

Name: \_\_\_\_\_

Instructor: \_\_\_\_\_

**Math 10550, Exam III**  
**November 13, 2012**

- The Honor Code is in effect for this examination. All work is to be your own.
- No calculators.
- The exam lasts for 1 hour and 15 min.
- Be sure that your name is on every page in case pages become detached.
- Be sure that you have all 9 pages of the test.

PLEASE MARK YOUR ANSWERS WITH AN X, not a circle!					
1.	(a)	(b)	(c)	(d)	(e)
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9.	(a)	(b)	(c)	(d)	(e)
10.	(a)	(b)	(c)	(d)	(e)

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<b>Multiple Choice</b>	_____
11.	_____
12.	_____
13.	_____
Total	_____

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### Multiple Choice

1.(6 pts.) In finding an approximate solution to the equation  $x^4 + x - 2 = 0$  using Newton's Method with initial approximation  $x_1 = -1$ , what is  $x_2$ ?

- (a)  $-\frac{1}{3}$       (b)  $-\frac{1}{5}$       (c)  $-\frac{5}{2}$       (d)  $-\frac{5}{3}$       (e)  $-\frac{7}{3}$

2.(6 pts.) If  $f'(x) = \sqrt{x} + \frac{1}{\sqrt{x}}$  and  $f(1) = \frac{8}{3}$ , find  $f(4)$ .

- (a)  $\frac{27}{3}$       (b)  $\frac{25}{3}$       (c)  $\frac{26}{3}$       (d)  $\frac{24}{3}$       (e)  $\frac{28}{3}$

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3.(6 pts.) Calculate the following indefinite integral

$$\int (4 - 3t^2)(4t + 1)dt.$$

- (a)  $-36t^2 + 16 + C$
- (b)  $-2t^5 - t^4 + 8t^3 + 4t^2 + C$
- (c)  $-3t^4 - t^3 + 8t^2 + 4t + C$
- (d)  $-12t^4 - 3t^3 + 16t^2 + 4t + C$
- (e)  $-\frac{3}{4}t^4 - t^3 + 8t^2 + 4t + C$

4.(6 pts.) Let  $f(x) = \int_{\sin x}^2 \frac{1}{\sqrt{t^4 + 6}} dt$ . What is  $f'(x)$ ?

- (a)  $\frac{1}{\sqrt{\sin^4 x + 6}}$
- (b)  $\frac{-1}{\sqrt{\sin^4 x + 6}}$
- (c)  $\frac{\cos x}{\sqrt{\sin^4 x + 6}}$
- (d)  $\frac{-2 \sin^3 x}{\sqrt{(\sin^4 x + 6)^3}}$
- (e)  $\frac{-\cos x}{\sqrt{\sin^4 x + 6}}$

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5.(6 pts.) Evaluate the indefinite integral

$$\int \frac{\sec^2(\sqrt{x})}{\sqrt{x}} dx.$$

(a)  $\tan^2(\sqrt{x}) + C$

(b)  $\frac{1}{2} \sec(\sqrt{x}) \tan(\sqrt{x}) + C$

(c)  $2 \tan(\sqrt{x}) + C$

(d)  $2 \sec(\sqrt{x}) \tan(\sqrt{x}) + C$

(e)  $\frac{1}{2} \tan(\sqrt{x}) + C$

6.(6 pts.) Evaluate the definite integral  $\int_0^1 x^2(\sqrt{x} + 3) dx.$

(a)  $\frac{5}{2}$

(b)  $\frac{9}{7}$

(c)  $\frac{7}{5}$

(d)  $\frac{5}{3}$

(e)  $\frac{9}{2}$

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7.(6 pts.) Calculate the definite integral

$$\int_{-1}^2 |x| dx.$$

(a)  $\frac{5}{2}$

(b) 1

(c)  $\frac{9}{2}$

(d)  $\frac{7}{2}$

(e)  $\frac{3}{2}$

8.(6 pts.) Evaluate the definite integral

$$\int_0^\pi (2x + 1) \sin(x^2 + x) dx.$$

(a)  $2 \cos(\pi^2 + \pi) - 2$

(b)  $\sin(\pi^2 + \pi) - 1$

(c)  $1 - \cos(\pi^2 + \pi)$

(d)  $\cos(\pi + 1) - \cos(\pi^2)$

(e) 0

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9.(6 pts.) Find the equation of the slant asymptote of the curve

$$y = \frac{2x^3 - 3x^2 + 4x + 6}{x^2 + 2x}.$$

(a)  $y = 2x + 1$

(b)  $y = 2x - 7$

(c)  $y = 2x + 4$

(d)  $y = 2x - 3$

(e)  $y = 0$

10.(6 pts.) Let  $A = \int_0^1 \frac{x}{x+1} dx$ . Which of the following is true of  $A$ ?

(a)  $A$  is undefined

(b)  $-\frac{1}{4} \leq A \leq 0$

(c)  $\frac{1}{2} \leq A \leq \frac{3}{4}$

(d)  $0 \leq A \leq \frac{1}{2}$

(e)  $A = \frac{1}{4}$

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### Partial Credit

You must show your work on the partial credit problems to receive credit!

11.(14 pts.) (1) Using the definition of the definite integral, evaluate

$$\int_0^2 1 + x^2 dx.$$

Hint:

$$1^2 + 2^2 + \cdots + n^2 = \frac{1}{6}n(n+1)(2n+1).$$

(2) Verify your result using the Fundamental Theorem of Calculus.

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**12.**(13 pts.) A ball is thrown upward from a height of 32 feet above the ground on the planet Calculuto, with an initial velocity of 12 feet per second. The velocity of the ball at time  $t$  is  $12 - 4t$  feet per second.

(1) Find  $s(t)$ , the function giving the height of the ball at time  $t$ .

(2) How long will the ball take to reach the ground?

(3) How high will the ball go?



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**13.**(13 pts.) An open rectangular box (a box with no top) with square base and with a volume of 27 cubic feet is needed. Material for the base costs \$2 per square foot, and material for the sides costs \$1 per square foot. Determine the dimensions of the box that will minimize the cost of materials. *Justify that your answer is a minimum.*

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