

Name: \_\_\_\_\_

Instructor: \_\_\_\_\_

**Math 10-350, Calculus A**  
**Fall Semester 2006**  
**Exam 3**  
**Tuesday, November 28: 8:00–9:15 a.m.**

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This Examination contains **16** problems, worth a total of **100** points, on **9** sheets of paper including the front cover. The first **12** problems (Section A) are multiple choice with no partial credit, and each is worth **5** points. Record your answers to these problems by placing an  $\times$  through one letter for each problem below:

- |    |                                     |                            |                                     |                                     |                                     |     |                                     |                                     |                                     |                                     |                                     |
|----|-------------------------------------|----------------------------|-------------------------------------|-------------------------------------|-------------------------------------|-----|-------------------------------------|-------------------------------------|-------------------------------------|-------------------------------------|-------------------------------------|
| 1. | <input type="checkbox"/> a          | <input type="checkbox"/> b | <input checked="" type="checkbox"/> | <input type="checkbox"/> d          | <input type="checkbox"/> e          | 7.  | <input type="checkbox"/> a          | <input type="checkbox"/> b          | <input type="checkbox"/> c          | <input type="checkbox"/> d          | <input checked="" type="checkbox"/> |
| 2. | <input checked="" type="checkbox"/> | <input type="checkbox"/> b | <input type="checkbox"/> c          | <input type="checkbox"/> d          | <input type="checkbox"/> e          | 8.  | <input type="checkbox"/> a          | <input type="checkbox"/> b          | <input checked="" type="checkbox"/> | <input type="checkbox"/> d          | <input type="checkbox"/> e          |
| 3. | <input type="checkbox"/> a          | <input type="checkbox"/> b | <input type="checkbox"/> c          | <input checked="" type="checkbox"/> | <input type="checkbox"/> e          | 9.  | <input type="checkbox"/> a          | <input checked="" type="checkbox"/> | <input type="checkbox"/> c          | <input type="checkbox"/> d          | <input type="checkbox"/> e          |
| 4. | <input type="checkbox"/> a          | <input type="checkbox"/> b | <input checked="" type="checkbox"/> | <input type="checkbox"/> d          | <input type="checkbox"/> e          | 10. | <input type="checkbox"/> a          | <input type="checkbox"/> b          | <input type="checkbox"/> c          | <input checked="" type="checkbox"/> | <input type="checkbox"/> e          |
| 5. | <input type="checkbox"/> a          | <input type="checkbox"/> b | <input type="checkbox"/> c          | <input type="checkbox"/> d          | <input checked="" type="checkbox"/> | 11. | <input type="checkbox"/> a          | <input type="checkbox"/> b          | <input checked="" type="checkbox"/> | <input type="checkbox"/> d          | <input type="checkbox"/> e          |
| 6. | <input type="checkbox"/> a          | <input type="checkbox"/> b | <input checked="" type="checkbox"/> | <input type="checkbox"/> d          | <input type="checkbox"/> e          | 12. | <input checked="" type="checkbox"/> | <input type="checkbox"/> b          | <input type="checkbox"/> c          | <input type="checkbox"/> d          | <input type="checkbox"/> e          |

The last **4** problems (Section B) are partial credit problems worth **10** points each. For these problems, **show all your work** and **clearly mark your answers** on the page. Books and notes are not allowed. You may not use your calculator.

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**Sign the pledge:** “On my honor, I have neither given nor received unauthorized aid on this Exam”:

\_\_\_\_\_

**GOOD LUCK!**

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1.  a  b  c  d  e

2.  a  b  c  d  e

3.  a  b  c  d  e

4.  a  b  c  d  e

5.  a  b  c  d  e

6.  a  b  c  d  e

7.  a  b  c  d  e

8.  a  b  c  d  e

9.  a  b  c  d  e

10.  a  b  c  d  e

11.  a  b  c  d  e

12.  a  b  c  d  e

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### Part A: Multiple Choice Problems

1. (5 pts.) Let  $x, y$  be positive numbers whose product is 100. The minimum of their sum  $x + y$  is:

- a) 50      b) 10      c) 20      d) 30      e) 40

2. (5 pts.) Compute the sum

$$\sum_{i=1}^{200} \frac{i+5}{100}.$$

- a) 211      b) 201      c) 205      d) 206      e) 216

3. (5 pts.) Find the Riemann sum for  $f(x) = 2 + x^2$ ,  $0 \leq x \leq 3$ , with three subintervals of equal length and using their right endpoints.

- a) 25      b) 36      c) 2      d) 20      e) 15

4. (5 pts.) Find  $x_3$  by completing two iterations of Newton's Method for the function  $y = x^3$  using the initial value  $x_1 = 3$ .

- a)  $x_3 = \frac{5}{2}$       b)  $x_3 = 10/3$       c)  $x_3 = \frac{4}{3}$       d)  $x_3 = 1$       e)  $x_3 = 2$

5. (5 pts.) For the function  $y = 2\sqrt{x}$  find the differential  $dy$  when  $x = 4$  and  $dx = 0.2$ .

- a)  $dy = 0.2$       b)  $dy = 0.3$       c)  $dy = 0.4$   
d)  $dy = 0.5$       e)  $dy = 0.1$

6. (5 pts.) The  $\lim_{n \rightarrow \infty} \sum_{i=1}^n \frac{\pi}{3n} \sin\left(\frac{i\pi}{3n}\right)$  is equal to:

- (a)  $\int_0^{\frac{\pi}{3}} \cos x dx$       (b)  $\int_0^{\frac{1}{3}} \cos x dx$       (c)  $\int_0^{\frac{\pi}{3}} \sin x dx$   
(d)  $\int_0^{\frac{1}{3}} \sin x dx$       (e)  $\int_0^{\frac{\pi}{3n}} \sin x dx$

7. (5 pts.) Compute the indefinite integral  $\int \frac{1+u}{\sqrt{u}} du$ .

(a)  $\frac{1}{2}u^{\frac{1}{2}} + \frac{3}{2}u^{\frac{3}{2}} + C$

(b)  $-\frac{1}{2}u^{-\frac{3}{2}} + \frac{1}{2}u^{-\frac{1}{2}} + C$

(c)  $(1+u)^{\frac{1}{2}}2u + C$

(d)  $(1+u)^2u^{\frac{1}{2}} + C$

(e)  $2u^{\frac{1}{2}} + \frac{2}{3}u^{\frac{3}{2}} + C$ .

8. (5 pts.) Compute the definite integral  $\int_0^3 (6 + 6x - x^2) dx$ .

a) 54      b) -12      c) 36      d) -18      e) 45

9. (5 pts.) Use differentials to approximate  $\tan(0.1)$  recognizing that  $\tan(0) = 0$ .

a) 0.3      b) 0.1      c) 0      d) -0.1      e) 0.2

10. (5 pts.) Compute  $\frac{d}{dx} \left( \int_0^{x^2} \sin^2 t dt \right)$ .

a)  $2x \cos(x^2)$

b)  $2x \cos x \sin(x^2)$

c)  $2x \cos(x^2) \sin(x^2)$

d)  $2x \sin^2(x^2)$

e)  $\sin^2(x^2)$

11. (5 pts.) Compute  $\int_{-1}^1 |x| dx$ .

a) 2

b) -2

c) 1

d) 0

e)  $\frac{1}{2}$

12. (5 pts.) Compute the area bounded by the graph of  $y = x^2 - 1$ , the  $x$ -axis, and the vertical lines  $x = -1$ ,  $x = 1$ .

a)  $\frac{4}{3}$

b)  $-\frac{4}{3}$

c)  $\frac{8}{3}$

d)  $-\frac{8}{3}$

e) 0

**Part B: Partial Credit Problems**

Remember to show all your work.

- 13.** (10 pts.) Compute the integral  $\int_0^1 x^2 dx$  using the limit definition. You may use the formula  $\sum_{i=1}^n i^2 = \frac{n(n+1)(2n+1)}{6}$ .

**Answer:**

14. (10 pts.) Sketch the graph of the function  $y = x^3 - 3x$ .



15. (10 pts.) Find the point on the line  $y = 4x + 8$  closest to the origin.

**Answer:**

**16.** (10 pts.) The acceleration function of a particle moving along a line is given by

$$a(t) = t + 4 \text{ ft/sec}^2.$$

Find the position function  $s(t)$  if the initial velocity is  $v(0) = 2 \text{ ft/sec}$  and the initial position is  $s(0) = 0 \text{ ft}$ .

**Answer:**