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## CSE 30321 - Computer Architecture I - Fall 2010 <br> Final Exam

December 13, 2010

## Test Guidelines:

1. Place your name on EACH page of the test in the space provided.
2. Answer every question in the space provided. If separate sheets are needed, make sure to include your name and clearly identify the problem being solved.
3. Read each question carefully. Ask questions if anything needs to be clarified.
4. The exam is open book and open notes.
5. All other points of the ND Honor Code are in effect!
6. Upon completion, please turn in the test and any scratch paper that you used.

## Suggestion:

- Whenever possible, show your work and your thought process. This will make it easier for us to give you partial credit.

| Question | Possible Points | Your Points |
| :---: | :---: | :--- |
| 1 | 17 |  |
| 2 | 10 |  |
| 3 | 17 |  |
| 4 | 15 |  |
| 5 | 15 |  |
| 6 | 17 |  |
| 7 | 100 |  |
| Total |  |  |

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## Problem 1: (17 points)

## Question A: (5 points)

A cache may be organized such that:

- In one case, there are more data elements per block and fewer blocks
- In another case, there are fewer elements per block but more blocks

However, in both cases - i.e. larger blocks but fewer of them OR shorter blocks, but more of them - the cache's total capacity (amount of data storage) remains the same.

What are the pros and cons of each organization? Support your answer with a short example assuming that the cache is direct mapped. Your answer must fit in the box below.

## Question B: (5 points)

Assume:

- A processor has a direct mapped cache
- Data words are 8 bits long (i.e. 1 byte)
- Data addresses are to the word
- A physical address is 20 bits long
- The tag is 11 bits
- Each block holds 16 bytes of data


## How many blocks are in this cache?

Name:

Question C: (7 points)
Consider a 16-way set-associative cache

- Data words are 64 bits long
- Words are addressed to the half-word
- The cache holds 2 Mbytes of data
- Each block holds 16 data words
- Physical addresses are 64 bits long

How many bits of tag, index, and offset are needed to support references to this cache?
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## Problem 2: (10 points)

## Question A: (5 points)

The average memory access time for a microprocessor with 1 level of cache is 2.4 clock cycles

- If data is present and valid in the cache, it can be found in 1 clock cycle
- If data is not found in the cache, 80 clock cycles are needed to get it from off-chip memory

Designers are trying to improve the average memory access time to obtain a $65 \%$ improvement in average memory access time, and are considering adding a $2^{\text {nd }}$ level of cache on-chip.

- This second level of cache could be accessed in 6 clock cycles
- The addition of this cache does not affect the first level cache's access patterns or hit times
- Off-chip accesses would still require 80 additional CCs.

To obtain the desired speedup, how often must data be found in the $2^{\text {nd }}$ level cache?
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Question B: (5 points)
Assume that the base CPI for a pipelined datapath on a single core system is 1 .

- Note that this does NOT include the overhead associated with cache misses!!!

Profiles of a benchmark suite that was run on this single core chip with an L1 cache suggest that for every $10,000,000$ accesses to the cache, there are 308,752 L1 cache misses.

- If data is found in the cache, it can be accessed in 1 clock cycle, and there are no pipe stalls
- If data is not found in the cache, it can be accessed in 10 clock cycles

Now, consider a multi-core chip system where each core has an equivalent L1 cache:

- All cores references a common, centralized, shared memory
- Potential conflicts to shared data are resolved by snooping and an MSI coherency protocol

Benchmark profiling obtained by running the same benchmark suite on the multi-core system suggests that, on average, there are now 452,977 misses per 10,000,000 accesses.

- If data is found in a cache, it can still be accessed in 1 clock cycle
- On average, 14 cycles are now required to satisfy an L1 cache miss

What must the CPI of the multi-core system be for it to be worthwhile to abandon the single core approach?
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## Problem 3: (17 points)

## Question A: (6 points)

Below, you are provided with a snapshot of a 4 entry, fully associative TLB and a page table.

- The TLB uses a "least recently used" replacement policy - i.e. the entry that has not been used for the longest time will be evicted if a new entry is to be added
- If needed, you may assume that the value of the page table register is 0
- The page size is 4 KB

Initial TLB State:
(Note that ' 1 ' = "Most Recently Used and ' 4 ' = "Least Recently Used")
(Note that ' 1 ' in the Valid column indicates that the entry is valid)
(Note that ' 0 ' in the Dirty column of the TLB indicates that data has NOT been modified)

| Valid | Dirty | LRU | Tag | Physical Page \# |
| :---: | :---: | :---: | :---: | :---: |
| 1 | 0 | 3 | 0110 | 1000 |
| 1 | 0 | 4 | 0011 | 1101 |
| 1 | 0 | 2 | 1000 | 0110 |
| 1 | 0 | 1 | 0100 | 1010 |

Initial Page Table State:

| Address | Valid | Physical Page \# |
| :---: | :---: | :---: |
| 0000 | 1 | 1110 |
| 0001 | 0 | Disk |
| 0010 | 1 | 1100 |
| 0011 | 1 | 1101 |
| 0100 | 1 | 1010 |
| 0101 | 1 | 1011 |
| 0110 | 1 | 1000 |
| 0111 | 1 | 1001 |
| 1000 | 1 | 0110 |
| 1001 | 1 | 0111 |
| 1010 | 1 | 0100 |
| 1011 | 0 | Disk |
| 1100 | 1 | Disk |
| 1101 | $\ldots$ | 0011 |
| $\ldots$ |  | $\ldots$ |

Show the final state of the TLB after processing the $\mathbf{2}$ virtual address sequence given below.

- If there is a page fault, the physical page number to be entered into the page table would be 0000 ; if there is another page fault, use physical page number 0001

Virtual addresses supplied: (MSB) 1011 ■ $0000 ■ 0001$ ■ 0010 (LSB) (this is a load instruction) (MSB) 1011 - 1101 - 1110 ■ 1111 (LSB) (this is a store instruction)
$\qquad$
(Work space)
(Fill in this table)

| Valid | Dirty | LRU | Tag | Physical Page \# |
| :--- | :--- | :--- | :--- | :--- |
|  |  |  |  |  |
|  |  |  |  |  |
|  |  |  |  |  |
|  |  |  |  |  |

## Question B: (8 points)

- Assume that you have 4 Gbytes of main memory at your disposal
- 1 Gbyte of the 4 Gbytes has been reserved for process page table storage
- Each page table entry consists of:
- A physical frame number
- 1 valid bit
- 1 dirty bit
- 1 LRU status bit
- Virtual addresses are 32 bits
- Physical addresses are 26 bits
- The page size is 8 Kbytes

How many process page tables can fit in the 1 Gbyte space?

Question C: (3 points)
If a virtual-to-physical address translation takes $\boldsymbol{\sim} 100$ clock cycles, what is the most likely reason for this particular latency? Your answer must fit in the box below.
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Problem 4: (15 points)
This question considers the basic, MIPS, 5 -stage pipeline (F, D, EX, M, WB).
(For this problem, you may assume that there is full forwarding for all questions.)
Question A: (5 points)
Assume that you have the following sequence of pipelined instructions:

| lw | $\$ 6,0(\$ 7)$ |
| :--- | :--- |
| add | $\$ 8, \$ 9, \$ 10$ |
| sub | $\$ 11, \$ 6, \$ 8$ |

## Where will the data operands that are processed during the EX stage of the subtract (sub)

 instruction come from? Also, you might take into account the following suggestions:1. Draw a simple diagram to help support your answer.
2. If you are using more than a few sentences, or drawing anything put a simple picture to answer this question, you are making it too hard. You don't need to draw any control signals, etc.

## Question B: (6 points)

## Show how the instructions in the sequence given below will proceed through the pipeline:

- We will predict that the beq instruction is not taken
- When the beq instruction is executed, the value in $\$ 1$ is equal to the value in $\$ 2$
(Fill in this chart)

|  | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| beq $\$ 1, \$ 2, \mathbf{X}$ |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Iw \$10, 0(\$11) |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| sub \$14, \$10, \$10 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| X: add \$4, \$1, \$2 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Iw \$1, 0(\$4) |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| sub \$1, \$1, \$1 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| add \$1, \$1, \$1 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |

## Question C: (4 points)

For the instruction mix above, on what instruction results does the last add instruction depend on?
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## Problem 5: (15 points)

The multi-cycle and pipelined datapaths that we have discussed in class have generally been broken down into 5 steps:

1. Hardware to support an instruction fetch
2. Hardware to support an instruction decode (i.e. a register file read)
3. Hardware to support instruction execution (i.e. the ALU)
4. Hardware to support a memory load or store
5. Hardware to support the write back of the ALU operation back to the register file

Assume that each of the above steps takes the amount of time specified in the table below.

| Fetch | Decode | Execute | Memory | Write Back |
| :--- | :--- | :--- | :--- | :--- |
| 305 ps | 275 ps | 280 ps | 305 ps | 250 ps |

*** Note that these times include the overhead of performing the operation AND storing the data in the register needed to save intermediate results between steps.***

- Thus, the times (Q) capture the critical path of the logic + latching overhead.
- After the $Q$ seconds listed for each stage above, the data can be used by another stage

Question A: (4 points)
Given the times for the datapath stages listed above, what would the clock period be for the entire datapath?

Question B: (3 points)
In a pipelined datapath, assuming no hazards or stalls, how many seconds will it take to execute 1 instruction?
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Question C: (4 points)
Assuming that $\mathbf{N}$ instructions are executed, and all $\mathbf{N}$ instructions are add instructions, what is the speedup of a pipelined implementation when compared to a multi-cycle implementation? Your answer should be an expression that is a function of N .

Question D: (4 points) This question should be answered independently of Questions A-C
Assume you break up the memory stage into 2 stages instead of 1 to improve throughput in a pipelined datapath.

- Thus, the pipeline stages are now: F, D, EX, M1, M2, WB

Show how the instructions below would progress though this 6 stage pipeline. Like before, full forwarding hardware is available.
(Fill in this chart)

|  | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Iw $\$ 5,0(\$ 4)$ |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| add $\$ 7, \$ 5, \$ 5$ |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| sub $\$ 8, \$ 5, \$ 9$ |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |

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## Problem 6: (17 points)

## Question A: (4 points)

In your opinion, what are the 2 most significant impediments to obtaining speedup from $\mathbf{N}$ cores on a multi-core chip (irrespective of finding a good parallel algorithm)? You should also add a 1-2 sentence justification for each item. Your answer must fit in the box below.

## Question B: (9 points)

As was discussed in lecture, as more and more cores are placed on chip, it can make sense to connect them with some sort of interconnection network to support core-to-core communication.

Assume that you have a 6-core chip that you want to program to solve a given problem:

- You can use as few as 1 core or as many as 6 cores to solve the problem
- The problem require 450,000 iterations of a main loop to complete
- Each loop iteration requires 100 clock cycles
- Any startup overhead can be ignored
- (i.e. instructions outside of the loop, to instantiate a new instance of the problem on another core, etc. etc.)

If more than 1 core is used to solve a problem, communication overhead must be added to the total execution time,

- Communication overhead is a function of the number of cores used to solve the problem, and is specified in the table below:

| Number of cores used to solve problem | Communication overhead per iteration |
| :--- | :--- |
| 1 | 0 cycles |
| 2 | 10 cycles |
| 3 | 20 cycles |
| 4 | 30 cycles |
| 5 | 40 cycles |
| 6 | 50 cycles |

- Thus, for example, the communication overhead if 2 cores are used is:
- 10 cycles $/$ iteration $\times 450,000$ iterations $=4,500,000$ cycles

How many cores should be used to solve this problem? (work space provided on next page)

Name:
(work space)

Question C: (4 points)

- Assume that you have 10 cores that you can use to solve a problem in parallel - $98 \%$ of your code is parallelizable

Can you get a speedup of 7 ? If so, how many cores are needed?
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## Problem 7: (9 points)

A snapshot of the state associated with 2 caches, on 2 separate cores, in a centralized shared memory system is shown below. In this system, cache coherency is maintained with an MSI snooping protocol. You can assume that the caches are direct mapped.

PO:

|  | Tag | Data Word 1 | Data Word 2 | Data Word 3 | Data Word 4 | Coherency State |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Block 0 | 1000 | 10 | 20 | 30 | 40 | M |
| Block 1 | 4000 | 500 | 600 | 700 | 800 | S |
| $\ldots$ |  |  |  |  |  |  |
| Block N | 3000 | 2 | 4 | 6 | 8 | S |

P1:

|  | Tag | Data Word 1 | Data Word 2 | Data Word 3 | Data Word 4 | Coherency State |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Block 0 | 1000 | 10 | 10 | 10 | 10 | I |
| Block 1 | 8000 | 500 | 600 | 700 | 800 | S |
| $\ldots$ |  |  |  |  |  |  |
| Block N | 3000 | 2 | 4 | 6 | 8 | S |

## Question A: (3 points)

If PO wants to write Block 0, what happens to its coherency state?

Question B: (3 points)
If P1 writes to Block 1, is Block 1 on P0 invalidated? Why or why not?

## Question C: (3 points)

If P1 brings in Block M for reading, and no other cache has a copy, what state is it cached in?

