

Worksheet 4

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September 14, 2009

I. Evaluate the following integrals

1. $\int \frac{x^5 + 1}{x^3 - 3x^2 - 10x} dx.$

2. $\int e^{\sqrt{3x+2}} dx.$

3. $\int \frac{x}{\sqrt{3-x^4}} dx.$

4. $\int \frac{1}{x + \sqrt[3]{x}} dx.$

5. $\int x \sin(x)^2 \cos(x) dx.$

6. $\int \frac{x \ln(x)}{\sqrt{x^2 - 1}} dx.$

II. Use your favorite approximation method to approximate $\int_0^4 x^3 dx$ (use $n = 4$ intervals). Evaluate the errors and compare them to the theoretical error bounds.

III. Determine whether each integral is convergent or divergent. Evaluate those that are convergent.

1. $\int_1^{\infty} \frac{e^{-\sqrt{x}}}{\sqrt{x}} dx.$

2. $\int_{-\infty}^{\infty} \cos(\pi t) dt.$

3. $\int_0^{\infty} \frac{dz}{z^2 + 3z + 2}.$