

Name: _____

Instructor: _____

Math 20550, Old Exam 2
October 26, 2017

- The Honor Code is in effect for this examination. All work is to be your own.
- No calculators.
- The exam lasts for 1 hour and 15 minutes..
- Be sure that your name is on every page in case pages become detached.
- Be sure that you have all 9 pages of the test.
- Each multiple choice question is 6 points, each partial credit problem is 12 points.
You will receive 4 extra points.

PLEASE MARK YOUR ANSWERS WITH AN X, not a circle!					
1.	(a)	(b)	(c)	(d)	(e)
2.	(a)	(b)	(c)	(d)	(e)
.....					
3.	(a)	(b)	(c)	(d)	(e)
4.	(a)	(b)	(c)	(d)	(e)
.....					
5.	(a)	(b)	(c)	(d)	(e)
6.	(a)	(b)	(c)	(d)	(e)
.....					
7.	(a)	(b)	(c)	(d)	(e)
8.	(a)	(b)	(c)	(d)	(e)
.....					
9.	(a)	(b)	(c)	(d)	(e)
10.	(a)	(b)	(c)	(d)	(e)

Please do NOT write in this box.

Multiple Choice _____

11. _____

12. _____

13. _____

Extra Points. 4 _____

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Multiple Choice

1.(6 pts) Find the absolute maximum and minimum of $f(x, y) = 4y + x^2 - 2x + 1$ on the closed triangular region with vertices $(0, 0)$, $(2, 0)$ and $(0, 2)$.

- (a) maximum value = 9, minimum value = 0
- (b) maximum value = 4, minimum value = 0
- (c) maximum value = 8, minimum value = 1
- (d) maximum value = 1, minimum value = 0
- (e) maximum value = 10, minimum value = -1

2.(6 pts) Find the equation of the tangent plane to the surface $xz + \ln(2x + y) = 5$ at the point $(-1, 3, -5)$.

- (a) $3x + y - z - 5 = 0$
- (b) $-4x + y - z - 4 = 0$
- (c) $4x - y + z + 12 = 0$
- (d) $5x - y + z + 13 = 0$
- (e) $-3x + y - z - 11 = 0$

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3.(6 pts) If $z = f(x, y)$, where f is differentiable, and $x = g(t), y = h(t), g(1) = 3, h(1) = 4, g'(1) = -2, h'(1) = 5, f_x(3, 4) = 7$ and $f_y(3, 4) = 6$. Find dz/dt when $t = 1$.

- (a) 13 (b) 44 (c) 32 (d) 23 (e) 16

4.(6 pts) Find the directional derivative of the function $f(x, y) = x^2 + y^3$ at the point $(2, 1)$ in the direction $\langle 1, 1 \rangle$

- (a) $\frac{3}{\sqrt{2}}$
(b) 7
(c) None of the above
(d) $\frac{7}{\sqrt{2}}$
(e) 3

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5.(6 pts) For a function $f(x, y)$, suppose that $f_{xx} = x^2$ and $D(x, y) = f_{xx}f_{yy} - f_{xy}^2 = x^2y^2 - 2$. Which is true for the points $P(1, 1)$ and $Q(1, 2)$ where P and Q are critical points of f .

- (a) P is a local min and Q is a local max.
- (b) P is a local max and Q is a local min.
- (c) P is a saddle point and Q is a local min.
- (d) None of the above
- (e) P is a saddle point and Q is a local max.

6.(6 pts) What is the equation of the tangent line to the curve of intersection between the two surfaces defined by $z = x^2 + y^2$ and $x^2 + 2y^2 + z^2 = 7$ at the point $(-1, 1, 2)$.

- (a) $\langle x, y, z \rangle = \langle -1, 1, 2 \rangle + t\langle 1, 2, 1 \rangle$
- (b) $\langle x, y, z \rangle = \langle -1, 1, 2 \rangle + t\langle 12, 10, -4 \rangle$
- (c) $\langle x, y, z \rangle = \langle -1, 1, 2 \rangle + t\langle -2, 2, 1 \rangle$
- (d) None of the above
- (e) $\langle x, y, z \rangle = \langle -1, 1, 2 \rangle + t\langle -2, 4, 4 \rangle$

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7.(6 pts) Find the maximum rate of change of $f(x, y) = 3e^{xy}$ at the point $(2, 0)$ and the direction in which it occurs.

- (a) Rate of change = $\sqrt{3}$ in the direction $\langle 1, 0 \rangle$
- (b) Rate of change = 36 in the direction $\langle -1, 0 \rangle$
- (c) Rate of change = 3 in the direction $\langle 1, 1 \rangle$
- (d) Rate of change = $\sqrt{6}$ in the direction $\langle 1, -1 \rangle$
- (e) Rate of change = 6 in the direction $\langle 0, 1 \rangle$

8.(6 pts) Find absolute maximum and minimum of $3x - y - 3z$ subject to the constraints $x + y - z = 0$ and $x^2 + 2z^2 = 6$.

- (a) Max=12, Min=-12 (b) Max=6, Min=-1 (c) Max=15, Min=5
- (d) Max= $3\sqrt{5}$, Min=0 (e) Max=5, Min= $-3\sqrt{5}$

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9.(6 pts) Evaluate the iterated integral

$$\int_0^2 \int_y^{2y} 2xy \, dx \, dy.$$

- (a) 5 (b) 3 (c) 12 (d) 4 (e) 2

10.(6 pts) Which integral represents the volume of the solid below the plane $x + y + z = 3$ and over the rectangle $[0, 2] \times [0, 1]$.

- (a) $\int_0^1 \int_0^2 3 - x - y \, dy \, dx$ (b) $\int_0^1 \int_0^2 x + y + z \, dy \, dx$
(c) $\int_0^2 \int_0^1 x + y + z \, dy \, dx$ (d) $\int_0^2 \int_0^1 1 \, dy \, dx$
(e) $\int_0^2 \int_0^1 3 - x - y \, dy \, dx$

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Partial Credit

You must show your work on the partial credit problems to receive credit!

11.(12 pts) Find all critical points of $f(x, y) = x^3 - xy + y^2/2$ and classify them using the second derivative test.

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12.(12 pts) Use Lagrange Multipliers to find extrema values of the function $f(x, y) = 2x^3 - y^3$ subject to the constraint $x^2 + y^2 = 5$.

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13.(12 pts) Find the volume of the solid that lies under the graph of $f(x, y) = xe^{xy}$ and above the rectangle $R = \{(x, y) \mid 0 \leq x \leq 1, 0 \leq y \leq 1\}$.