

Project 3, due on 04/12.

Problem. Implementing Arnoldi algorithm.

Step 1: Generate a 50×50 strictly diagonally dominant matrix. Do this by modifying the code `my_io.c` at:

`/afs/crc.nd.edu/user/z/zxu2/Public/ACMS40212-S12/col_decomp_mat_vec_multi/data_gen`

The current `my_io.c` code generates a matrix with randomly filled entries.

Step 2: Implement your stable Arnoldi algorithm. You can simply use unit vector \mathbf{e}_1 as \mathbf{v}_1 .

Let the dimension k of the Krylov subspace be much less than the dimension of the matrix. For instance, let $k = 20$.

Hand-In.

1. The hardcopy of your source code (Also send the source code to me by email. Please use the email title: Project 3: your name).
2. A report which contains validation of results and a description of your algorithm using the pseudo code language.
3. Validation. Since now you have the orthonormal basis Q of the Krylov subspace $\text{span}\{\mathbf{r}^{(0)}, A\mathbf{r}^{(0)}, A^2\mathbf{r}^{(0)}, \dots, A^{k-1}\mathbf{r}^{(0)}\}$, generate a vector \mathbf{b} in this subspace by doing a linear combination of $\mathbf{r}^{(0)}, A\mathbf{r}^{(0)}, A^2\mathbf{r}^{(0)}, \dots, A^{k-1}\mathbf{r}^{(0)}$, then solve $Q\mathbf{x} = \mathbf{b}$ for \mathbf{x} by $\mathbf{x} = Q^T\mathbf{b}$ to see if \mathbf{x} agrees with coefficients of the linear combination to generate \mathbf{b} .

Remark: for parallel implementation of GMRES method, see

(a) H.F. Walker. Implementation of the GMRES method using Householder transformations, SIAM Journal on Scientific and Statistical Computing, 1988

(b) J. Erhel. A parallel GMRES version for general sparse matrices, Electronic Transactions on Numerical Analysis, 1995