX | M | WB |  |  |  |  |  |  |  |

## Example 4:

- Assume that $16 \%$ of instructions change the flow of a program
- 1 in 6 is about right actually.
- $4 \%$ are unconditional branches
- Unconditional branches would incur a 3 CC penalty because you would need to calculate a new address
- $12 \%$ are conditional branches
- $50 \%$ of conditional branches are taken
- $50 \%$ of conditional branches are not taken
- What is the impact on performance assuming:
- $N$ instructions are executed
- We predict that branches are not taken
- Seemingly the only way right?
- Well...
- $4 \%$ of the time we will have a 3 CC penalty
- Therefore: $0.04 \times \mathrm{N} \times 3=0.12 \mathrm{~N}$
- $6 \%$ of the time we will also have a 3 CC penalty because we guessed wrong
- i.e. $0.12 \times 0.5 \times 3 \times \mathrm{N}=0.18 \mathrm{~N}$
- If our ideal CPI is 1 we now have...

$$
\text { - } N+0.3 \mathrm{~N}=1.3 \mathrm{~N}
$$

- We take a $30 \%$ performance hit!


## Example 5:

Assume the following:

- $25 \%$ of instructions are loads $\rightarrow 50 \%$ of the time, the next instruction uses the loaded value
- $13 \%$ of instructions are stores
- $19 \%$ of instructions are conditional branches
- $2 \%$ of instructions are unconditional branches
- $43 \%$ of instructions are something else


## Also...

- You have a 5 stage pipeline with forwarding
- There is a 1 CC penalty if an instruction immediately needs a loaded value
- We have added extra hardware to resolve a jump/branch instruction in the decode stage
- Therefore, there is just a 1 CC penalty
- $75 \%$ of conditional branches are predicted correctly

What is the CPI of our pipeline?

- $0.23 \times 0.5 \times 1=0.115$
- $23 \%$ of the time we have a lw and $50 \%$ of those times, we need the result right away
- $0.02 \times 1=0.02$
- $2 \%$ of the time we have a jump and have a 1 CC penalty
- $0.25 \times 0.19 \times 1=0.0475$
- $25 \%$ of the time we guess wrong on our branch and have a 1 CC penalty

Therefore $0.115+0.02+0.0475=0.1825$
If our ideal CPI is 1 , then our new CPI is 1.1825

## Example 6:

- Assume that forwarding HAS been implemented
- We will stall if we encounter a branch instruction
- Branches or Jumps are resolved after the EX stage.
- Assume that register $\$ 2$ has the value of 0 and $\$ 3$ has the value of 0

| Instruction | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| LW <br> $\$ 1,4(\$ 9)$ | IF | ID | EX | M | W |  |  |  |  |  |  |  |  |  |  |  |  |
| Add <br> $\$ 4, \$ 1, \$ 9$ |  | IF | ID | ID | EX | M | W |  |  |  |  |  |  | Add gets data from Iw <br> forwarding |  |  |  |
| Sub <br> $\$ 7, \$ 4, \$ 9$ |  |  | IF | IF | ID | EX | M | WB |  |  |  |  |  | Sub gets data from <br> add forwarding |  |  |  |
| BEQ <br> $\$ 2, \$ 3, ~ X ~$ |  |  |  |  | IF | ID | EX |  |  |  |  |  |  | BEQ must still wait to <br> enter the pipeline |  |  |  |
| Add <br> $\$ 9, \$ 8, \$ 7$ |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| And <br> $\$ 4, \$ 5, \$ 5$ |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| X: Add <br> $\$ 4, \$ 5, \$ 9$ |  |  |  |  |  |  |  | IF | ID | EX | M | WB |  | Can't start Add until <br> after BEQ finishes <br> executing (comparing) |  |  |  |

## Example 7:

- Assume that forwarding HAS been implemented
- We will predict that any branch instruction is NOT TAKEN
- Branches or Jumps are resolved after the EX stage.
- Assume that register $\$ 2$ has the value of 0 and $\$ 3$ has the value of 0

| Instruction | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{gathered} \mathrm{LW} \\ \$ 1,4(\$ 9) \end{gathered}$ | IF | ID | EX | M | W |  |  |  |  |  |  |  |  |  |  |  |  |
| $\begin{gathered} \text { Add } \\ \$ 4, \$ 1, \$ 9 \end{gathered}$ |  | IF | ID | ID | EX | M | W |  |  |  |  |  |  |  |  |  |  |
| $\begin{gathered} \text { Sub } \\ \$ 7, \$ 4, \$ 9 \end{gathered}$ |  |  | IF | IF | ID | EX | M | WB |  |  |  |  |  |  |  |  |  |
| $\begin{gathered} \text { BEQ } \\ \$ 2, \$ 3, x \end{gathered}$ |  |  |  |  | IF | ID | EX |  |  |  |  |  |  |  |  |  |  |
| $\begin{gathered} \text { Add } \\ \$ 9, \$ 8, \$ 7 \end{gathered}$ |  |  |  |  |  | IF | ID |  |  |  |  | Add and And start down pipeline; however, they would not change state until CC 10 and 11. They never get this far so there is no harm done. We can kill them and restart the next add instruction. |  |  |  |  |  |
| $\begin{gathered} \text { And } \\ \$ 4, \$ 5, \$ 5 \end{gathered}$ |  |  |  |  |  |  | IF |  |  |  |  |  |  |  |  |  |  |
| $\begin{gathered} \text { X: Add } \\ \$ 4, \$ 5, \$ 9 \end{gathered}$ |  |  |  |  |  |  |  | IF | ID | EX | M | W |  |  |  |  |  |

## Example 8:

- Assume that forwarding HAS been implemented
- We will predict that any branch instruction is TAKEN
- Branches or jumps are resolved after the EX stage.
- Assume that register $\$ 2$ has the value of 0 and $\$ 3$ has the value of 0

| Instruction | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| LW <br> $\$ 1,4(\$ 9)$ | IF | ID | EX | M | W |  |  |  |  |  |  |  |  |  |  |  |  |
| Add <br> $\$ 4, \$ 1, \$ 9$ |  | IF | ID | ID | EX | M | W |  |  |  |  |  |  |  |  |  |  |
| Sub <br> $\$ 7, \$ 4, \$ 9$ |  |  | IF | IF | ID | EX | M | WB |  |  |  |  |  |  |  |  |  |
| BEQ <br> $\$ 2, \$ 3, ~ X ~$ |  |  |  |  | IF | ID | EX |  |  |  |  |  |  |  |  |  |  |
| Add <br> $\$ 9, \$ 8, \$ 7$ |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| And <br> $\$ 4, \$ 5, \$ 5$ |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| X: Add <br> $\$ 4, \$ 5, \$ 9$ |  |  |  |  |  | IF | ID | EX | M | W |  |  |  |  |  |  |  |

This is the best situation - the last add instruction finishes 2 CC's earlier.

Example 9:
For the sequence of instructions shown below, show how they would progress through the pipeline.

## Part 1:

- Assume that forwarding HAS been implemented
- We will predict that any branch instruction is NOT TAKEN
- Branches or Jumps are resolved after the EX stage.
- Assume that register $\$ 8$ does not equal $\$ 1$ for the $1^{\text {st }} \mathrm{Beq}$ instruction
- Assume that register $\$ 17$ does equal $\$ 26$ for the $2^{\text {nd }}$ Beq instruction

| Instruction | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{aligned} & \hline \text { SUB } \\ & \$ 1, \$ 2, \$ 3 \end{aligned}$ | F | D | E | M | W |  |  |  |  |  |  |  |  |  |  |  |  |
| $\begin{aligned} & \hline \text { Add } \\ & \$ 8, \$ 9, \$ 10 \end{aligned}$ |  | F | D |  | M | W |  |  |  |  |  |  |  |  |  |  |  |
| $\begin{aligned} & \hline \text { Beq } \\ & \$ 1, \$ 8, x \end{aligned}$ |  |  | F | D | E | M | W |  |  |  | Tech instr | ically, ction | nothin prog | $\begin{aligned} & \text { done } \\ & \text { essin } \end{aligned}$ | $\begin{aligned} & \text { but ce } \\ & \text { be } \end{aligned}$ | think pipel |  |
| $\begin{aligned} & \hline \mathrm{Lw} \\ & \$ 7,0(\$ 20) \end{aligned}$ |  |  |  | F | D | E | M | W |  |  |  |  |  |  |  |  |  |
| $\begin{aligned} & \hline \text { Add } \\ & \$ 11, \$ 7, \$ 12 \end{aligned}$ |  |  |  |  | F | D | D |  | M |  |  |  |  |  |  |  |  |
| $\begin{aligned} & \hline \text { Sw } \\ & \$ 11,0(\$ 24) \end{aligned}$ |  |  |  |  |  | F | F | D | E | M $\nabla$ | W |  |  |  |  |  |  |
| $\begin{aligned} & \hline \text { X: Addi } \\ & \$ 17, \$ 17,1 \end{aligned}$ |  |  |  |  |  |  |  | F | D |  |  | w |  |  |  |  |  |
| $\begin{aligned} & \hline \text { Beq } \\ & \$ 17, \$ 26, Y \end{aligned}$ |  |  |  |  |  |  |  |  | F |  |  | M ${ }^{\text {- }}$ | W V |  |  |  |  |
| $\begin{aligned} & \hline \text { Sub } \\ & \$ 5, \$ 6, \$ 7 \end{aligned}$ |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| $\begin{aligned} & \hline \text { Or } \\ & \$ 8, \$ 5, \$ 5 \end{aligned}$ |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| $\begin{aligned} & \hline \text { Y: Addi } \\ & \$ 17, \$ 17,1 \end{aligned}$ |  |  |  |  |  |  |  |  |  |  |  | F | D | E | M | W | $\checkmark$ |
| $\begin{aligned} & \hline \text { Sw } \\ & \$ 17,0(\$ 10) \end{aligned}$ |  |  |  |  |  |  |  |  |  |  |  |  | F | D | E | M $\nabla$ | W |
| $\begin{aligned} & \hline \text { SUB } \\ & \$ 1, \$ 2, \$ 3 \end{aligned}$ |  |  |  |  |  |  |  |  |  |  |  |  |  | F | D | E | ... |
| $\begin{aligned} & \hline \text { Add } \\ & \$ 8, \$ 9, \$ 10 \end{aligned}$ |  |  |  |  |  |  |  |  |  |  |  |  |  |  | F | D | ... |

## Part 2:

- (i) Assume that this sequence of code is executed 100 times. How many cycles does the pipelined implementation take?
- (ii) How many cycles would this code take in a multi-cycle implementation?
- From Part 1, you can see that it takes 17 clock cycles to execute 12 instructions.
- However, we can start the next "iteration" in clock cycle 14. Therefore, it really only takes 13 cycles for each iteration and 17 CCs for the last one.
- Therefore, iterations 1 through 99 take 13 CCs each
- $(13 \times 99=1287$ CCs $)$
- Iteration 100 takes 17 CCs
- Therefore 1287 CCs + 17 CCs $=1304$ CCs
- For the multi-cycle implementation, we have:
- 9 instructions that take 4 CCs
- 2 instructions that take 3 CCs
- 1 instruction that takes 5 CCs
- Therefore, each "iteration" takes: $(9 \times 4)+(2 x 3)+(1 \times 5)=36+6+5=47$ CCs
- If there are 100 iterations, then 4700 CCs are required

Pipelining gives us a speed up of $4700 / 1304=3.6$ for this implemention

- Little to no extra HW is needed!

