gologit2: Generalized Logistic Regression/ Partial Proportional Odds Models for Ordinal Dependent Variables

Part 1: The gologit model & gologit2 program

Richard Williams Department of Sociology University of Notre Dame Last updated March 27, 2019 https://www.nd.edu/~rwilliam/

Key features of gologit2

- Backwards compatible with Vincent Fu's original gologit program but offers many more features
- Can estimate models that are less restrictive than ologit (whose assumptions are often violated)
- Can estimate models that are more parsimonious than non-ordinal alternatives, such as mlogit

Specifically, gologit2 can estimate:

- Proportional odds models (same as ologit all variables meet the proportional odds/ parallel lines assumption)
- Generalized ordered logit models (same as the original gologit no variables need to meet the parallel lines assumption)
- Partial Proportional Odds Models (some but not all variables meet the pl assumption)

Example: Proportional Odds Assumption Violated

- (Adapted from Long & Freese, 2003 Data from the 1977 & 1989 General Social Survey)
- Respondents are asked to evaluate the following statement: "A working mother can establish just as warm and secure a relationship with her child as a mother who does not work."
 - 1 = Strongly Disagree (SD)
 - 2 = Disagree(D)
 - $\bullet \quad 3 = \text{Agree (A)}$
 - $\mathbf{4} = \text{Strongly Agree (SA)}.$

Explanatory variables are

- yr89 (survey year; 0 = 1977, 1 = 1989)
- $\bullet male (0 = female, 1 = male)$
- white (0 = nonwhite, 1 = white)
- age (measured in years)
- ed (years of education)
- prst (occupational prestige scale).

Ologit results

. ologit warm yr89 male white age ed prst

Ordered logit e Log likelihood		3		LR ch	> chi2	= = = =	2293 301.72 0.0000 0.0504
warm		Std. Err.	Z	P> z	[95% Cor	nf.	Interval]
yr89 male white age	.5239025 7332997 3911595 0216655 .0671728	.0798988 .0784827 .1183808 .0024683 .015975 .0032929	6.56 -9.34 -3.30 -8.78 4.20 1.84	0.000 0.000 0.001 0.000 0.000 0.065	.367303 8871229 6231815 0265032 .0358624 0003813	9 5 2 4	.6805013 5794766 1591374 0168278 .0984831 .0125267
_cut1 _cut2 _cut3	-2.465362 630904 1.261854	.2389126 .2333155 .2340179		(Ancillar	y paramete:	rs)	

Interpretation of ologit results

- These results are relatively straightforward, intuitive and easy to interpret. People tended to be more supportive of working mothers in 1989 than in 1977. Males, whites and older people tended to be less supportive of working mothers, while better educated people and people with higher occupational prestige were more supportive.
- But, while the results may be straightforward, intuitive, and easy to interpret, are they correct? Are the assumptions of the ologit model met? The following Brant test suggests they are not.

Brant test shows assumptions violated

. brant

Brant Test of Variable		Regression 12 p>chi2	Assumption df
	+		
All	49.1	L8 0.000	12
yr89	+ 13.(0.001	2
male	22.2	24 0.000	2
white	1.2	0.531	2
age	7.3	38 0.025	2
ed	4.3	31 0.116	2
prst	4.3	33 0.115	2

A significant test statistic provides evidence that the parallel regression assumption has been violated.

How are the assumptions violated?

• brant, detail

Estimated coefficients from j-1 binary regressions

	y>1	y>2	у>З
yr89	.9647422	.56540626	.31907316
male	30536425	69054232	-1.0837888
white	55265759	31427081	39299842
age	0164704	02533448	01859051
ed	.10479624	.05285265	.05755466
prst	00141118	.00953216	.00553043
_cons	1.8584045	.73032873	-1.0245168

- □ This is a series of binary logistic regressions. First it is 1 versus 2,3,4; then 1 & 2 versus 3 & 4; then 1, 2, 3 versus 4
- □ If proportional odds/ parallel lines assumptions were not violated, all of these coefficients (except the intercepts) would be the same except for sampling variability.

Dealing with violations of assumptions

- □ Just ignore it! (A fairly common practice)
- □ Go with a non-ordinal alternative, such as mlogit
- □ Go with an ordinal alternative, such as the original gologit & the default gologit2 (see next slide)
- Try an in-between approach: partial proportional odds

<pre>. gologit warm yr89 male white age ed prst Generalized Ordered Logit Estimates Number of obs Model chi2(18) Prob > chi2 Log Likelihood = -2820.3109918 Pseudo R2</pre>						
warm	Coef.	Std. Err.	Z	P> z	[95% Conf.	Interval]
 mleq1	-+ 					
yr89	.95575	.1547185	6.18	0.000	.6525073	1.258993
male		.1287712	-2.34	0.019	5533645	0485906
white	5287267	.2278446	-2.32	0.020	975294	0821595
age	0163486	.0039508	-4.14	0.000	0240921	0086051
ed	.1032469	.0247377	4.17	0.000	.0547618	.151732
prst	0016912	.0055997	-0.30	0.763	0126665	.009284
_cons	1.856951	.3872576	4.80	0.000	1.09794	2.615962
nleq2	-+ 					
yr89	.5363707	.0919074	5.84	0.000	.3562355	.716506
male		.0894852	-8.02	0.000	8933827	5426072
white	3492339	.1391882	-2.51	0.012	6220378	07643
age	0249764	.0028053	-8.90	0.000	0304747	0194782
ed	.0558691	.0183654	3.04	0.002	.0198737	.0918646
prst	.0098476	.0038216	2.58	0.010	.0023575	.0173377
_cons	.7198119	.265235	2.71	0.007	.1999609	1.239663
 nleq3	-+ 					
yr89	.3312184	.1127882	2.94	0.003	.1101577	.5522792
male	•	.1217755	-8.91	0.000	-1.324294	8469423
white	3775375	.1568429	-2.41	0.016	684944	070131
age	0186902	.0037291	-5.01	0.000	025999	0113814
ed	.0566852	.0251836	2.25	0.024	.0073263	.1060441
prst	.0049225	.0048543	1.01	0.311	0045918	.0144368
cons	-1.002225	.3446354	-2.91	0.004	-1.677698	3267524

The gologit model

- Note that the gologit results are very similar to what we got with the series of binary logistic regressions and can be interpreted the same way.
- □ The gologit model can be written as

$$P(Y_i > j) = \frac{\exp(\alpha_j + X_i\beta_j)}{1 + [\exp(\alpha_j + X_i\beta_j)]}, j = 1, 2, ..., M - 1$$

- Note that the logit model is a special case of the gologit model, where M = 2. When M > 2, you get a series of binary logistic regressions, e.g. 1 versus 2, 3 4, then 1, 2 versus 3, 4, then 1, 2, 3 versus 4.
- The ologit model is also a special case of the gologit model, where the betas are the same for each j (NOTE: ologit actually reports cut points, which equal the negatives of the alphas used here)

$$P(Y_i > j) = \frac{\exp(\alpha_j + X_i\beta)}{1 + [\exp(\alpha_j + X_i\beta)]}, j = 1, 2, ..., M - 1$$

A key enhancement of gologit2 is that it allows some of the beta coefficients to be the same for all values of j, while others can differ. i.e. it can estimate partial proportional odds models. For example, in the following the betas for X1 and X2 are constrained but the betas for X3 are not.

$$P(Y_i > j) = \frac{\exp(\alpha_j + X_{i_i}\beta_{1} + X_{i_i}\beta_{2} + X_{i_i}\beta_{3_j})}{1 + [\exp(\alpha_j + X_{i_i}\beta_{1} + X_{i_i}\beta_{2} + X_{i_i}\beta_{3_j})]}, j = 1, 2, ..., M - 1$$

gologit2/ partial proportional odds

- Either mlogit or the original gologit can be overkill – both generate many more parameters than ologit does.
 - <u>All</u> variables are freed from the proportional odds constraint, even though the assumption may only be violated by <u>one</u> or a <u>few</u> of them
- gologit2, with the *autofit* option, will <u>only</u> relax the parallel lines constraint for those variables where it is violated

gologit2 with autofit

. gologit2 warm yr89 male white age ed prst, auto lrforce

```
Testing parallel lines assumption using the .05 level of significance...
Step 1: white meets the pl assumption (P Value = 0.7136)
Step 2: ed meets the pl assumption (P Value = 0.1589)
Step 3: prst meets the pl assumption (P Value = 0.2046)
Step 4: age meets the pl assumption (P Value = 0.0743)
Step 5: The following variables do not meet the pl assumption:
    yr89 (P Value = 0.00093)
    male (P Value = 0.00002)
```

If you re-estimate this exact same model with gologit2, instead of autofit you can save time by using the parameter

pl(white ed prst age)

□ gologit2 is going through a stepwise process here. Initially no variables are constrained to have proportional effects. Then Wald tests are done. Variables which pass the tests (i.e. variables whose effects do not significantly differ across equations) have proportionality constraints imposed.

Genera	lized Ordered Logit Estimates	Number of obs LR chi2(10) Prob > chi2		2293 338.30 0.0000
Log li	kelihood = -2826.6182	Pseudo R2	=	0.0000
(2) (3) (4) (5) (6)	<pre>[SD]white - [D]white = 0 [SD]ed - [D]ed = 0 [SD]prst - [D]prst = 0 [SD]age - [D]age = 0 [D]white - [A]white = 0 [D]ed - [A]ed = 0 [D]prst - [A]prst = 0</pre>			

 Internally, gologit2 is generating several constraints on the parameters. The variables listed above are being constrained to have their effects meet the proportional odds/ parallel lines assumptions

(8) [D]age - [A]age = 0

 Note: with ologit, there were 6 degrees of freedom; with gologit & mlogit there were 18; and with gologit2 using autofit there are 10. The 8 d.f. difference is due to the 8 constraints above.

warm	Coef.	Std. Err.	Z	P> z	[95% Conf.	Interval]
SD	+					
yr89	.98368	.1530091	6.43	0.000	.6837876	1.283572
male	3328209	.1275129	-2.61	0.009	5827417	0829002
white	3832583	.1184635	-3.24	0.001	6154424	1510742
age	0216325	.0024751	-8.74	0.000	0264835	0167814
ed	.0670703	.0161311	4.16	0.000	.0354539	.0986866
prst	.0059146	.0033158	1.78	0.074	0005843	.0124135
_cons	2.12173	.2467146	8.60	0.000	1.638178	2.605282
D	+					
yr89	.534369	.0913937	5.85	0.000	.3552406	.7134974
male	6932772	.0885898	-7.83	0.000	8669099	5196444
white	3832583	.1184635	-3.24	0.001	6154424	1510742
age	0216325	.0024751	-8.74	0.000	0264835	0167814
ed	.0670703	.0161311	4.16	0.000	.0354539	.0986866
prst	.0059146	.0033158	1.78	0.074	0005843	.0124135
_cons	.6021625	.2358361	2.55	0.011	.1399323	1.064393
А	+					
yr89	.3258098	.1125481	2.89	0.004	.1052197	.5464
male	-1.097615	.1214597	-9.04	0.000	-1.335671	8595579
white	3832583	.1184635	-3.24	0.001	6154424	1510742
age	0216325	.0024751	-8.74	0.000	0264835	0167814
ed	.0670703	.0161311	4.16	0.000	.0354539	.0986866
prst	.0059146	.0033158	1.78	0.074	0005843	.0124135
_cons	-1.048137	.2393568	-4.38	0.000	-1.517268	5790061

• At first glance, it appears there are just as many parameters as before – but 8 of them are duplicates because of the proportionality constraints that have been imposed.

Interpretation of the gologit2 results

- Effects of the constrained variables (white, age, ed, prst) can be interpreted pretty much the same as they were in the earlier ologit model.
- For yr89 and male, the differences from before are largely a matter of degree. People became more supportive of working mothers across time, but the greatest effect of time was to push people away from the most extremely negative attitudes. For gender, men were less supportive of working mothers than were women, but they were especially unlikely to have strongly favorable attitudes.

Example: Imposing and testing constraints

- Rather than use *autofit*, you can use the *pl* and *npl* parameters to specify which variables are or are not constrained to meet the proportional odds/ parallel lines assumption
 - Gives you more control over model specification & testing
 - Lets you use LR chi-square tests rather than Wald tests
 - Could use BIC or AIC tests rather than chi-square tests if you wanted to when deciding on constraints
 - *pl* without parameters will produce same results as ologit

- Other types of linear constraints can also be specified, e.g. you can constrain two variables to have equal effects
- □ The *store* option will cause the command *estimates store* to be run at the end of the job, making it slightly easier to do LR chi-square contrasts
- Here is how we could do tests to see if we agree with the model produced by *autofit*:

LR chi-square contrasts using gologit2

- . * Least constrained model same as the original gologit
 . quietly gologit2 warm yr89 male white age ed prst, store(gologit)
- . * Partial Proportional Odds Model, estimated using autofit
 . quietly gologit2 warm yr89 male white age ed prst, store(gologit2) autofit
- . * Ologit clone
- . quietly gologit2 warm yr89 male white age ed prst, store(ologit) pl
- . * Confirm that ologit is too restrictive
- . lrtest ologit gologit

Likelihood-ratio test	LR chi2(12) =	49.20
(Assumption: ologit nested in gologit)	Prob > chi2 =	0.0000

. * Confirm that partial proportional odds is not too restrictive . lrtest gologit gologit2

Likelihood-ratio test	LR chi2(8) =	12.61
(Assumption: gologit2 nested in gologit)	Prob > chi2 =	0.1258

Example: Substantive significance of gologit2

- □ gologit2 may be "better" than ologit but substantively, how much should we care?
 - ologit assumptions are often violated
 - Substantively, those violations may not be that important
 but you can't know that without doing formal tests
 - Violations of assumptions can be substantively important. The earlier example showed that the effects of gender and time were not uniform. Also, ologit may hide or obscure important relationships. e.g. using nhanes2f.dta,

health	Coef.	Std. Err.	t	P> t	[95% Conf	. Interval]
poor	 					
female	.1212723	.0975363	1.24	0.223	0776543	.3201989
_cons	2.940598	.0957485	30.71	0.000	2.745317	3.135878
 fair	·+					
female	1833293	.0640565	-2.86	0.007	3139733	0526852
_cons	1.682043	.058651	28.68	0.000	1.562424	1.801663
average	·+					
female	1772901	.0545539	-3.25	0.003	2885535	0660268
_cons	.2938385	.0402766	7.30	0.000	.2116939	.3759831
good	·+					
female	2356111	.05914	-3.98	0.000	356228	1149943
_cons	8493609	.0382026	-22.23	0.000	9272756	7714461

 Females are less likely to report poor health than are males (see the positive female coefficient in the poor panel), but they are also less likely to report higher levels of health (see the negative female coefficients in the other panels), i.e. women tend to be less at the extremes of health than men are. Such a pattern would be obscured in a straight proportional odds (ologit) model.

Other gologit2 features of interest

- The predict command can easily compute predicted probabilities
- Despite its name, gologit2 also supports the logit, probit, cloglog, loglog, and cauchit links.
- As of October 2014, gologit2 supports factor variables, the margins command, and the svy: prefix. (NOTE: Long and Freese 2014 came out before this was done. The example they give on pp. 371-377 can now be done much more easily.)

- The *lrforce* option (now the default) causes Stata to report a Likelihood Ratio Statistic under certain conditions when it ordinarily would report a Wald statistic. Stata is being cautious but LR statistics are appropriate for most common gologit2 models
- gologit2 uses an unconventional but seeminglyeffective way to label the model equations. If problems occur, the *nolabel* option can be used.
- Most other standard options (e.g. *robust*, *cluster*, *level*) are supported.

For more information, see:

http://www.stata-journal.com/article.html?article=st0097

https://www.tandfonline.com/doi/full/10.1080/0022250X.2015.1112384

http://www.statalist.org/forums/forum/general-stata-discussion/general/296459-majorupdate-to-gologit2-now-available

https://www.nd.edu/~rwilliam/gologit2

https://www3.nd.edu/~rwilliam/gologit2/tsfaq.html