# EE 30372, Spring 2006 <br> Final Exam 

10-11 May, 2005

Show all your work and your answers clearly on the test pages. In any plots and sketches, label and include units (if possible) on anything that might be of interest. You are each allowed one two-sided 8.5 by 11 inch page of formulae for reference. Calculators may be used only for simple trigonometric and (complex variable) arithmetic operations. For full credit, simplify your answers as much as possible.

Problem 1 (40) $\qquad$

Problem 2 (20)

Problem 3 (35) $\qquad$

Problem 4 (20) $\qquad$

Total (115)

Name

1. Short answers (5 pts. each):
(a) A shunt-wound DC motor with armature resistance of $1 \Omega$ and field resistance of $3 \Omega$ runs at 1500 rpm clockwise with 75 V applied to its terminals. What is its rotation when the voltage is reversed to -75 V ?
(b) Write the transform matrix we would need to represent three-phase voltages $V_{A}, V_{B}$ and $V_{C}$ as a function of the symmetric components $V_{C 0}, V_{C 1}$ and $V_{C 2}$
(c) Sketch a circuit containing a $5 \Omega$ resistor, an inductor and a 25 micro-farad capacitor which will have power factor of 1.0 when connected to a 60 Hz source. All elements must carry current. Specify the inductor's size.
(d) A three-phase, $\Delta$-connected generator has internal impedance of $2.0 \angle 60^{\circ}$ and internal generated voltage of 480 V . The generator suffers a spectacular triple line-to-ground fault; what are the fault currents in the $A, B, C$ leads?
(e) You have a "black box" power system with four ports, and unknown interconnections inside. Your goal is to find the system impedance matrix by using an adjustable current source and a voltmeter. Imagine that you must pay a fee of $\$ 1$ each time you measure a voltage. What is the minimum you can spend to find all the entries in the matrix? Give brief justification for your answer.
(f) If a single-phase load is consuming 15 kWatts at 240 V AC and has power factor 0.7 , what is the rms current flowing to the load?
(g) A particular region of a three-phase power system has $S_{\text {base }}=10 M V A, V_{\text {base }}($ line line $)=4160 \mathrm{~V}$. One-line analysis in pu has a generator in the region supplying real power of 0.2 pu. How many Watts of real power is the three-phase generator supplying?
(h) You find that a 100 Watt, 120 V bulb is just right for your room when connected to a 120 V outlet. What wattage of 120 V bulb should you use to get the same amount of light when connected to a 240 V source? (Don't worry here about just how long the bulb would last at 240 V .)
2. ( 20 pts .) A permanent magnet DC motor with armature resistance $R_{A}$ of $2 \Omega$ runs at 1000 rpm under load with input terminal voltage of 100 V , drawing current of 10 A . Suppose induced torque does not change, but the input voltage is reduced to 50 V . What will the motor's rotational speed be?
3. The components of the power system below have the following ratings:

Generator $1\left(G_{1}\right)$ :
$100 \mathrm{MVA}, 12.4 \mathrm{kV}, X_{1}=0.2 \mathrm{pu}, X_{2}=0.2 \mathrm{pu}, X_{q 0}=0.2 \mathrm{pu}$
Motor 2( $M_{2}$ ):
Motor $3\left(M_{3}\right)$ :
All $Y-\Delta$ transformers:
All $\Delta-\Delta$ transformers:
Line 1:
Line 2:
$100 \mathrm{MVA}, 13.8 \mathrm{kV}, X_{1}=0.1 \mathrm{pu}, X_{2}=0.1 \mathrm{pu}, X_{g 0}=0.1 \mathrm{pu}$ $100 \mathrm{MVA}, 13.8 \mathrm{kV}, X_{1}=0.05 \mathrm{pu}, X_{2}=0.1 \mathrm{pu}, X_{g 0}=0.1 \mathrm{pu}$ $100 \mathrm{MVA}, 13.8 / 138 \mathrm{kV}, X_{1}=0.05 \mathrm{pu}, X_{2}=0.1 \mathrm{pu}, X_{0}=0.05 \mathrm{pu}$ $100 \mathrm{MVA}, 13.8 / 138 \mathrm{kV}, X_{1}=0.1 \mathrm{pu}, X_{2}=0.1 \mathrm{pu}, X_{0}=0.05 \mathrm{pu}$ $\mathrm{X}=15 \Omega$
$\mathrm{X}=30 \Omega$

(a) (20 pts.) Find the first rows of the bus admittance matrices for the positive and zerosequence components in this system, in pu with $S_{\text {base }}$ of 100 MVA and $V_{\text {base }}$ of 12.4 kV at bus 1 .
(b)(15 pts.) A single line-to-ground (phase A) fault occurs at bus 2. Assuming all bus voltages were at $1 \angle 0^{\circ}$ before the fault, find the fault currents flowing at this bus, and the voltages of all three phases at bus 2 after the fault.
4. (20 pts.) Suppose we have the following bus impedance matrix for a 3-phase power system. A generator maintaining 1 volt at its output terminals is applied to bus 3 ; no other sources are connected. Find the voltages at the other two buses. (You may assume that the internal impedance of the generator does not affect the impedance matrix.

$$
\mathbf{Z}_{\text {bus }}=\left(\begin{array}{ccc}
j 0.2 & 0 & j 0.1 \\
0 & j 0.3 & j 0.2 \\
j 0.1 & j 0.2 & j 0.3
\end{array}\right)
$$

