Using Stata 11 & higher for Logistic Regression

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NOTE: The routines spost13 and extremes are used in this handout. Use the findit command to locate and install them. See related handouts for the statistical theory underlying logistic regression and for SPSS examples. Most but not all of the commands shown in this handout will also work in earlier versions of Stata, but the syntax is sometimes a little different. The output may also look a little different in different versions of Stata.

This handout will just go over the commands. Other handouts explain the theory and methods.

Commands. Stata and SPSS differ a bit in their approach, but both are quite competent at handling logistic regression. With large data sets, I find that Stata tends to be far faster than SPSS, which is one of the many reasons I prefer it.

Stata has various commands for doing logistic regression. They differ in their default output and in some of the options they provide. My personal favorite is logit.

```
. use "https://www3.nd.edu/~rwilliam/statafiles/logist.dta", clear
. logit grade gpa tuce psi
Iteration 0: log likelihood = -20.59173
Iteration 1: log likelihood = -13.496795
Iteration 2: log likelihood = -12.929188
Iteration 3: log likelihood = -12.889941
Iteration 4: log likelihood = -12.889633
Iteration 5: log likelihood = -12.889633
                                              Number of obs = 32
LR chi2(3) = 15.40
Prob > chi2 = 0.0015
Logit estimates
                                                                  0.3740
                                                            =
                                              Pseudo R2
Log likelihood = -12.889633
 _____
     grade | Coef. Std. Err. z P>|z| [95% Conf. Interval]
 _____
                                                    _____
      gpa |2.8261131.2629412.240.025.35079385.301432tuce |.0951577.14155420.670.501-.1822835.3725988psi |2.3786881.0645642.230.025.292184.465195_cons |-13.021354.931325-2.640.008-22.68657-3.35613
                   _____
```

Note that the log likelihood for iteration 0 is LL_0 , i.e. it is the log likelihood when there are no explanatory variables in the model - only the constant term is included. The last log likelihood reported is LL_M . From these we easily compute

 $DEV_0 = -2LL_0 = -2 * -20.59173 = 41.18$ $DEV_M = -2LL_M = -2 * -12.889633 = 25.78$

Also note that the default output does not include exp(b). To get that, include the or parameter (or = odds ratios = exp(b)).

. logit grade	e gpa tuce psi	, or nolog						
Logistic regression Number of obs = LR chi2(3) = Prob > chi2 =								
Log likelihood	d = -12.889633	}		Pseudo	o R2	= 0.3740		
grade 		Std. Err.	Z	P> z	[95% Con	f. Interval]		
gpa tuce psi _cons	16.87972 1.099832 10.79073 2.21e-06	21.31809 .1556859 11.48743 .0000109	2.24 0.67 2.23 -2.64	0.025 0.501 0.025 0.008	1.420194 .8333651 1.339344 1.40e-10	200.6239 1.451502 86.93802 .03487		

Or, you can use the logistic command, which reports exp(b) (odds ratios) by default:

. logistic grade gpa tuce psi

Logistic regre Log likelihood		3		Number LR chi Prob > Pseudo	> chi2 =	= 32 = 15.40 = 0.0015 = 0.3740
grade	Odds Ratio	Std. Err.	Z	P> z	[95% Con:	f. Interval]
gpa tuce psi _cons	16.87972 1.099832 10.79073 2.21e-06	21.31809 .1556859 11.48743 .0000109	2.24 0.67 2.23 -2.64	0.025 0.501 0.025 0.008	1.420194 .8333651 1.339344 1.40e-10	200.6239 1.451502 86.93802 .03487

[Note: Starting with Stata 12, the exponentiated constant is also reported]. To have logistic instead give you the coefficients,

. logistic grade gpa tuce psi, coef

Logistic regres Log likelihood			LR ch	> chi2	= = =	32 15.40 0.0015 0.3740	
grade	Coef.	Std. Err.	Z	P> z	[95% Cor	nf.	Interval]
gpa tuce psi _cons	2.826113 .0951577 2.378688 -13.02135	1.262941 .1415542 1.064564 4.931325	2.24 0.67 2.23 -2.64	0.025 0.501 0.025 0.008	.3507938 1822835 .29218 -22.6865	5 3	5.301432 .3725988 4.465195 -3.35613

There are various other options of possible interest, e.g. just as with OLS regression you can specify robust standard errors, change the confidence interval and do stepwise logistic regression.

You can further enhance the functionality of Stata by downloading and installing spost13 (which includes several post-estimation commands). Use the findit command to get these. The rest of this handout assumes these routines are installed, so if a command isn't working, it is probably because you have not installed it.

Hypothesis testing. Stata makes you go to a little more work than SPSS does to make contrasts between nested models. You need to use the estimates store and lrtest commands. Basically, you estimate your models, store the results under some arbitrarily chosen name, and then use the lrtest command to contrast models. Let's run through a sequence of models:

. * Model 0: Intercept only . quietly logit grade . est store M0		
. * Model 1: GPA added . quietly logit grade gpa . est store M1		
. * Model 2: GPA + TUCE . quietly logit grade gpa tuce . est store M2		
. * Model 3: GPA + TUCE + PSI . quietly logit grade gpa tuce psi . est store M3		
. * Model 1 versus Model 0 . lrtest M1 M0		
likelihood-ratio test (Assumption: M0 nested in M1)	LR chi2(1) = Prob > chi2 =	
. * Model 2 versus Model 1 . lrtest M2 M1		
likelihood-ratio test (Assumption: M1 nested in M2)	LR chi2(1) = Prob > chi2 =	0.43 0.5096
. * Model 3 versus Model 2 . lrtest M3 M2		
likelihood-ratio test (Assumption: M2 nested in M3)	LR chi2(1) = Prob > chi2 =	6.20 0.0127
. * Model 3 versus Model 0 . lrtest M3 M0		
likelihood-ratio test (Assumption: M0 nested in M3)	LR chi2(3) = Prob > chi2 =	

Also note that the output includes z values for each coefficient (where z = coefficient divided by its standard error). SPSS reports these values squared and calls them Wald statistics. Technically, Wald statistics are not considered 100% optimal; it is better to do likelihood ratio tests, where you estimate the constrained model without the parameter and contrast it with the unconstrained model that includes the parameter.

You can also use the test command for hypothesis testing, but the Wald tests that are estimated by the test command are considered inferior to estimating separate models and then doing LR chi-square contrasts of the results.

```
. test psi
(1) psi = 0
chi2(1) = 4.99
Prob > chi2 = 0.0255
```

Also, Stata 9 added the nestreg prefix. This makes it easy to estimate a sequence of nested models and do chi-square contrasts between them. The lr option tells nestreg to do likelihood ratio tests rather than Wald tests. This can be more time-consuming but is also more accurate. The store option is optional but, in this case, will store the results of each model as m1, m2, etc. This would be handy if, say, you wanted to do a chi-square contrast between model 3 and model 1.

```
. nestreg, lr store(m): logit grade gpa tuce psi
[intermediate output deleted]
  +------------+
  | Block | LL LR df Pr > LR AIC BIC |
  |------|

      1
      -16.2089
      8.77
      1
      0.0031
      36.4178
      39.34928
      |

      2
      -15.99148
      0.43
      1
      0.5096
      37.98296
      42.38017
      |

      3
      -12.88963
      6.20
      1
      0.0127
      33.77927
      39.64221

  +--
. lrtest m3 m1
Likelihood-ratio test
                                                         LR chi2(2) = 6.64
                                                          Prob > chi2 = 0.0362
(Assumption: m1 nested in m3)
```

Also, you don't have to enter variables one at a time; by putting parentheses around sets of variables, they will all get entered in the same block.

```
. nestreg, lr: logit grade gpa (tuce psi) [intermediate output deleted]
```

+	LL	LR	df	Pr > LR	AIC	BIC
	-16.2089 -12.88963	8.77 6.64			36.4178 33.77927	39.34928 39.64221

Note that AIC and BIC are reported. These are also useful statistics for comparing models, but I won't talk about them in this handout. Adding the stats option to lrtest will also cause these statistics to be reported, e.g.

. lrtest m3 m1, stats

Likelihood-ratio (Assumption: ml		in m3)			LR chi2(2) = Prob > chi2 =	
Model		ll(null)	ll(model)	df	AIC	BIC
m1 m3	32	-20.59173	-16.2089 -12.88963	2 4	36.4178 33.77927	39.34928 39.64221

 R^2 analogs and goodness of fit measures. Although it is not clearly labeled, the Pseudo R^2 reported by Stata is McFadden's R^2 , which seems to be the most popular of the many alternative measures that are out there. One straightforward formula is

Pseudo
$$R^2 = 1 - \frac{LL_M}{LL_0} = 1 - \frac{-12.889633}{-20.59173} = 1 - .625961636 = .374$$

You can also get a bunch of other pseudo R^2 measures and goodness of fit statistics by typing fitstat (part of the spost13 routines) after you have estimated a logistic regression:

. fitstat

	logit
Log-likelihood	
Model	-12.890
Intercept-only	-20.592
Chi-square	
Deviance(df=28)	25.779
LR(df=3)	15.404
p-value	0.002
R2	
McFadden	0.374
McFadden(adjusted)	0.180
McKelvey & Zavoina	0.544
Cox-Snell/ML	0.382
Cragg-Uhler/Nagelkerke Efron	0.528
Tjur's D	0.426 0.429
IJUI S D Count	0.813
Count(adjusted)	0.455
IC	+
AIC	33.779
AIC divided by N	1.056
BIC(df=4)	39.642
Variance of	+
e	3.290
y-star	7.210

To get the equivalent of SPSS's classification table, you can use the estat clas command (lstat also works). This command shows you how many cases were classified correctly and incorrectly, using a cutoff point of 50% for the predicted probability.

. lstat

Logistic model for grade

	True		
Classified	D	~ D	Total
+ _	8 3	3 18	11 21
Total	11	21	32
	- if predicted Pr(D) ned as grade != 0	>= .5	
-	edictive value edictive value	Pr(D	D) 72.73% ~D) 85.71% +) 72.73% -) 85.71%
False - rate False + rate	e for true ~D e for true D e for classified + e for classified -		D) 27.27% +) 27.27%
Correctly cl	lassified		81.25%

Predicted values. Stata makes it easy to come up with the predicted values for each case. You run the logistic regression, and then use the predict command to compute various quantities of interest to you.

```
. quietly logit grade gpa tuce psi
. * get the predicted log odds for each case
. predict logodds, xb
. * get the odds for each case
. gen odds = exp(logodds)
. * get the predicted probability of success
. predict p, p
```

. list grade gpa tuce psi logodds odds p

-	+			·			+
	grade 	gpa 	tuce	psi	logodds	odds	p
1. 2. 3. 4. 5.	0 1 0 0	2.06 2.39 2.63 2.92 2.76	22 19 20 12 17	1 1 0 0	-2.727399 -2.080255 -3.685518 -3.627206 -3.603596	.0653891 .1248984 .0250842 .0265904 .0272256	.0613758 .1110308 .0244704 .0259016 .026504
6. 7. 8. 9. 10.	0 0 0 0	2.66 2.89 2.74 2.86 2.83	20 14 19 17 19	0 1 0 0	-3.600734 -1.142986 -3.469803 -3.320985 -3.215453	.0273037 .3188653 .0311232 .0361172 .0401371	.026578 .2417725 .0301837 .0348582 .0385883
11. 12. 13. 14. 15.	 0 0 0 0 1	2.67 2.87 2.75 2.89 2.83	24 21 25 22 27	1 0 0 0 1	8131546 -2.912093 -2.870596 -2.760413 075504	.4434569 .0543618 .0566651 .0632657 .927276	.3072187 .051559 .0536264 .0595013 .481133
16. 17. 18. 19. 20.	0 0 0 1 1	3.1 3.03 3.12 3.39 3.16	21 25 23 17 25	1 0 1 1 1	.1166004 -2.079284 .363438 .5555431 .6667984	1.12367 .1250196 1.438266 1.742887 1.947991	.5291171 .1111266 .5898724 .6354207 .6607859
21. 22. 23. 24. 25.	 0 0 1 0 1	3.28 3.32 3.26 3.57 3.54	24 23 25 23 24	0 0 0 0 1	-1.467914 -1.450027 -1.429278 7434988 1.645563	.2304057 .234564 .2394817 .4754475 5.183929	.1872599 .1899974 .1932112 .3222395 .8382905
26. 27. 28. 29. 30.	 1 0 0 1 1	3.65 3.51 3.53 3.62 4	21 26 26 28 21	1 1 0 1 0	1.670963 1.751095 5710702 2.252283 .2814147	5.317286 5.760909 .5649205 9.509419 1.325003	.8417042 .8520909 .3609899 .9048473 .569893
31. 32.	 1 1	4 3.92	23 29	1 0	2.850418 .8165872	17.295 2.262764	.9453403 .6935114

Hypothetical values. Stata also makes it very easy to plug in hypothetical values. One way to do this in Stata 11 or higher is with the margins command (with older versions of Stata you can use adjust). We previously computed the probability of success for a hypothetical student with a gpa of 3.0 and a tuce score of 20 who is either in psi or not in psi. To compute these numbers in Stata,

. quietly log	ity of getting git grade gpa i, at(gpa = 3	tuce i.psi				
Adjusted prea Model VCE				Numbe	r of obs =	32
Expression at	: Pr(grade), : gpa tuce	predict() = =	3 20			
		Delta-method Std. Err.	Z	P> z	[95% Conf.	Interval]
psi 0 1	.066617	.0611322 .1812458				

This hypothetical, about average student would have less than a 7% chance of getting an A in the traditional classroom, but would have almost a 44% chance of an A in a psi classroom.

Now, consider a strong student with a 4.0 gpa and a tuce of 25:

. margins psi, at(gpa = 4 tuce = 25) Number of obs = 32 Adjusted predictions Model VCE : OIM Expression : Pr(grade), predict() at : gpa = 4 25 _ tuce _____ | Delta-method | Margin Std. Err. z P>|z| [95% Conf. Interval] _____+ psi | 0 | .6597197 .2329773 2.83 0.005 .2030926 1.116347 1 | .9543808 .0560709 17.02 0.000 .8444837 1.064278 _____

This student has about a 2/3 chance of an A in a traditional classroom, and a better than 95% chance of an A in psi.

If you want the log odds instead of the probabilities, give commands like

. margins psi, at(gpa = 4 tuce = 25) predict(xb)

Adjusted prea Model VCE					Number	of	obs =	32
Expression at		Linear prec gpa tuce	diction (log = =	odds), 4 25	predict(xb)			
	 	Margin	Delta-metho Std. Err.		P> z	[9	95% Conf.	. Interval]
psi 0 1		.6620453	1.037809 1.287859		4 0.524 6 0.018		.372022 5165768	

To get the odds, you need to exponentiate the log odds. You can do that via

. margins psi, at(gpa = 4 tuce = 25) expression(exp(predict(xb)))								
Adjusted pred Model VCE				Numbe	r of obs =	32		
Expression	: exp(predict	(xb))						
at	: gpa	=	4					
	tuce	=	25					
psi 0	Margin 	Delta-method Std. Err. 2.012055			[95% Conf. -2.004802			
1	20.92057	26.94274	0.78	0.437	-31.88622	73.72737		

Long & Freese's spost commands provide several other good ways of performing these sorts of tasks; see, for example, the mtable and mchange commands.

Stepwise Logistic Regression. This works pretty much the same way it does with OLS regression. However, by adding the lr parameter, we force Stata to use the more accurate (and more time-consuming) Likelihood Ratio tests rather than Wald tests when deciding which variables to include. (Note: stepwise is available in earlier versions of Stata but the syntax is a little different.)

. sw, pe(.05) lr: logit grade gpa tuce psi

LR test p = 0.0031 < 0. p = 0.0130 < 0.	0500 addir	h with empty ng gpa ng psi	model				
Logistic regression				Number of obs = LR chi2(2) = Prob > chi2 =		32 14.93 0.0006	
Log likelihood = -13.126573				Pseudo R2 =		0.3625	
grade +	Coef.	Std. Err.	Z	P> z	[95% Cc	onf.	Interval]
gpa psi		1.22285 1.040784 4.212904	2.51 2.25 -2.75	0.012 0.025 0.006	.666625 .297875 -19.8587	5	5.46011 4.377676 -3.344425

Diagnostics. The predict command lets you compute various diagnostic measures, just like it did with OLS. For example, the predict command can generate a standardized residual. It can also generate a deviance residual (the deviance residuals identify those cases that contribute the most to the overall deviance of the model.) [WARNING: SPSS and Stata sometimes use different formulas and procedures for computing residuals, so results are not always identical across programs.]

```
. * Generate predicted probability of success
. predict p, p
. * Generate standardized residuals
. predict rstandard, rstandard
. * Generate the deviance residual
. predict dev, deviance
. * Use the extremes command to identify large residuals
. extremes rstandard dev p grade gpa tuce psi
   +-----+
   | obs: rstandard dev p grade gpa tuce psi |
   |-----|

      27.
      -2.541286
      -1.955074
      .8520909
      0
      3.51
      26
      1

      18.
      -1.270176
      -1.335131
      .5898724
      0
      3.12
      23
      1

      16.
      -1.128117
      -1.227311
      .5291171
      0
      3.1
      21
      1

      28.
      -.817158
      -.9463985
      .3609899
      0
      3.53
      26
      0

      24.
      -.7397601
      -.8819993
      .3222395
      0
      3.57
      23
      0

   +-----+

      19.
      .8948758
      .9523319
      .6354207
      1
      3.39
      17
      1

      30.
      1.060433
      1.060478
      .569893
      1
      4
      21
      0

      15.
      1.222325
      1.209638
      .481133
      1
      2.83
      27
      1

      23.
      2.154218
      1.813269
      .1932112
      1
      3.26
      25
      0

      2.
      3.033444
      2.096639
      .1110308
      1
      2.39
      19
      1

   +------
```

The above results suggest that cases 2 and 27 may be problematic. Several other diagnostic measures can also be computed.

Multicollinearity. Multicollinearity is a problem of the X variables, and you can often diagnose it the same ways you would for OLS. Phil Ender's collin command is very useful for this:

. collin gpa tuce psi if !missing(grade)

Robust standard errors. If you fear that the error terms may not be independent and identically distributed, e.g. heteroscedasticity may be a problem, you can add the robust parameter just like you did with the regress command. Or, vce (robust) also works.

```
. logit grade gpa tuce psi, robust
```

```
Iteration 0: log pseudo-likelihood = -20.59173
Iteration 1: log pseudo-likelihood = -13.496795
Iteration 2: log pseudo-likelihood = -12.929188
Iteration 3: log pseudo-likelihood = -12.889941
Iteration 4: log pseudo-likelihood = -12.889633
Iteration 5: log pseudo-likelihood = -12.889633
                                          Number of obs=32Wald chi2(3)=9.36Prob > chi2=0.0249Pseudo R2=0.3740
Logit estimates
Log pseudo-likelihood = -12.889633
_____
         1
                       Robust
    grade | Coef. Std. Err. z P>|z| [95% Conf. Interval]
gpa2.8261131.2878282.190.028.30201645.35021tuce.0951577.11980910.790.427-.1396639.3299793psi2.378688.97985092.430.015.45821524.29916_cons-13.021355.280752-2.470.014-23.37143-2.671264
```

Note that the standard errors have changed very little. However, Stata now reports "pseudolikelihoods" and a Wald chi-square instead of a likelihood ratio chi-square for the model. I won't try to explain why. Stata will surprise you some times with the statistics it reports, but it generally seems to have a good reason for them (although you may have to spend a lot of time reading through the manuals or the online FAQs to figure out what it is.)

Additional Information. Long and Freese's spost13 routines include several other commands that help make the results from logistic regression more interpretable. Their book is very good:

<u>Regression Models for Categorical Dependent Variables Using Stata, Third Edition</u>, by J. Scott Long and Jeremy Freese. 2014.

The notes for my Soc 73994 class, <u>Categorical Data Analysis</u>, contain a lot of additional information on using Stata for logistic regression and other categorical data techniques. See

https://www3.nd.edu/~rwilliam/stats3/index.html