# **Missing Data Part II: Multiple Imputation**

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Warning: I teach about Multiple Imputation with some trepidation. You should know what it is and at least have reading competency with it. However, I have seen people try incredibly complicated imputation models before they have a lot of other basics down. For many/most purposes, at least for the work typically done in this class, listwise deletion is fine and MI adds little. Some people say to not even consider MI unless at least 15% or 20% of your data is missing. For your own papers, if you use it at all, MI should probably be one of the last things you do, rather than the first. And, if you do want to seriously use it, you should do a lot more reading than is in these notes.

# I. Advanced methods: Maximum Likelihood Estimation and Multiple Imputation.

Allison concludes that, of the conventional methods listed in Part I, listwise deletion often works the best. However, he argues that, under certain conditions, Maximum Likelihood Methods and Multiple Imputation Methods can work better. As Newman (2003, p. 334) notes, "MI [multiple imputation] is a procedure by which missing data are imputed several times (e.g. using regression imputation) to produce several different complete-data estimates of the parameters. The parameter estimates from each imputation are then combined to give an overall estimate of the complete-data parameters as well as reasonable estimates of the standard errors." Maximum Likelihood (ML) approaches "operate by estimating a set of parameters that maximize the probability of getting the data that was observed" (Newman, p. 332).

Allison argues that, while Maximum Likelihood techniques may be superior when they are available, either the theory or the software needed to estimate them is often lacking. Therefore this handout will focus on multiple imputation.

In a 2000 Sociological Methods and Research paper entitled "Multiple Imputation for Missing Data: A Cautionary Tale" Allison summarizes the basic rationale for multiple imputation:

Multiple imputation (MI) appears to be one of the most attractive methods for general-purpose handling of missing data in multivariate analysis. The basic idea, first proposed by Rubin (1977) and elaborated in his (1987) book, is quite simple:

- 1. Impute missing values using an appropriate model that incorporates random variation.
- 2. Do this <u>M</u> times producing <u>M</u> "complete" data sets.
- 3. Perform the desired analysis on each data set using standard complete-data methods.
- 4. Average the values of the parameter estimates across the  $\underline{M}$  samples to produce a single point estimate.
- 5. Calculate the standard errors by (a) averaging the squared standard errors of the  $\underline{\mathbf{M}}$  estimates (b) calculating the variance of the  $\underline{\mathbf{M}}$  parameter estimates across samples, and (c) combining the two quantities using a simple formula.

#### Allison adds that

Multiple imputation has several desirable features:

• Introducing appropriate random error into the imputation process makes it possible to get approximately unbiased estimates of all parameters. No deterministic imputation method can do this in general settings.

• Repeated imputation allows one to get good estimates of the standard errors. Single imputation methods don't allow for the additional error introduced by imputation (without specialized software of very limited generality).

With regards to the assumptions needed for MI, Allison says that

- First, the data must be missing at random (MAR), meaning that the probability of missing data on a particular variable Y can depend on other observed variables, but not on Y itself (controlling for the other observed variables).
  - Example: Data are MAR if the probability of missing income depends on marital status, but within each marital status, the probability of missing income does not depend on income; e.g. single people may be more likely to be missing data on income, but low income single people are no more likely to be missing income than are high income single people.
- Second, the model used to generate the imputed values must be "correct" in some sense.
- Third, the model used for the analysis must match up, in some sense, with the model used in the imputation...
- The problem is that it's easy to violate these conditions in practice. There are often strong reasons to suspect that the data are not MAR. Unfortunately, not much can be done about this. While it's possible to formulate and estimate models for data that are not MAR, such models are complex, untestable, and require specialized software. Hence, any general-purpose method will necessarily invoke the MAR assumption.

We now show some of the ways Stata can handle multiple imputation problems.

# II. Using Stata 11 or higher for Multiple Imputation for One Variable

This example is adapted from pages 1-14 of the Stata 12 Multiple Imputation Manual (which I highly recommend reading) and also quotes directly from the Stata 12 online help. If you have Stata 11 or higher the entire manual is available as a PDF file. This is a simple example and there are other commands and different ways to do multiple imputation, so you should do a lot more reading if you want to use MI yourself.

NOTE: This example focuses on using regress to impute missing values for a single continuous variable. *Appendix A* shows other examples, such as logit and mlogit for categorical variables. It also shows how to use Predictive Mean Matching (PMM), a sometimes attractive alternative to regress for continuous variables with missing data. *Appendix B* shows how to do multiple imputation when more than one variable has missing data. *Appendix C* shows roughly how multiple imputation works its magic.

The file mheart 0.dta is a fictional data set with 154 cases, 22 of which are missing data on bmi (Body Mass Index). The dependent variable for this example is attack, coded 0 if the subject did not have a heart attack and 1 if he or she did.

- . version 12.1
- . \* Imputation for a single continuous variable using regress
- . webuse mheart0, clear

(Fictional heart attack data; bmi missing)

#### . sum

Variable	Obs	Mean	Std. Dev.	Min	Max
attack smokes age bmi female	154   154   154   132   154	.4480519 .4155844 56.48829 25.24136 .2467532	.4989166 .4944304 11.73051 4.027137 .4325285	0 0 20.73613 17.22643 0	1 87.14446 38.24214
hsgrad marstatus alcohol hightar	+   154   154   154   154	.7532468 1.941558 1.181818 .2077922	.4325285 .8183916 .6309506 .407051	0 1 0 0	1 3 2 1

. mi set mlong

[From the Stata 12 online help:] mi set is used to set a regular Stata dataset to be an mi dataset. An mi set dataset has the following attributes:

- The data are recorded in a style: wide, mlong, flong, or flongsep.
- Variables are registered as imputed, passive, or regular, or they are left unregistered.
- In addition to m=0, the data with missing values, the data include M>=0 imputations of the imputed variables.

For this example, the Stata 12 Manual says "we choose to use the data in the marginal long style (mlong) because it is a memory-efficient style." Type help mi styles for more details.

```
mi register imputed bmi
(22 m=0 obs. now marked as incomplete)
mi register regular attack smokes age hsgrad female
```

An *imputed* variable is a variable that has missing values and for which you have or will have imputations. All variables whose missing values are to be filled in must be registered as imputed variables. A *passive* variable (not used in this example) is a variable that is a function of imputed variables (e.g. an interaction effect) or of other passive variables. A passive variable will have missing values in m=0 (the original data set) and varying values for observations in m>0 (the imputed data sets). A *regular* variable is a variable that is neither imputed nor passive and that has the same values, whether missing or not, in all m; registering regular variables is optional but recommended. In the above, we are telling Stata that the values of bmi will be imputed while the values of the other variables will not be.

#### . mi impute regress bmi attack smokes age hsgrad female, add(20) rseed(2232)

	Observations per m				
Variable	complete	incomplete	imputed	total	
bmi	132	22	22	154	

(complete + incomplete = total; imputed is the minimum across m
 of the number of filled in observations.)

The mi impute command fills in missing values (.) of a single variable or of multiple variables using the specified method. In this case, the use of regress means use a linear regression for a continuous variable; i.e. bmi is being regressed on attack smokes age hsgrad & female. The Stata 12 manual includes guidelines for choosing variables to include in the imputation model. One of the most common/important recommendations is that the analytic model and the imputation model should be congenial, i.e. the imputation model should include the same variables (including the dependent variable) that are in the analytic model; otherwise relationships with the variables that have been omitted will be biased toward 0. Other methods include logit, ologit and mlogit, e.g. you would use logit if you had a binary variable you wanted to impute values for. The add option specifies the number of imputations, in this case 20. (Stata recommends using at least 20 although it is not unusual to see as few as 5.) The rseed option sets the random number seed which makes results reproducible (different seeds will produce different imputed data sets). Case 8 is the first case with missing data on bmi, so let's see what happens to it after imputation:

. list bmi attack smokes age hsgrad female \_mi\_id \_mi\_miss \_mi\_m if \_mi\_id ==8

	bmi	attack	smokes	age	hsgrad	female	_mi_id	_mi_miss	_mi_m
8.		0	0	60.35888	0	0	8	1	0
155.	20.58218	0	0	60.35888	0	0	8		1
177.	27.40752	0	0	60.35888	0	0	8		2
199.	22.1714	0	0	60.35888	0	0	8		3
221.	22.45379	0	0	60.35888	0	0	8		4
243.	31.89095	0	0	60.35888	0	0	8		5
265.	27.42568	0	0	60.35888	0	0	8		6
287.	27.62364	0	0	60.35888	0	0	8		7
309.	33.36433	0	0	60.35888	0	0	8		8
331.	21.90939	0	0	60.35888	0	0	8	•	9
353.	26.93499	0	0	60.35888	0	0	8	•	10
375.	25.82896	0	0	60.35888	0	0	8		11
397.	24.6579	0	0	60.35888	0	0	8		12
419.	23.59406	0	0	60.35888	0	0	8		13
441.	24.35756	0	0	60.35888	0	0	8	•	14
463.	28.23293	0	0	60.35888	0	0	8		15
485.	31.92563	0	0	60.35888	0	0	8		16
507.	31.16652	0	0	60.35888	0	0	8		17
529.	20.54303	0	0	60.35888	0	0	8		18
551.	21.39175	0	0	60.35888	0	0	8		19
573.	   27.27427 +	0	0	60.35888	0	0	8		20   

bmi is missing in the original unimputed data set (\_mi\_m = 0). For each of the 20 imputed data sets, a different value has been imputed for bmi. The imputation of multiple plausible values will let the estimation procedure take into account the fact that the true value is unknown and hence uncertain.

The Stata 12 Manual recommends checking to see whether the imputations appear reasonable. In this case we do so by running the mi xeq command, which executes command(s) on individual imputations. Specifically, we run the summarize command on the original data set (m = 0) and on the (arbitrarily chosen) first and last imputed data sets. The means and standard deviations for bmi are all similar and seem reasonable in this case:

# 

The mi estimate command does estimation using multiple imputations. The desired analysis is done on each imputed data set and the results are then combined into a single multiple-imputation result (the dots option just tells Stata to print a dot after each estimation; it helps you track progress and an X gets printed out if there is a problem doing one of the estimations):

#### . mi estimate, dots: logit attack smokes age bmi hsgrad female

Imputations (2	20): 20 de	one				
Multiple-imput	ation estima	tes		Impu	tations =	20
Logistic regre	ession			Numb	er of obs =	154
				Aver	age RVI =	0.0404
				Larg	est FMI =	0.1678
DF adjustment:	Large sam	ple		DF:	min =	694.17
					avg =	115477.35
					max =	287682.25
Model F test:	Equal :	FMI		F(	5,43531.9) =	3.74
Within VCE typ	e:	MIO		Prob	> F =	0.0022
attack	Coef.	Std. Err.	t	P>   t	[95% Conf.	Interval]
smokes	1.239172	.3630877	3.41	0.001	.5275236	1.950821
age	.0354929	.0154972	2.29			.065867
bmi	.1184188	.0495676	2.39	0.017	.0210985	.2157391
hsgrad	.185709	.4075301	0.46	0.649	6130435	.9844615
female	0996102	.4193583	-0.24	0.812	9215408	.7223204
_cons	-5.845855	1.72309	-3.39	0.001	-9.225542	-2.466168

Note that you don't always get the same information as you do with non-imputed data sets (e.g. Pseudo  $R^2$ ), partly because these things don't always make sense with imputed data or because it is not clear how to compute them.

Compare this to the results when we only analyze the original unimputed data:

#### . mi xeq 0: logit attack smokes age bmi hsgrad female, nolog

m=0 data: -> logit attac	k smokes age	bmi hsgrad	female, r	nolog			
Logistic regre	ession			Numbe	er of obs	=	132
					ni2(5)	=	24.03
	I I I I I I I I I I I I I I I I I I I	,			> chi2		
Log likelihood	l = -/9.3422	L		Pseud	lo R2	=	0.1315
attack	Coef.	Std. Err.	z	P>   z	[95%	Conf.	Interval]
smokes	1.544053	.3998329	3.86	0.000	.7603	945	2.327711
age	.026112	.017042	1.53	0.125	0072	898	.0595137
bmi	.1129938	.0500061	2.26	0.024	.0149	837	.211004
hsgrad	.4048251	.4446019	0.91	0.363	4665	786	1.276229
female	.2255301	.4527558	0.50	0.618	6618	549	1.112915
_cons	-5.408398	1.810603	-2.99	0.003	-8.957	115	-1.85968

The most striking difference is that the effect of age is statistically significant in the imputed data, whereas it wasn't in the original data set.

III. Already existing MI data sets. If you are lucky, somebody else may have already done the imputation for you (although it is possible that you might do even better since you know what variables are in your analytic models); and if you are super-lucky, the MI data will already be in Stata format. If not, you'll have to convert it to Stata yourself. The mi import command may be useful for this purpose. Once the data are in Stata format, the mi describe command can be used to provide a detailed report. Using the above data,

#### . mi describe

# IV. Other comments on multiple imputation

Imputation is pretty easy when only one variable has missing data. It can get more complicated in the more typical case when several variables have missing data. Again, this handout is just a brief introduction; read the manual and some related articles if you want to use multiple imputation in your own analyses.

Random number generator. Stata's random number generator has changed across versions, so even if you do specify rseed you may not get identical results, e.g. some results I got using Stata 11 were not the same as results I got using Stata 12. Using version control should keep things consistent.

Soft versus hard missing data codes. Stata has "soft" missing codes (coded as .) and "hard" missing codes (.a, .b, .c, ... .z). The former are eligible for imputation, the latter are not. This distinction can be useful when variables should not be imputed, e.g. "Number of times pregnant" is not applicable for men; either code it as zero or leave it as missing. Depending on the nature of the variable, you may need to change some soft codes to hard or hard codes to soft. Otherwise you may fail to impute values when you should or else impute values when you shouldn't. As stated before, you need to understand why data are missing.

Multiple imputation on the dependent variable. Multiple imputation on the independent variables can be good because it lets you use the non-missing information on the other independent variables. Multiple imputation of the dependent variable, however, tends to gain you little or nothing. (One possible exception is when you have auxiliary variables that are strongly correlated with the dependent variable, e.g. r = .5 or greater, such as the same variable measured

at different points in time.) Of course, the dependent variable in one part of the analysis may be an independent variable in a different part, so you may go ahead and do the imputation on the variable anyway.

Other programs for multiple imputation. User-written programs like ice and mim can also be used for imputation and estimation. I think Stata 12 largely eliminates the need for those programs. But even if you have Stata 12, the articles that have been written about these programs may be helpful to you in understanding how the ICE method works.

Passive imputation versus "just another variable" (JAV) approach. Passive imputation is somewhat controversial. With passive imputation, you would, for example, impute values for x1 and x2, and then multiply those values together to create the interaction term x1x2. The alternative is to multiply x1 \* x2 before imputation, and then impute values for the resulting x1x2 interaction term, i.e. the "just another variable" (JAV) approach. Perhaps surprisingly, some people (including Paul Allison) claim that the JAV approach is superior. The issue was discussed on Stata List in February 2009. If interested, see

http://www.stata.com/statalist/archive/2009-02/msg00602.html

http://www.stata.com/statalist/archive/2009-02/msg00613.html

In the latter message, Paul Allison says "In multiple imputation, interactions should be imputed as though they are additional variables, not constructed by multiplying imputed values. The same is true if you have x and x^2 in a model. The x^2 term should be imputed just like any other variable, not constructed by squaring the imputed values of x. While this principle may seem counterintuitive, it is easily demonstrated by simulation that the more "natural" way to do it produces biased estimates."

For more good discussion of JAV vs Passive Imputation, as well as several other issues, see

White, Ian R., Royston, Patrick, Wood, Angela M. 2011. "Multiple imputation using chained equations: Issues and guidance for practice." Statistics in Medicine. Pp. 377-399.

Estimating marginal effects after using multiple imputation. The margins command does not work after using mi estimate. Daniel Klein's user-written mimrgns (available from SSC) does. While mimrgns can be extremely helpful, it is also a use at your own risk sort of routine. Be sure to carefully read the help file first, which warns that "There might be good reasons why margins does not work after mi estimate." The help file includes links that explain the approach mimrgns uses.

# Appendix A: More Examples of Multiple Imputation for a Single Variable

These examples (and much of the text) are pretty much copied straight from the Stata 12 or 13 Multiple Imputation Manual. Read the manual for more details. Further, multiple methods can be used if you specify mi impute chained (see Appendix B). Read the manual if you want to get into other methods or more complicated imputations. I will either go over these quickly or not at all in class.

PMM – Predictive Mean Matching. PMM is an alternative to regress when imputing values for continuous variables. It may be preferable to linear regression when the normality of the variable is suspect (which is likely the case with BMI). The basic idea is that you again use regression methods to come up with an estimate of the missing value for variable X. However, rather than use that estimate, you identify one or more neighbors who have similar estimated values. (Note that it is the estimated value for the neighbor, not the neighbor's observed value.) The observed value of the nearest neighbor (or the randomly chosen nearest neighbor) is then used for the imputed value for the case with missing data on X.

So, for example, suppose that case 8 is missing on X, and the estimated value for X is 18.71. Suppose the nearest neighbor has an estimated value of 18.73, with an observed value of 20. Twenty will be used as the imputed value of X for case 8. (If the nearest neighbor was a big outlier, e.g. estimated value of 18.73 with observed value of 50, you would still use the observed value of 50 as the imputed value.) Or, if you have specified, say, 5 nearest neighbors, one of them will be chosen at random and their observed value on X will be used as the imputed value for case 8.

In other words, the method identifies neighbors who have complete data that have estimated values on X that are close to the estimated value for the person with incomplete data. One of these neighbors is chosen as a "donor", and the donor's observed value on the variable replaces the recipient's missing value.

You have to choose how many neighbors are to be used. If you only choose 1, your MI estimates may be highly variable from one imputation to the next. Including too many neighbors may bias your point estimates. In other words there is a tradeoff between biased estimators and estimators that have larger standard errors. The Stata Manual seems to use 1, 3 or 5 neighbors in its examples.

Here is an example from the manual. It uses the same data we used in our earlier example but uses PMM instead of regress to impute values for BMI.

```
. webuse mheart0, clear
(Fictional heart attack data; bmi missing)
. mi set mlong
. mi register imputed bmi
(22 m=0 obs. now marked as incomplete)
. mi impute pmm bmi attack smokes age hsgrad female, add(20) knn(5) rseed(2232)
Univariate imputation
                                    Imputations =
                                        added = 20
updated = 0
Predictive mean matching
Imputed: m=1 through m=20
                               Nearest neighbors =
                            Observations per m
        Variable | Complete Incomplete Imputed | Total
                   _____
            bmi | 132 22 22 | 154
        _____
(complete + incomplete = total; imputed is the minimum across m
of the number of filled-in observations.)
```

As the Stata Manual explains, "By default, mi impute pmm uses one nearest neighbor to draw from. That is, it replaces missing values with an observed value whose linear prediction is the closest to that of the missing value. Using only one nearest neighbor may result in high variability of the MI estimates. You can increase the number of nearest neighbors from which the imputed value is drawn by specifying the knn() option." In the example above I told Stata to select a donor from the 5 nearest neighbors. If you look at the imputed values, you may even be able to figure out who the donor was (e.g. if the imputed value for case 8 is 20 and case 47 is the only case with an observed value of 20, then case 47 must be the donor).

#### . mi estimate: logit attack smokes age bmi hsgrad female

Multiple-imput Logistic regre		tes		Numb Aver	tations er of obs age RVI	=	20 154 0.0419
DF adjustment:	: Large sam	ple		Larg DF:	est FMI min avg	=	0.1801 603.59 287949.70
					max		751953.76
Model F test:	-			•	5,40396.	,	
Within VCE typ		OIM 		Prob 		= 	0.0028
attack	Coef.	Std. Err.	t 	P> t	[95%	Conf.	Interval]
smokes	1.215069	.3622206	3.35	0.001	.5051	101	1.925029
age	.0362938	.0154764	2.35	0.019	.0059	605	.066627
bmi	.1133446	.0505589	2.24	0.025	.0140	518	.2126374
hsgrad	.1702272	.4049114	0.42	0.674	6233	872	.9638415
female	0961759	.4171239	-0.23	0.818	913	725	.7213732
_cons	-5.741508	1.753138	-3.27	0.001	-9.180	562 	-2.302453

While PMM may be superior to regress in some cases, it barely matters here. Recall that this is what we got earlier when we used regress to impute the values of BMI:

Logistic regression  DF adjustment: Large	gample		Avera	er of obs = age RVI =	= 154 = 0.0404	
DF adjustment: Large	gample			age RVI =	0.0404	
DF adjustment: Large	aamplo		_		3.0101	
DF adjustment: Large	aammla		Large	est FMI =	0.1678	
	sampre		DF:	min =	694.17	
				avg =	115477.35	
				max =	287682.25	
Model F test: Equ	al FMI		F(	5,43531.9) =		
Within VCE type:	MIO		Prob	> F =	0.0022	
attack   Coe	f. Std. Err.	t	P> t	[95% Conf		
smokes   1.2391	72 .3630877	3.41	0.001	.5275236	1.950821	
age   .03549	29 .0154972	2.29	0.022	.0051187	.065867	
bmi   .11841	88 .0495676	2.39	0.017	.0210985	.2157391	
hsgrad   .1857	09 .4075301	0.46	0.649	6130435	.9844615	
female  09961	02 .4193583	-0.24	0.812	9215408	.7223204	
_cons   -5.8458	55 1.72309	-3.39	0.001	-9.225542	-2.466168	

I suppose if you were really worried about whether pmm or regress was most appropriate, you could try both and see if it makes much difference.

Logit. Logit imputation is used when the variable with missing data has only two possible values, 0 and 1. In this example, hsgrad (coded 1 if high school graduate, 0 otherwise) has the missing data.

#### . webuse mheart2, clear

(Fictional heart attack data; hsgrad missing)

- . mi set mlong
- . \* This will show us how much missing data, and the ranges of observed values
- . mi misstable summarize

					ODS .	
Variable	   Obs=.	Obs>.	Obs<.	Unique   values	Min	Max
hsgrad	18		136	2	0	1

#### . mi register imputed hsgrad

(18 m=0 obs. now marked as incomplete)

. mi impute logit hsgrad attack smokes age bmi female, add(10) rseed(2232)

Univariate imputation	Imputations =	10
Logistic regression	added =	10
<pre>Imputed: m=1 through m=10</pre>	updated =	0

	Observations per m					
Variable	Complete	Incomplete	Imputed	Total		
hsgrad	136	18	18	154		

(complete + incomplete = total; imputed is the minimum across m
 of the number of filled-in observations.)

- . \* Estimates before imputation
- . mi xeq 0: logit attack smokes age bmi female hsgrad, nolog

#### m=0 data:

-> logit attack smokes age bmi female hsgrad

Logistic regression	Number of obs	=	136
	LR chi2(5)	=	23.99
	Prob > chi2	=	0.0002
Log likelihood = $-81.903374$	Pseudo R2	=	0.1278

attack	   Coef.	Std. Err.	z	P>   z	[95% Conf.	Interval]
smokes	1.475308	.3901501	3.78	0.000	.7106284	2.239989
age	.0294918	.0166343	1.77	0.076	0031108	.0620944
bmi	.1168109	.0498207	2.34	0.019	.0191641	.2144578
female	.170943	.4452731	0.38	0.701	7017761	1.043662
hsgrad	.3634346	.436017	0.83	0.405	4911431	1.218012
_cons	-5.688296	1.791735	-3.17	0.001	-9.200032	-2.17656

- . \* Estimates after imputation
- . mi estimate: logit attack smokes age bmi female hsgrad

Multiple-imput		Impu	tations	=	10		
Logistic regre	ession			Numb	er of obs	: =	154
				Aver	age RVI	=	0.0244
				Larg	est FMI	=	0.1267
DF adjustment:	Large sam	ple		DF:	min	=	588.19
					avg	=	7.02e+07
					max	=	2.75e+08
Model F test:	Equal	FMI		F(	5,47292.	4) =	3.85
Within VCE typ	pe:	OIM		Prob	> F	=	0.0017
attack	Coef.	Std. Err.	t	P> t	 [059	Conf	Interval]
actack		5tu. EII.					Incervar]
smokes	1.274902	.3654074	3.49	0.000	.5587	127	1.991092
age	.0369741	.0154912	2.39	0.017	.0066	119	.0673363
bmi	.1236749	.0464216	2.66	0.008	.0326	902	.2146596
female	1111262	.4195926	-0.26	0.791	9335	126	.7112603
hsgrad	.3176137	.4394874	0.72	0.470	5455	419	1.180769
_cons	-6.169885	1.680838	-3.67	0.000	-9.464	291	-2.875478

mlogit. Multinomial logit can be used when a variable is nominal and has more than 2 categories. Marital Status (1 = single, 2 = married, 3 = divorced) is the missing data victim this time.

#### . webuse mheart3, clear

(Fictional heart attack data; marstatus missing)

- . mi set mlong
- . mi misstable summarize

				<b>.</b>	0bs<.	
Variable	   Obs=.	Obs>.	Obs<.	Unique   values	Min	Max
marstatus	†7   7		147	3 	1	3

## . mi register imputed marstatus

(7 m=0 obs. now marked as incomplete)

#### . mi impute mlogit marstatus attack smokes age bmi female hsgrad, add(20) rseed(2232)

Univariate imputation	Imputations =	20
Multinomial logistic regression	added =	20
<pre>Imputed: m=1 through m=20</pre>	updated =	0

	Observations per m					
Variable	Complete	Incomplete	Imputed	Total		
marstatus	147	7	7	154		

(complete + incomplete = total; imputed is the minimum across m
 of the number of filled-in observations.)

#### . \* Estimates before imputation

## . $\min$ xeq 0: logit attack smokes age $\min$ female hsgrad i.marstatus

#### m=0 data:

-> logit attack smokes age bmi female hsgrad i.marstatus

Iteration 0: log likelihood = -101.126
Iteration 1: log likelihood = -87.825045
Iteration 2: log likelihood = -87.797081
Iteration 3: log likelihood = -87.797076

attack	Coef.	Std. Err.	Z	P>   z	[95% Conf.	Interval]
smokes age bmi female hsgrad	1.439608 .035506 .1076301 .1777255 .0844021	.3786929 .0164938 .047991 .4391299	3.80 2.15 2.24 0.40 0.20	0.000 0.031 0.025 0.686 0.840	.6973834 .0031787 .0135695 6829532 7332135	2.181832 .0678333 .2016907 1.038404 .9020176
marstatus 2 3 _cons	.7620136 0357522 -5.882399	.4520608 .4601057	1.69 -0.08	0.092 0.938 0.001	1240092 9375427 -9.282223	1.648036 .8660383

#### . \* Estimates after imputation

#### . mi estimate: logit attack smokes age bmi female hsgrad i.marstatus

Multiple-imputation estimates Logistic regression				Numb	tations er of obs age RVI	= =	20 154 0.0131
DF adjustment:		Larg DF:	est FMI min avg		0.0479 8349.75 3041131.92 7758178.52		
Model F test: Within VCE typ	Equal be:	FMI OIM		F( Prob	max 7,584619. > F		3.14
attack	Coef.	Std. Err.	t	P> t	[95% (	conf	. Interval]
smokes   age   bmi   female   hsgrad	1.345395 .0398306 .1254246 .0114877 .072225	.3736001 .0159254 .0466702 .4303667 .4139451	3.60 2.50 2.69 0.03 0.17	0.000 0.012 0.007 0.979 0.861	.61315 .00861 .03395 83201 73909	.73 526 .64	2.077638 .0710438 .2168966 .8549917 .8835427
marstatus   2   3   _cons	.7599448 0337952 -6.497155	.4521048 .4612619	1.68 -0.07	0.093 0.942 0.000	12627 9379 -9.8457	83	1.646163 .8703927

ologit. The ordered logistic regression imputation method can be used to fill in missing values of an ordinal variable (e.g. the variable is coded high, medium low; Strongly Disagree, Disagree, Neutral, Agree, Strongly Agree; Poor, Fair, Good, Excellent).

- . use http://www.stata-press.com/data/r13/mheart4, clear
- (Fictional heart attack data; alcohol missing)
- . tabulate alcohol, missing

Alcohol consumption: none, <2 drinks/day, >=2 drinks/day	   Freq.	Percent	Cum.
Do not drink Less than 3 drinks/day Three or more drinks/day	18 83	11.69 53.90 28.57	11.69 65.58 94.16
:	9	5.84	100.00
Total	154	100.00	

- . mi set mlong
- . mi register imputed alcohol
- (9 m=0 obs. now marked as incomplete)
- . mi impute ologit alcohol attack smokes age bmi female hsgrad, /// > add(10) rseed(2232)

Univariate imputation Imputations		=	10
Ordered logistic regression	added	=	10
Imputed: m=1 through m=10	updated	=	0

	Observations per m					
Variable	Complete	Incomplete	Imputed	Total		
alcohol	145	9	9	154		

(complete + incomplete = total; imputed is the minimum across  $\mbox{\it m}$  of the number of filled-in observations.)

## . $\mbox{mi estimate: } \mbox{logit attack smokes age } \mbox{bmi female } \mbox{hsgrad } \mbox{i.alcohol}$

Multiple-imputat:	Imputations	=	10	
Logistic regress:	ion	Number of obs	=	154
		Average RVI	=	0.0139
		Largest FMI	=	0.0769
DF adjustment:	Large sample	DF: min	=	1569.99
		avg	=	3.73e+07
		max	=	1.35e+08
Model F test:	Equal FMI	F( 7,228385.6	) =	2.79
Within VCE type:	MIO	Prob > F	=	0.0067

attack	Coef.	Std. Err.	t	P> t	[95% Conf	. Interval]
smokes age bmi female hsgrad	1.238867 .0359612 .122124 1121927 .1365788	.3625929 .0156974 .0461608 .4223499	3.42 2.29 2.65 -0.27 0.33	0.001 0.022 0.008 0.791 0.741	.5281983 .0051949 .0316505 9399833 6724527	1.949536 .0667274 .2125975 .715598 .9456104
alcohol   Less than 3 drinks/day   Three or more drinks/day   _cons	2666661 2682957 -5.690434	.5692751 .6090222	-0.47 -0.44 -3.33	0.640 0.660 0.001	-1.383099 -1.462878 -9.043387	.8497667 .9262868 -2.337482

Poisson & Nbreg — Count variables. mi impute poisson fills in missing values of a count variable using a Poisson regression imputation method. mi impute nbreg fills in missing values of an overdispersed count variable using a negative binomial regression imputation method (and will usually be better than the Poisson method). This won't mean a lot to you unless/until you have some background in categorical data analysis. For now, we will just briefly note the following:

Variables that count the # of times something happens are common in the Social Sciences.

- Hausman looked at effect of R & D expenditures on # of patents received by US companies
- Grogger examined deterrent effects of capital punishment on daily homicides
- King examined effect of # of alliances on the # of nations at war
- Long looked at # of publications of scientists

Count variables are often treated as though they are continuous and the linear regression model is applied; but this can result in inefficient, inconsistent and biased estimates. Fortunately, there are many models that deal explicitly with count outcomes. These include the Poisson and the (usually superior) Negative Binomial Regression method.

These examples illustrate another feature you can use when imputing: conditional imputation. In this example, most men are coded zero for number of pregnancies they have had. But 7 men, and 3 women, have missing values on the pregnancy variable. Imputing values for men would be a bit silly, as we can be cautiously optimistic that the true value for men on # of pregnancies is zero. With the conditional imputation procedure used below, the 7 men with missing values get assigned zero while the value for # of pregnancies is imputed for the 3 women with missing values.

#### . \*Poisson

. use http://www.stata-press.com/data/r13/mheartpois, clear (Fictional heart attack data; npreg missing)

#### . misstable summarize

				4	Obs<.	
Variable	   Obs=.	Obs>.	Obs<.	Unique   values	Min	Max
npreg	10		144	6	0	5

- . tab2 female npreg, missing
- -> tabulation of female by npreg

			Numbe	r of pregna	ncies			
Gender	0	1	2	3	4	5	-	Total
Male	+   109	0	0	0	0	0	7	116
Female	14 +	8	3	8	1	1	3	38 +
Total	123	8	3	8	1	1	10	154

- . mi set mlong
- . mi register imputed npreg

(10 m=0 obs. now marked as incomplete)

# . mi impute poisson npreg attack smokes age bmi hsgrad, /// > add(20) conditional(if female==1) rseed(2232)

Univariate imputation Imputation = 20
Poisson regression added = 20
Imputed: m=1 through m=20 updated = 0

Conditional imputation:

npreg: incomplete out-of-sample obs. replaced with value  ${\tt 0}$ 

	Observations per m					
Variable	Complete	Incomplete	Imputed	Total		
npreg	144	10	10	154		

(complete + incomplete = total; imputed is the minimum across  ${\tt m}$  of the number of filled-in observations.)

#### . mi estimate: logit attack smokes age bmi female hsgrad npreg

Multiple-imputati	lon estimates	Imputations =	20
Logistic regress:	lon	Number of obs =	154
		Average RVI =	0.0183
		Largest FMI =	0.1143
DF adjustment:	Large sample	DF: min =	1485.04
		avg =	6.31e+09
		max =	2.15e+10
Model F test:	Equal FMI	F( 6,243443.3)=	3.20
Within VCE type:	OIM	Prob > F =	0.0038

attack	Coef.	Std. Err.	t	P> t	[95% Conf.	Interval]
hsgrad   npreg   -	1.248284 .0367254 .121511 0904122 .1155058 0136322 -5.938172	.3609721 .0154729 .0459844 .5574949 .4053936 .276589	3.46 2.37 2.64 -0.16 0.28 -0.05 -3.62	0.001 0.018 0.008 0.871 0.776 0.961 0.000	.5407915 .006399 .0313833 -1.183272 6790511 5561788 -9.157553	1.955776 .0670518 .2116388 1.002448 .9100627 .5289144 -2.718791

# . \*nbreg

- . use http://www.stata-press.com/data/r13/mheartpois, clear (Fictional heart attack data; npreg missing)
- . mi set mlong
- . mi register imputed npreg

(10 m=0 obs. now marked as incomplete)

. mi impute nbreg npreg attack smokes age bmi hsgrad, ///
> add(20) conditional(if female==1) rseed(2232)

Dispersion: mean

 $\ensuremath{\text{npreg:}}$  incomplete out-of-sample obs. replaced with value 0

	Observations per m					
Variable	Complete	Incomplete	Imputed	Total		
npreg	144	10	10	154		

(complete + incomplete = total; imputed is the minimum across m of the number of filled-in observations.)

#### . mi estimate: logit attack smokes age bmi female hsgrad npreg

.0459979

.5452724

.4050585

.269944

.1213715

-.1467292

.1090878

.0268187

age bmi

female hsgrad

npreg

Multiple-imputa			_	ations r of obs	=	20 154	
- 5					ge RVI	=	0.0094
				Large	st FMI	=	0.0617
DF adjustment:	Large sam	ple		DF:	min	=	5047.18
					avg	=	2.26e+10
					max	=	9.44e+10
Model F test:	Equal	FMI		F( 6	5,909484	.4)=	3.23
Within VCE type	:	OIM		Prob :	> F	=	0.0035
attack	Coef.	Std. Err.	t	P> t	[95% (	Conf.	Interval]
smokes	1.245543	.3607367	3.45	0.001	.5385	 126	1.952574
age	.0367316	.0154561	2.38	0.017	.00643	383	.067025

0.10 0.921 -3.61 0.000 -9.147247 -2.710883 \_cons -5.929065 1.64196 -3.61

2.38 0.017

0.27 0.788

0.008

0.788

2.64

-0.27

-1.215486

-.6848123

-.5023888

.0312173

.2115257

.9220277

.9029879

.5560262

# Appendix B: Using Stata 12 for Multiple Imputation for Multiple Variables

Stata 12 introduced several new procedures and commands for multiple imputation. Among these is the mi impute chained command, which supports multivariate Imputation using Chained Equations (ICE). ICE uses iterative procedures to impute missing values when more than one variable is missing. These variables can be of different types, e.g. they might be binary, ordinal or continuous. Variables can have an arbitrary missing-data pattern. mi impute chained has numerous options, and Stata warns that you should do checks to make sure the imputation is working correctly. I am just going to give a simple example adapted from the Stata Manual; you should read the whole manual and/or related literature if you want to do a more detailed analysis of your own.

NOTE: Other commands for imputing multiple variables include mi impute monotone and mi impute mvn. While these can be good (or even better) than mi impute chained, the assumptions required to use these commands are often violated. mi impute mvn may be good if all your imputed variables happen to be continuous, e.g. you don't need to impute any dichotomies, but in practice you often will have mixed types of variables to impute.

First, we retrieve another version of the fictitious heart attack data, in which some data are missing for bmi and age.

The above shows that the data have previously been mi set in mlong format. bmi and age have previously been specified as variables whose missing values are to be imputed. bmi has 28 missing cases, age has 12. M=0 means that no imputed data sets have been computed yet, i.e. you just have the original data.

#### . mi misstable patterns, frequency

Missing-value patterns (1 means complete)

Frequency	Pattern
118	1 1   1 1
24 8 4	1 0 1 0 0
154	

Variables are (1) age (2) bmi

In the above table, a value of 1 indicates not missing, 0 indicates missing. So, we see that there are 118 cases with non-missing values on both age and bmi. Another 24 cases are missing age but not bmi, 8 cases are missing bmi but not age, and 4 cases have missing data on both age and bmi. Next we impute missing values using the mi impute chained command.

#### . mi impute chained (regress) bmi age = attack smokes hsgrad female, add(20) rseed(2232)

Conditional models:

age: regress age bmi attack smokes hsgrad female bmi: regress bmi age attack smokes hsgrad female

Performing chained iterations ...

Multivariate imputation Chained equations Imputed: m=1 through m=20	Imputations = added = updated =	= 20
Initialization: monotone	Iterations = burn-in =	

bmi: linear regression age: linear regression

	Observations per m						
Variable	Complete	Incomplete	Imputed	Total			
bmi age	126 142	28 12	28   12	154 154			

(complete + incomplete = total; imputed is the minimum across mof the number of filled-in observations.)

The (regress) option on the command told Stata that both bmi and age were continuous and that OLS regression should be used for imputation. If, instead, the two variables were dichotomies, we would have specified (logit) instead. (We could have also mixed different types on the same command, we could have used (logit), (regress), and (ologit) for different variables if that was appropriate, see the help for mi impute chained for more complicated examples where

different methods are mixed.) Like before, the add option told Stata to create 20 imputed data sets and the rseed option was used so we can exactly reproduce our results later.

The conditional models show us that age was regressed on every variable (both from the left and right hand side) except itself. The same is true for bmi. This is the default behavior, i.e. all variables except the one being imputed are included in the prediction equation. This will work well in many situations but there are numerous options for changing this behavior if you need more flexibility.

Having done the imputation, we can proceed as before. To get the unimputed results,

. mi xeq 0: logit attack smokes age bmi hsgrad female, nolog

m=0 data:

attack	Coef. +	Std. Err.	z	P>   z	[95% Conf.	Interval]
smokes	1.404968	.4163181	3.37	0.001	.5889992	2.220936
age	.0381199	.0184258	2.07	0.039	.002006	.0742338
bmi	.1004817	.0513924	1.96	0.051	0002455	.2012089
hsgrad	.2705538	.4530665	0.60	0.550	6174402	1.158548
female	.3143023	.4777947	0.66	0.511	6221581	1.250763
_cons	-5.654463	1.879328	-3.01	0.003	-9.337879	-1.971048

The analysis is limited to the 118 cases that had complete data, i.e. we have lost almost a third of the sample (36 cases) because of missing data. With multiple imputation, the results are

#### . mi estimate: logit attack smokes age bmi hsgrad female

Multiple-imput Logistic regre	Numb Aver	itations per of obs rage RVI rest FMI	= 3 = = =	20 154 0.0734 0.2627			
DF adjustment:	: Large sam	mple		DF:	min avg	= =	286.49 41220.53 144975.75
Model F test: Within VCE type	Equal pe:	FMI OIM		F( Prob	max 5,13852. > F		3.46
attack	Coef.	Std. Err.	t	P> t	[95%	Conf.	Interval]
smokes age bmi hsgrad female	1.170431 .0382372 .1038031 .1471189 0986277	.015968 .0519485 .4062852 .419447	3.22 2.39 2.00 0.36 -0.24	0.001 0.017 0.047 0.717 0.814	.4589 .0069 .0015 6492 9207	9384 5538 2007 7355	1.881875 .0695361 .2060523 .9434386 .72348
_cons	-5.560604	1.778105	-3.13	0.002	-9.052	2313	-2.068894

In this particular example, the coefficients and standard errors for the two imputed variables, age and bmi, change little. The other independent variables show modest changes.

# Appendix C (Optional): Approximate Do it Yourself Multiple Imputation for a Single Continuous Variable

Warning: I am NOT recommending that you use the approach shown in this handout! I am just giving it to you for pedagogical purposes. The goal of this handout is to give you a general idea of how multiple imputation works by showing you an approximate procedure by which it can be done without using mi commands. Additional (and somewhat complicated) adjustments should be made to take into account the fact that the regression coefficients from the imputation model are themselves estimated rather than known.

This (roughly) is the formula for an imputed value when a single continuous variable has missing data and you are using regress to impute values for the missing cases.

Imputed Value 
$$X_i = \hat{X}_i + rmse * \varepsilon_i, \ \varepsilon_i \sim N(0,1)$$

An alternative but equivalent formula is

Imputed Value 
$$X_i = \hat{X}_i + \varepsilon_i$$
,  $\varepsilon_i \sim N(0, \text{rmse})$ 

Basically, the procedure for multiple imputation with a single continuous variable is as follows.

- Regress X (the continuous variable with missing values) on the other variables in the imputation model.
- Retrieve the root mean square error (rmse) also known as the standard error of the estimate.
  - O Recall that the standard error of the estimate ( $s_e$ ) indicates how close the actual observations fall to the predicted values on the regression line. About 68.3% of the observations should fall within  $\pm$  1 $s_e$  units of the regression line, 95.4% should fall within  $\pm$  2 $s_e$  units, and 99.7% should fall within  $\pm$  3 $s_e$  units. (At least, that would be true in the population.)
- For those cases where X is missing, compute X hat, i.e. the predicted value for X given the values of the other variables in the equation.
- Add random variability to the imputed X. We do this by multiplying the rmse by a random variable epsilon that has a normal (0, 1) distribution. For example, for the first case, epsilon might equal .5. For the next case, epsilon might equal -1; etc.
- Estimate your analytic model using the imputed X and the other variables in the model.
- Repeat this process M times, where M is the number of imputations. Combine the estimates from the different imputations into a single set of estimates and standard errors. I won't show you how to do this but formulas are available for this purpose.

Here is how you can do this in Stata. Again, the results are approximate. Since the regression coefficients are themselves just estimates, I ought to estimate a different bmihat and rmse for each imputation, rather than using the same values for every imputation. Nonetheless, this should give you the general idea.

We begin by estimating the imputation model for bmi. We then compute bmihat for the cases that are missing bmi. We save the rmse so we can use it in our subsequent calculations.

version 12.1
webuse mheart0, clear
(Fictional heart attack data; bmi missing)
\* Imputation model for bmi
regress bmi attack smokes age hsgrad female

Source	SS	df	MS	Number of obs $F(5, 126)$		132 1.24
Model   Residual	99.5998228 2024.93667	126	19.9199646 16.070926	Prob > F R-squared	=	0.2946
Total	2124.5365			Adj R-squared Root MSE		4.0089
					· – –	

bmi	Coef.	Std. Err.	t	P> t	[95% Conf.	Interval]
attack smokes	1.71356  5153181	.7515229 .761685	2.28 -0.68	0.024	.2263179 -2.02267	3.200801
age	033553	.0305745	-1.10	0.275	0940591	.026953
hsgrad	4674308	.8112327	-0.58	0.566	-2.072836	1.137975
female	3072767	.8074763	-0.38	0.704	-1.905249	1.290695
_cons	26.96559	1.884309	14.31	0.000	23.2366	30.69458

```
. predict bmihat if missing(bmi)
(option xb assumed; fitted values)
(132 missing values generated)
. scalar rmse = e(rmse)
. * As shown in the output, the rmse is a little over 4. To confirm,
. display rmse
4.0088559
```

For the cases with missing data, we now generate 20 random variables, e1-e20, each of which has a normal (0, 1) distribution.

We now generate 20 imputed values for bmi. The imputed values = bmihat + random variability.

We will now show what some of the imputed values look like.

- . \* Compare the imputed values, first 3 imputations
- . list bmihat bmi bmi1 bmi2 bmi3 e1 e2 e3 if missing(bmi)

+	+							+
	bmihat	bmi	bmi1	bmi2	bmi3	e1	e2	e3
8.	24.94037		20.26646	29.12453	23.24085	-1.165896	1.04373	423942
11.	23.73765		21.25652	22.11762	10.19627	618912	4041111	-3.377865
18.	24.9775		29.89542	28.12042	23.199	1.226764	.7839947	4436428
19.	23.67863		29.40268	20.53067	25.60752	1.427849	785253	.4811565
23.	23.9666		28.3487	19.97047	24.61176	1.093105	9968241	.1609331
25.	   26.75463		25.36388	27.01864	26.36398	3469186	.0658563	0974478
34.	25.92009		22.23172	29.00936	27.42771	9200564	.7706099	.376072
38.	25.57589		26.58776	26.44681	22.82028	.2524079	.217249	6873806
47.	24.89569		24.81721	14.63025	29.79111	0195766	-2.560692	1.22115
51.	26.64985		31.43427	33.36421	31.75082	1.193464	1.674883	1.272426
60				10 50001		1 146074	1 414062	7500070
62.	24.2647 24.4496	•	28.86235 26.98282	18.59231	27.27137	1.146874 .6319062	-1.414963 .2248423	.7500079
64.		•		25.35096	22.36778			5193049
66.	26.43693	•	20.43546	27.4691	25.57946	-1.497052	.2574717	2138942
68.	25.05331	•	23.13218	23.87722	22.08071	4792223	2933746	7415092
70.	24.45155 	·	29.27277 	28.11036	17.34405 	1.202641	.912681	-1.772951
107.	23.73576		20.52475	25.12961	30.02304	8009791	.3476921	1.568349
111.	25.13115		20.08341	14.03033	31.53078	-1.259147	-2.769074	1.596376
116.	25.28776		33.68123	21.27818	27.55823	2.093732	-1.00018	.5663627
122.	24.75772		20.78931	18.22538	19.79584	9899129	-1.629478	-1.237731
134.	24.01538		27.33225	28.59109	17.61796	.8273882	1.141402	-1.595822
141.	   25.00403		25.42831	16.91262	22.28859	.1058361	-2.018384	 6773593
150.	24.62909	•	25.80076	23.54937	30.08058	.2922693	2693351	1.359861
+	+							+

As you can see, a different value of bmi is imputed with each imputation. You can easily see where the imputed values came from. For example, for case 8, bmihat = 24.94037 and e1 (which was created to have a normal (0, 1) distribution) equals -1.165896. Since rmse = 4.0089, for case 8 bmi1 = bmihat + rmse \* e1 = 24.94037 + (4.0089 \* -1.165896) = 24.94037 - 4.67396 = 20.266. The 24.94037 is the point estimate for the predicted value while -4.67396 is the random variability added to the point estimate.

- . \* Compare the summary stats, first 3 imputations
- . sum bmihat bmi bmil bmil bmil el el el el, sep(5)

Variable	Obs	Mean	Std. Dev.	Min	Max
bmihat	22	24.92336	.9089033	23.67863	26.75463
bmi	132	25.24136	4.027137	17.22643	38.24214
bmi1	154	25.28435	4.015896	17.22643	38.24214
bmi2	154	25.02149	4.224837	14.03033	38.24214
bmi3	154	25.13252	4.204955	10.19627	38.24214
e1	+	.1543893	1.033153	-1.497052	2.093732
e2		3046026	1.222324	-2.769074	1.674883
e3		1107343	1.230458	-3.377865	1.596376

Even though different values were imputed each time, the means and standard deviations of bmi stay about the same with each imputation. Each of the random error terms has a mean of about 0 and a standard deviation of 1, as they should. The same is true if you look at all 20 imputations.

We will now convert this into an MI data set, so we can use the mi estimate command. The data are currently in a wide format, i.e. we have one record per case, with several variables containing imputed values. The variable bmi contains the original values, while bmi1-bmi20 contain the imputed values. We will also treat e as imputed because its values differ with each imputation. We therefore import as wide, and then convert to the more efficient mlong format.

- . \* Convert to mi format. We will use wide, as each case now has
- . \* one record with several imputed variables
- . mi import wide, imputed(e = e1-e20 bmi = bmi1-bmi20) clear drop
- . \* We can now convert to the more efficient mlong format
- . mi convert mlong, clear

Finally, to do the analytic model,

- . \* Now do the analytic model
- . mi estimate: logit attack smokes age bmi hsgrad female

Multiple-imput	Impu	tations	=	20			
Logistic regression				Numb	Number of obs		154
				Aver	age RVI	=	0.0562
		Larg	Largest FMI		0.2277		
DF adjustment:	Large sam	ole		DF:	min	=	379.99
					avg	=	148236.68
					max	=	509974.85
Model F test:	Equal 1	FMI		F(	5,22572.1)	=	3.61
Within VCE typ	pe: (	MIC		Prob	> F	=	0.0029
attack	Coef.	Std. Err.	t	P> t	[95% Coi	nf.	Interval]
smokes	1.228637	.3653374	3.36	0.001	.512544	5	1.944729
age	.0359155	.0154973	2.32	0.020	.005541	4	.0662897
bmi	.1143556	.0513896	2.23	0.027	.013311	9	.2153993
hsgrad	.1773898	.4080986	0.43	0.664	622483	3	.9772628
female	0972318	.418408	-0.23	0.816	917299	8	.7228363
_cons	-5.758118	1.772189	-3.25	0.001	-9.23646	3	-2.279773

Note that, even though we didn't do the imputations exactly right, we get results that are very similar to the correct results we got earlier in the main part of this handout. (I can't guarantee that this will always be true though). Repeating the earlier results,

Imputations (20		one					
Multiple-imputa		ces	_	ations =			
Logistic regres	ssion			154			
					_	0.0404	
	_	-	_		0.1678		
DF adjustment:	Large samp	ole		DF:		694.17	
					5	115477.35	
	_					287682.25	
Model F test: Equal FMI					5,43531.9) =		
Within VCE type	e: (	MIC		Prob	> F =	0.0022	
attack	Coef.	Std. Err.	t	P> t	[95% Conf.	Interval]	
smokes	1.239172	.3630877	3.41	0.001	.5275236	1.950821	
age	.0354929	.0154972	2.29	0.022	.0051187	.065867	
bmi	.1184188	.0495676	2.39	0.017	.0210985	.2157391	
hsgrad	.185709	.4075301	0.46	0.649	6130435	.9844615	
female	0996102	.4193583	-0.24	0.812	9215408	.7223204	
_cons	-5.845855	1.72309	-3.39	0.001	-9.225542	-2.466168	

Conclusion. Again, I am not recommending do it yourself multiple imputation (unless maybe you are stuck with software that lacks built-in routines). But, by looking at this appendix, multiple imputation should be a little less magical to you. Taking into account the rmse, i.e. how much variability there can reasonably be about the predicted value for a case with missing data, you can generate a series of imputed values which will give you reasonable estimates of the coefficients and the standard errors.

Incidentally, we didn't actually need to compute the e variables. Here is a slightly simpler coding that uses the second variation of the imputed value formula presented earlier. The results are identical.

```
**********

*** Alternative coding; no need to generate the e vars

* MD Part 3: Approximate do it yourself multiple imputation
version 12.1

webuse mheart0, clear

* Imputation model for bmi
regress bmi attack smokes age hsgrad female
predict bmihat if missing(bmi)
scalar rmse = e(rmse)

* As shown in the output, the rmse is a little over 4. To confirm,
display rmse
```

```
* Impute the values for missing cases 20 times
set seed 2232
* Compute 20 imputed values for each case
* Imputed value = bmihat + random variation
forval i = 1/20 {
      quietly clonevar bmi i' = bmi
      quietly replace bmi`i' = bmihat + rnormal(0, rmse) if missing(bmi)
* Compare the imputed values, first 3 imputations
list bmihat bmi bmil bmi2 bmi3 if missing(bmi)
* Compare the summary stats, first 3 imputations
sum bmihat bmi bmi1 bmi2 bmi3 , sep(5)
* Convert to mi format. We will use wide, as each case now has
* one record with several imputed variables
mi import wide, imputed(bmi = bmi1-bmi20) clear drop
* We can now convert to the more efficient mlong format
mi convert mlong, clear
* Now do the analytic model
mi estimate: logit attack smokes age bmi hsgrad female
```