

# Tutorial: State-of-the-Art Flow Field Analysis and Visualization

## Texture-Based Flow Visualization

Daniel Weiskopf

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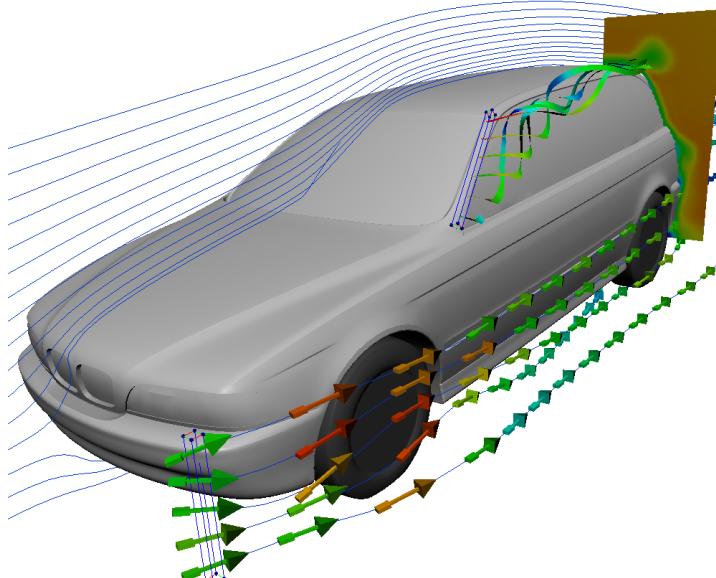
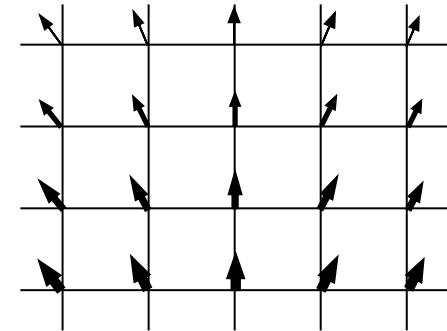
IEEE VIS 2013 | Atlanta | 2013-10-13

# Overview

- Background
- Line integral convolution and texture advection
- Hierarchical line integration
- Effective rendering and feature extraction
- Outlook and conclusion

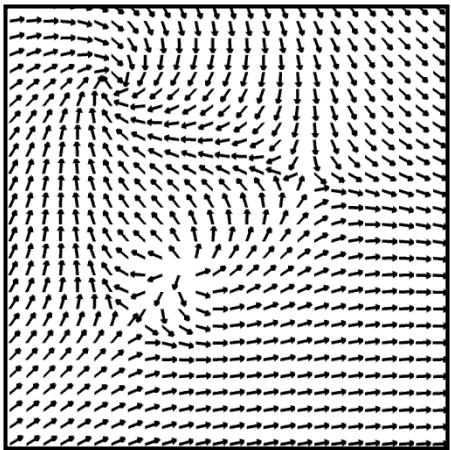
# Flow Visualization Approaches

- Direct approaches
  - Glyphs, arrows
  - Color coding
- Sparse, line-like representations
- Dense, line-like representations
- Characteristic lines
  - Streamlines
  - Pathlines
  - Streaklines

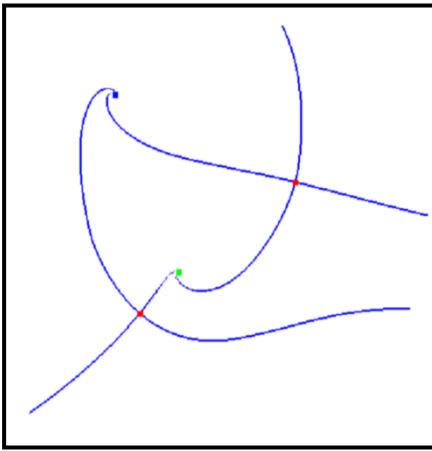


[courtesy of BMW Group and Martin Schulz]

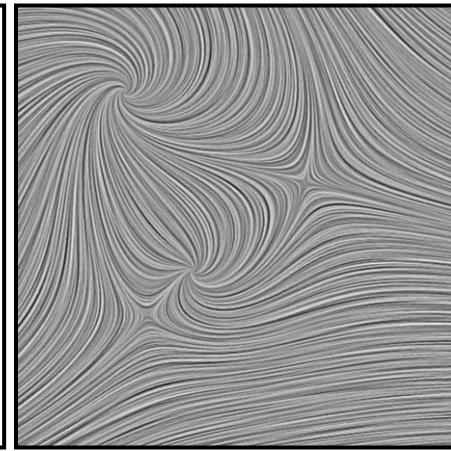
# Visualization Approaches



Arrows

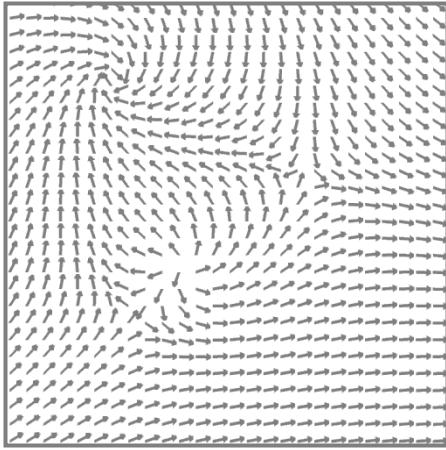


Sparse (topology)  
[Source: G. Scheuermann]

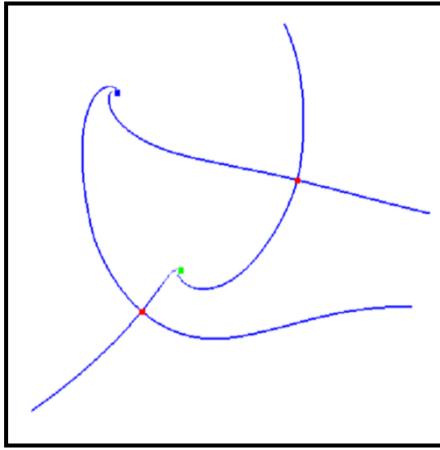


Dense (texture-based)

# Visualization Approaches

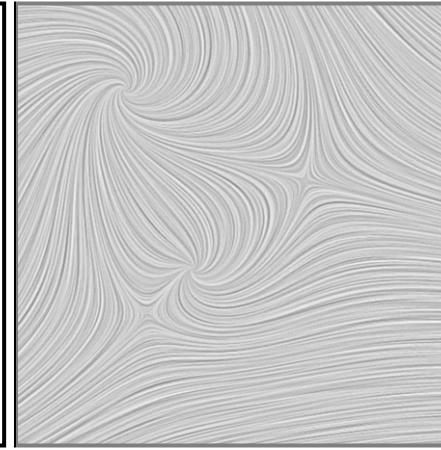


Arrows



**Sparse (topology)**

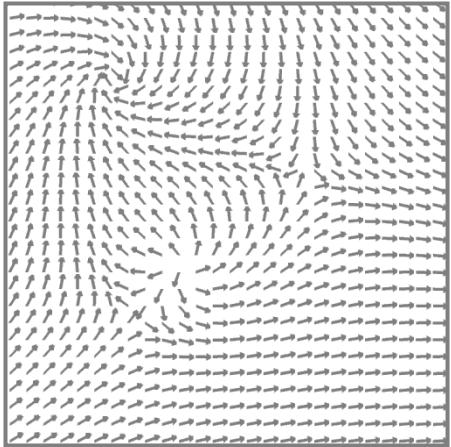
[Source: G. Scheuermann]



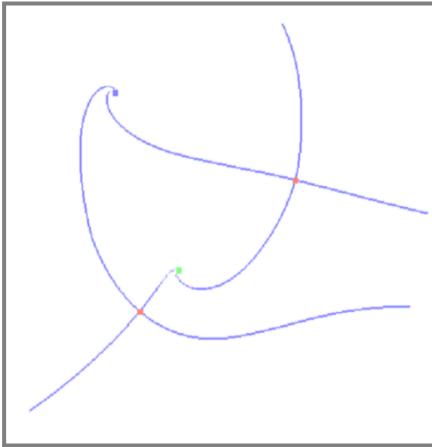
Dense (texture-based)

see later: Vector Field Topology in Flow Analysis and Visualization

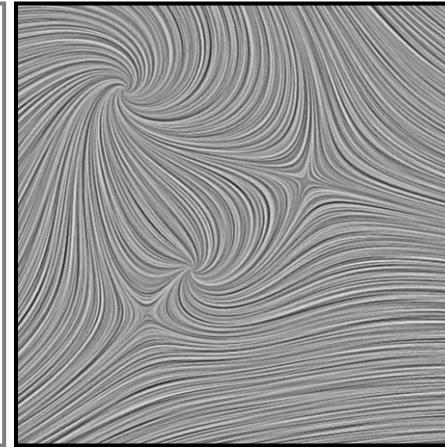
# Visualization Approaches



Arrows



Sparse (topology)  
[Source: G. Scheuermann]



**Dense (texture-based)**

# Why Texture-Based Flow Visualization?

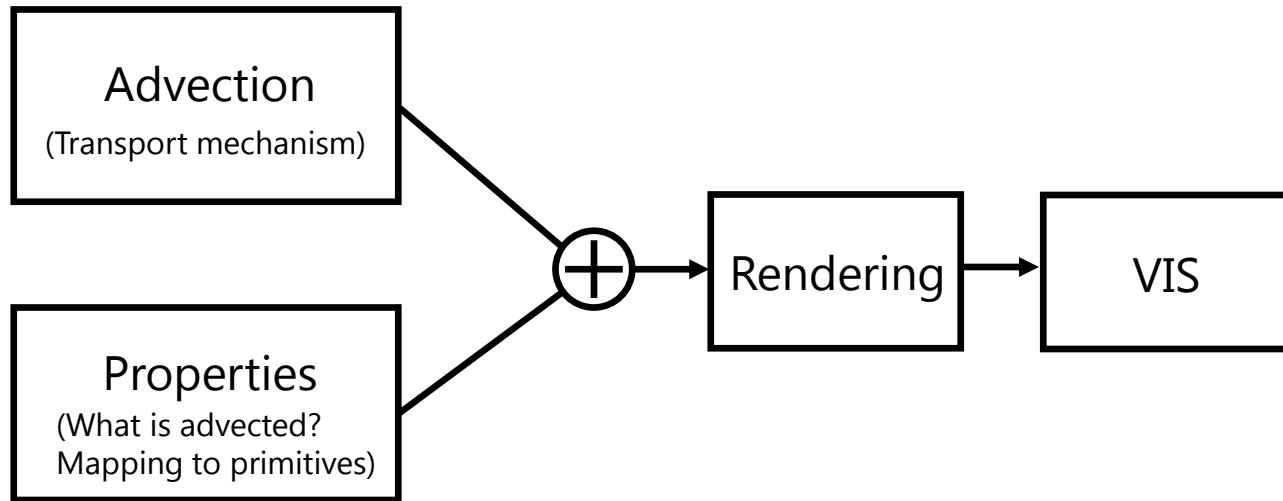
- Dense sampling
  - Better coverage of information
  - (Partially) solved problem of seeding
- Flexibility in visual representation
  - Good controllability of visual style
  - From line-like (crisp) all the way to fuzzy

# Dense Vector Field Visualization

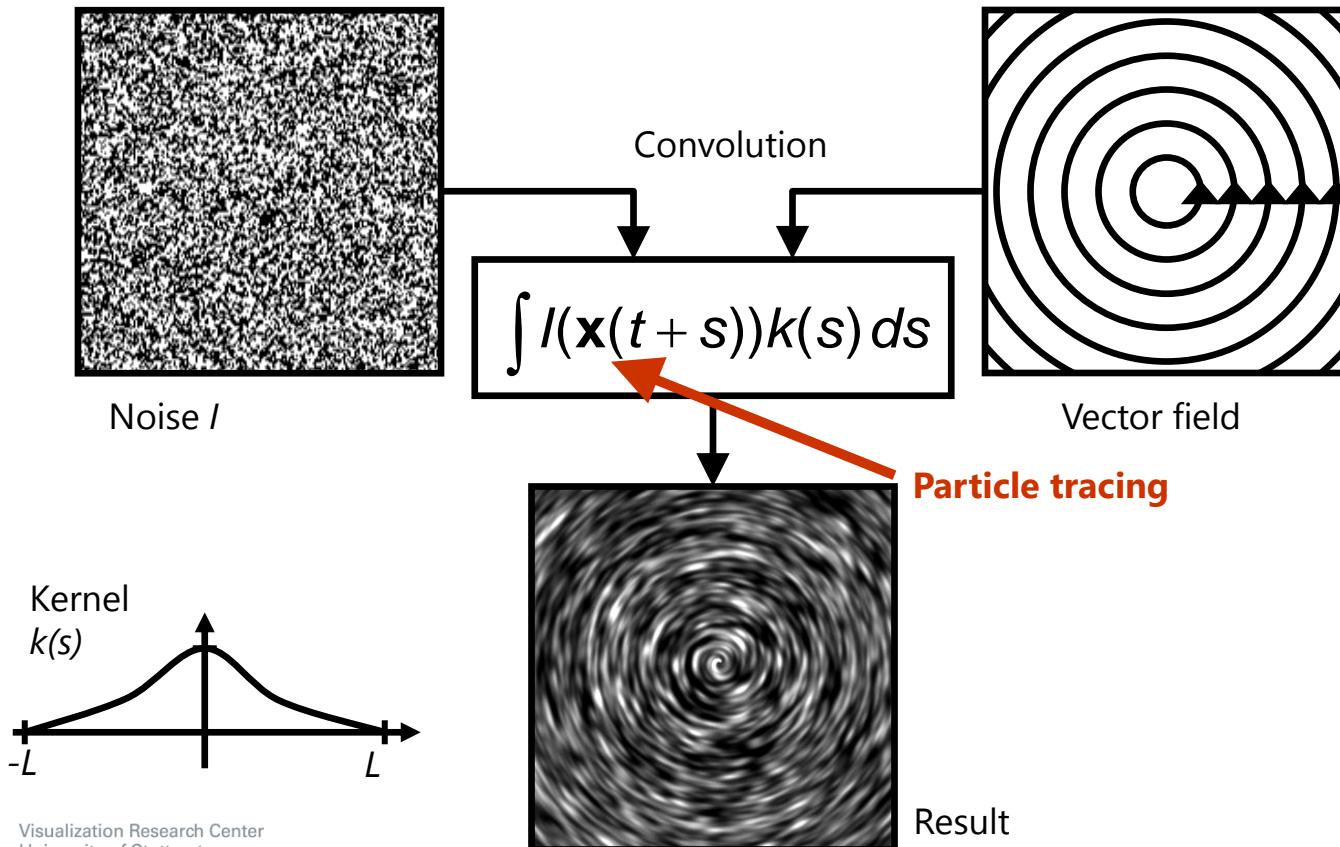
- Characteristic lines
- Challenges
  - Visualization speed
  - Quality
  - Effectiveness
- Interactive GPU methods
- Hierarchical computation
- Facilitate good visual perception
- Combine with feature extraction



# Ingredients of Vector Field Visualization



# Line Integral Convolution (LIC)



# Lagrangian Particle Tracing

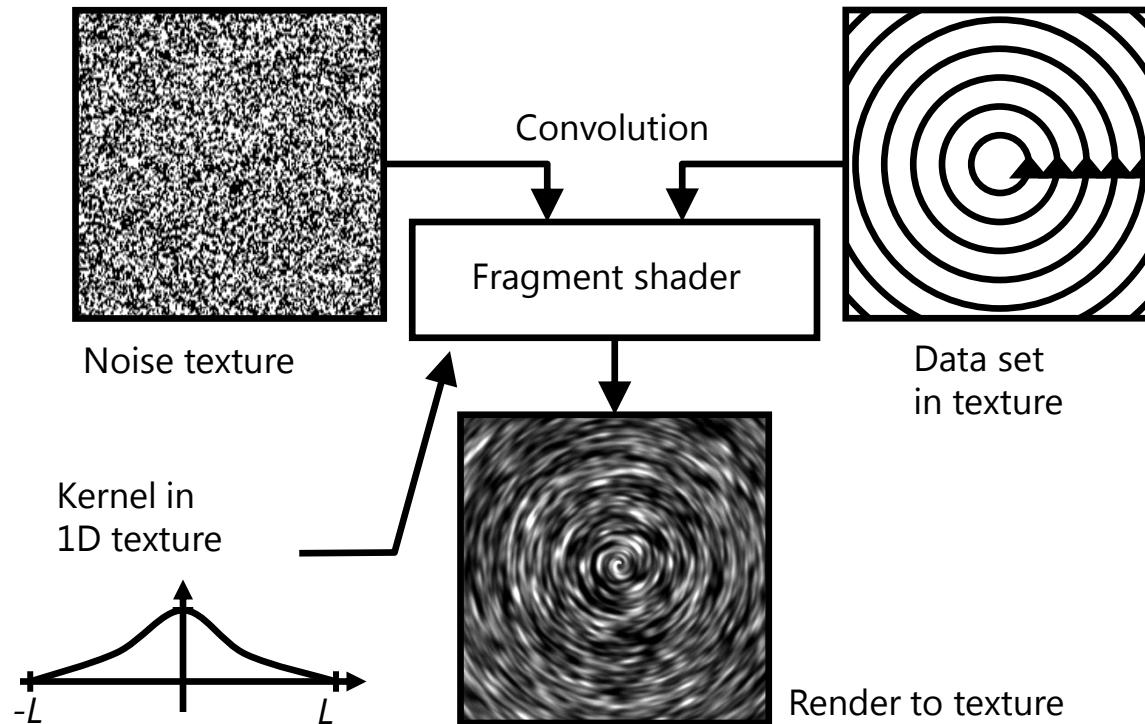
- Velocity vector  $\mathbf{v}$
- Trace massless particles
- Equation of motion:
- Explicit integration
  - Step-by-step
  - Possible in GPU fragment shaders

$$\frac{d\mathbf{r}}{dt} = \mathbf{v}(\mathbf{r}, t)$$

# Convolution

- Discretization of the convolution integral
- Integration simultaneously with particle tracing
- Accumulate noise values

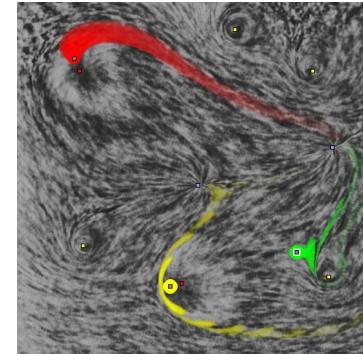
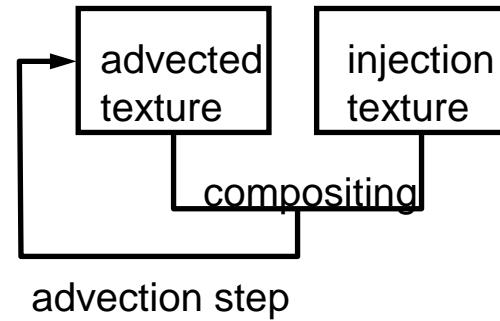
# Mapping to GPU: Parallel Computation



# Incremental LIC: Texture Advection

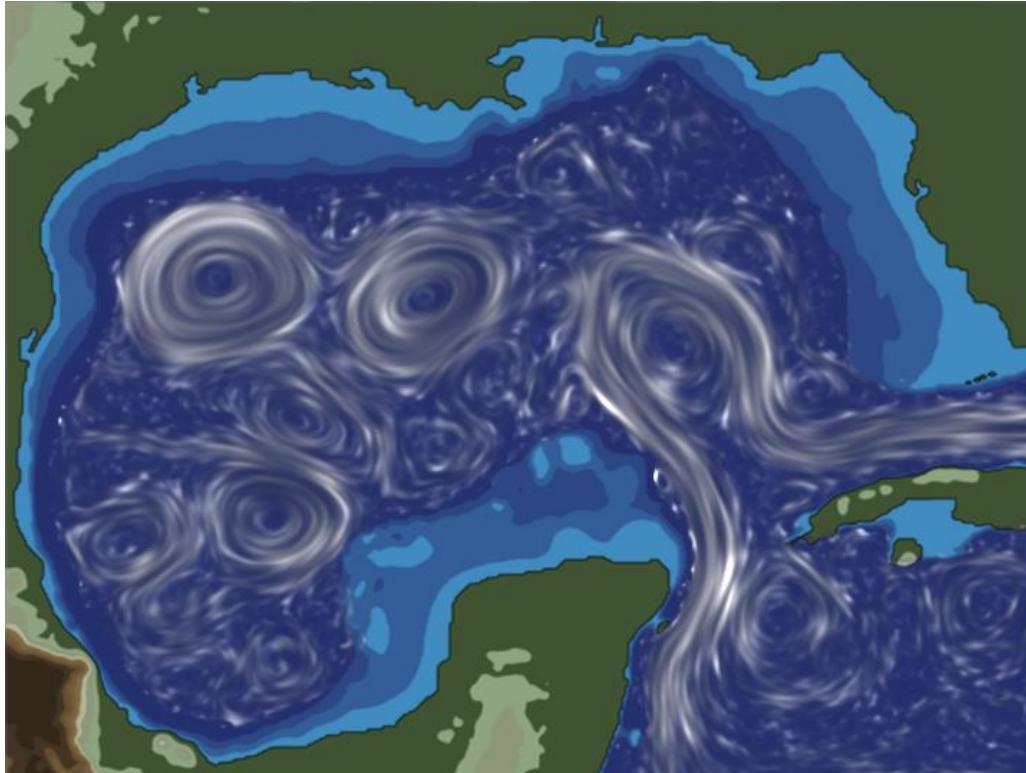
[Van Wijk 2002]

- Injection of new material
  - IBFV idea
  - Injection texture
- Alpha blending
  - Exponential filter kernel (steady case)
  - Streaklets (unsteady)



[generated by Van Wijk's demo program]

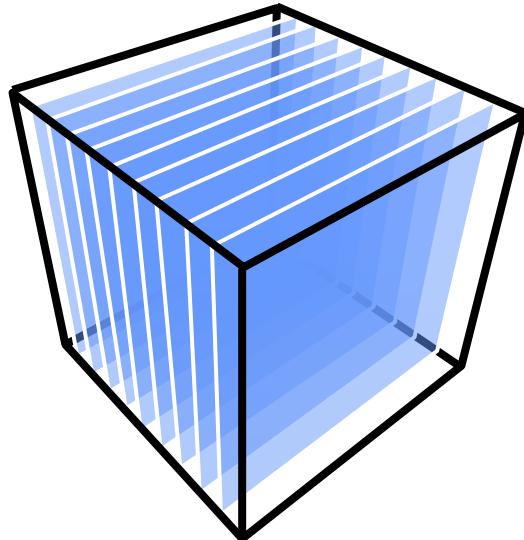
# Gulf of Mexico



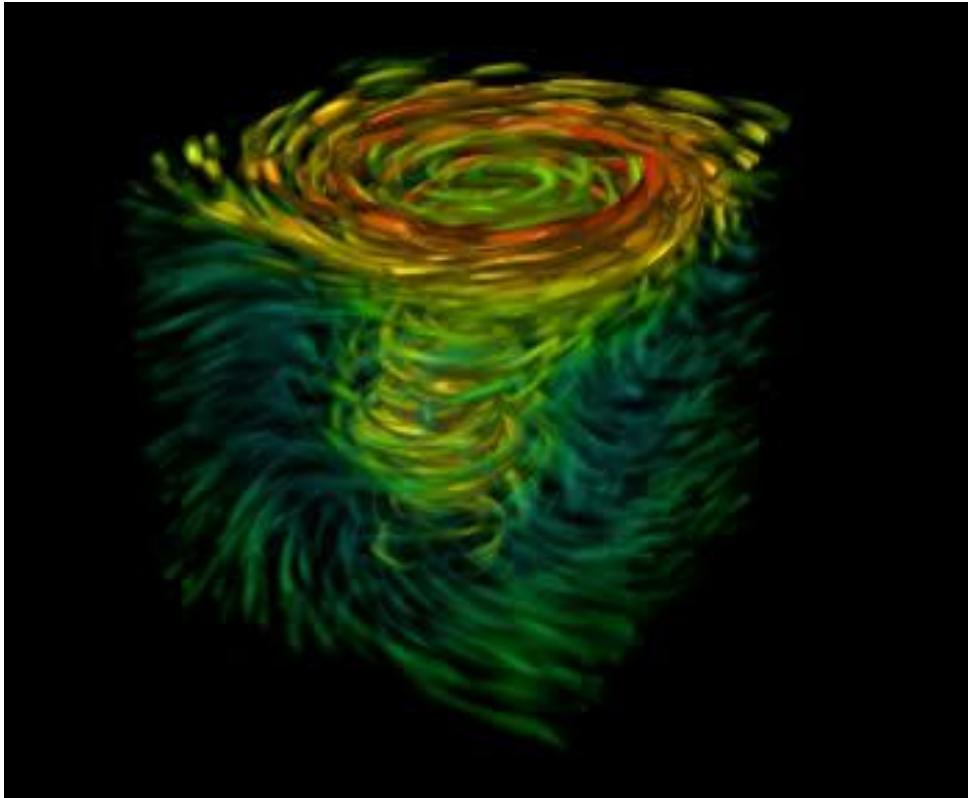
Data set: 352 x 320, 183 time steps [Data courtesy of O'Brien, FSU]

# 2D and 3D LIC

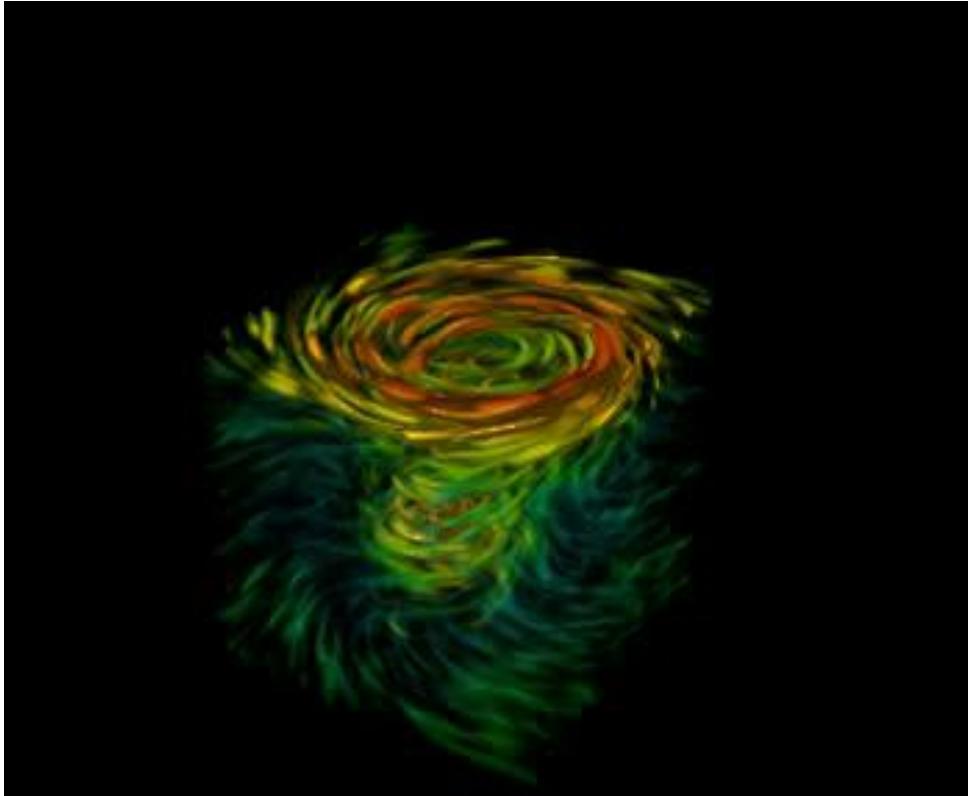
- 2D case:
  - Only 2D textures (vector field, noise, result)
  - Rendering is trivial: just 2D image
- 3D case:
  - 3D textures for vector field and noise
  - Slice-by-slice output
  - Volume rendering
- 3D alternative:
  - On-the-fly computation [Falk, Weiskopf 2008]
  - Integrated within GPU ray casting
  - Lazy evaluation: output sensitivity



# 3D LIC On-the-Fly



# 3D LIC On-the-Fly



# Hierarchical Line Integration

[Hlawatsch et al. 2011]

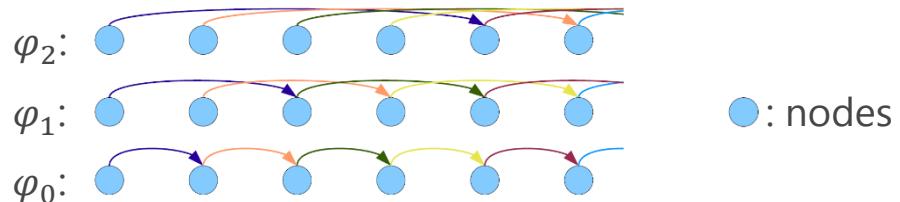
- Coordinate maps

$$\varphi_i : D \rightarrow D, D \subseteq \mathbb{R}^n$$

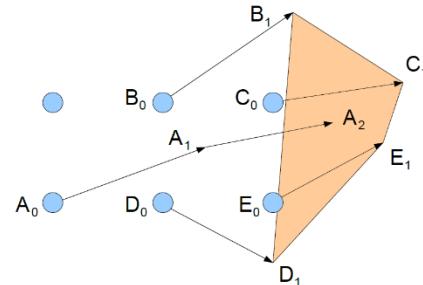
$x$  : start point of traj.

$\varphi_i(x)$  : end point of traj.

$i$  : hierarchy level



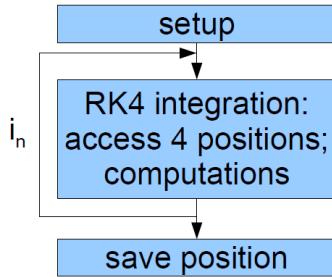
- $\varphi_0$  obtained, e.g., by integration
- $\varphi_{>0}$  constructed by “concatenation”
- All levels have same resolution (no pyramid)
- Overwrite (store only highest level)



- general case: end points not at nodes → interpolation

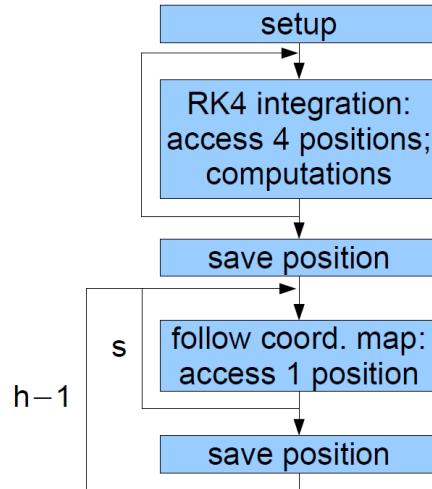
# Hierarchical Line Integration: Procedure

traditional approach  
( $n$  integration steps)



$O(n)$

hierarchical approach  
( $h$  levels)



$O(h) = O(\log n)$

integration of initial trajectories

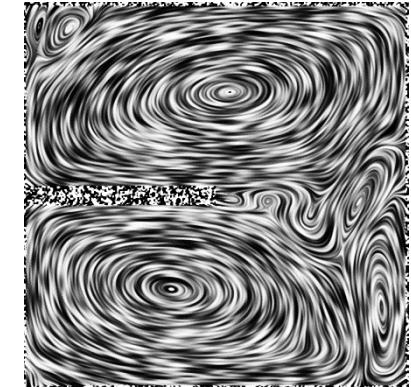
$\rightarrow \varphi_0$

one catenation ( $s = 2$ ) for next level

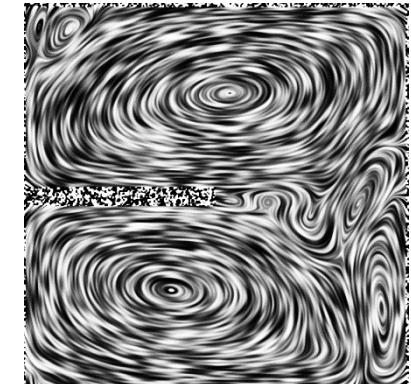
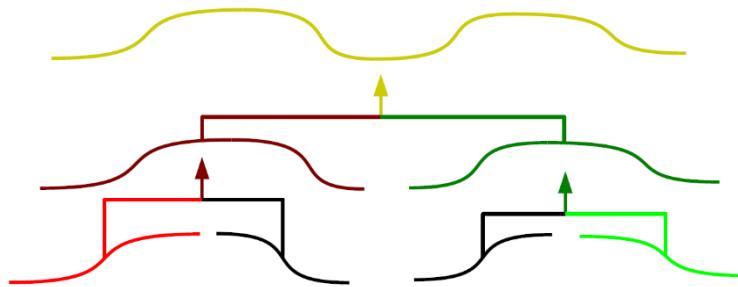
$\rightarrow \varphi_{+1}$

# Hierarchical Convolution

- Perform LIC operations inside hierarchical scheme
  - Combine intermediate quantities from integration
  - Convolution of Gaussian with Gaussian is Gaussian

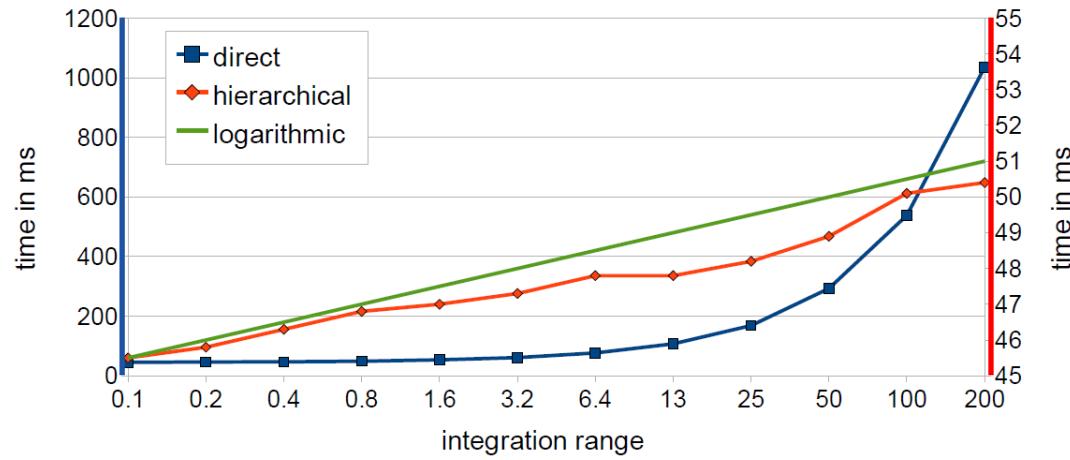


straightforward

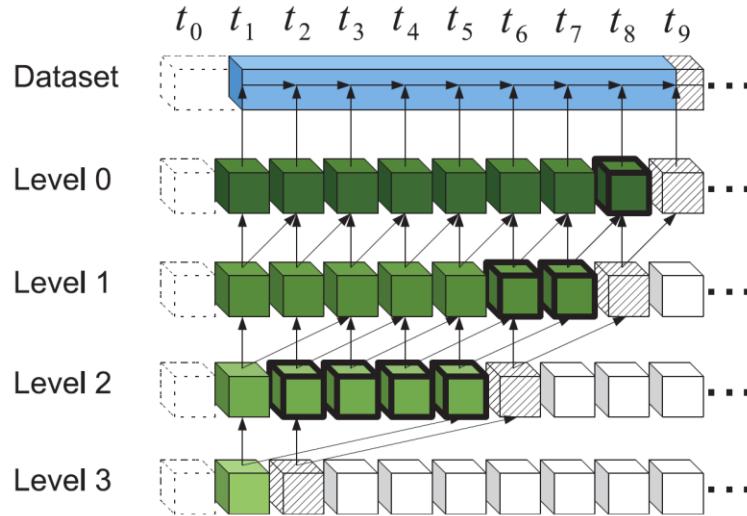


hierarchical

# Performance of Hierarchical Integration



# Time-Dependent Hierarchical Integration

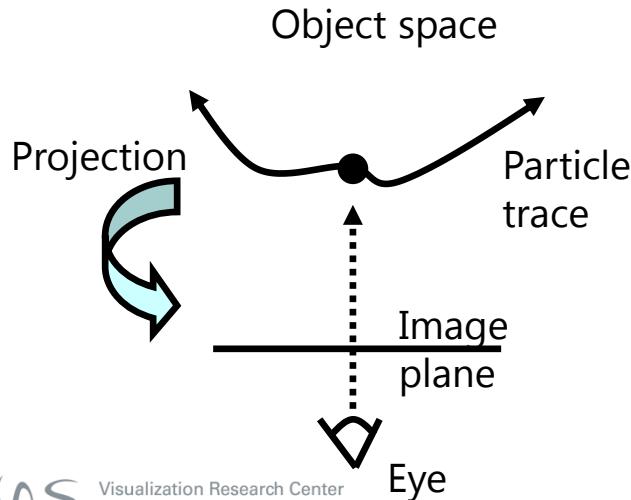


- level 0: from data set (by integration, blue)
- green: required for result at time  $t_1$  (at level 3)
- **bold outlines:** blocks kept in memory (overwrite)
- hatched: next time blocks
- integration range → number of blocks in memory
- scheme pays off for time series, i.e., dense trajectory seeding in time
- no temporal interpolation needed

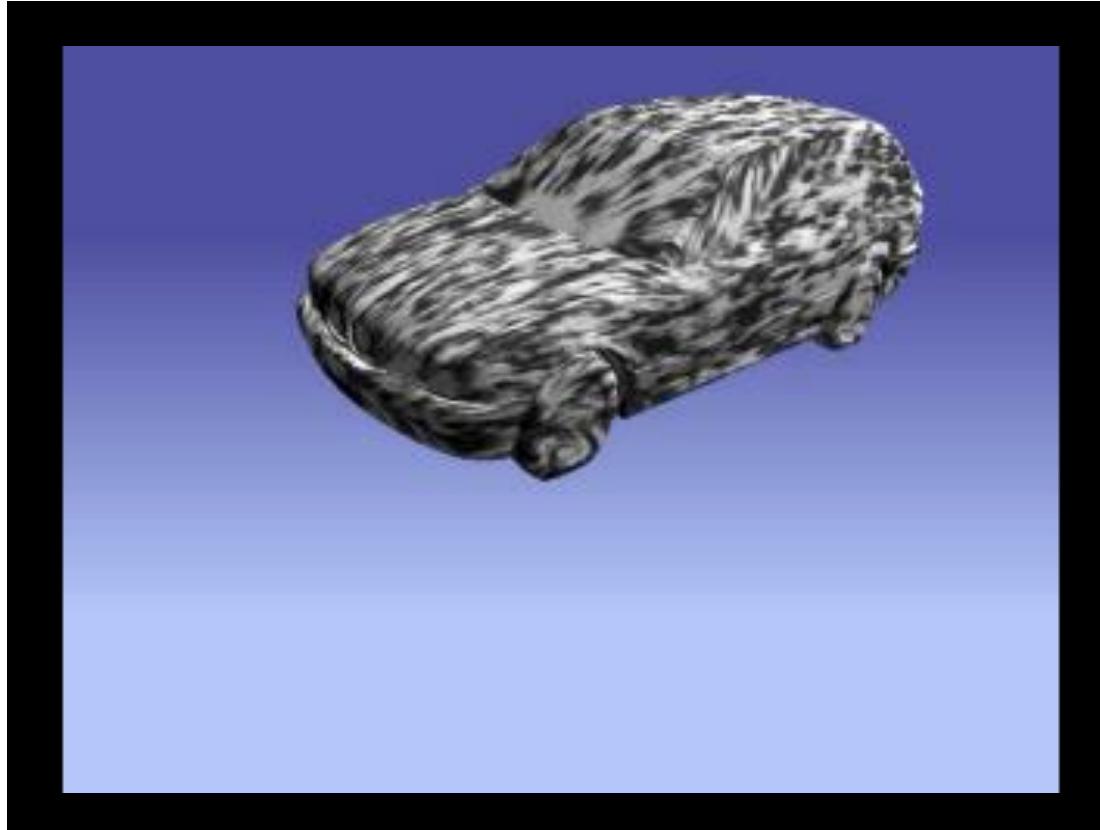
# 2.5D LIC

- Adapted to flow on boundaries
- Image-space methods

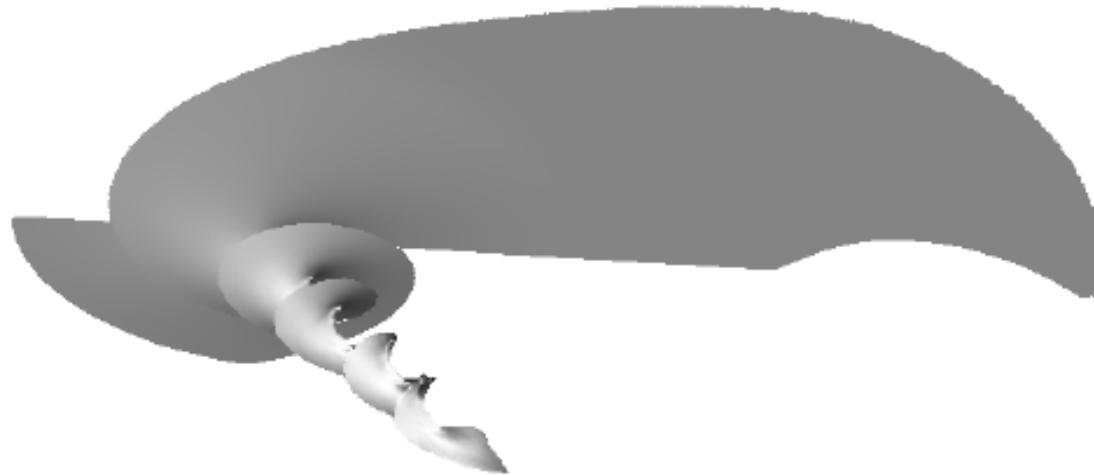
[Van Wijk 2003], [Laramee et al. 2003], [Weiskopf, Ertl 2004b]



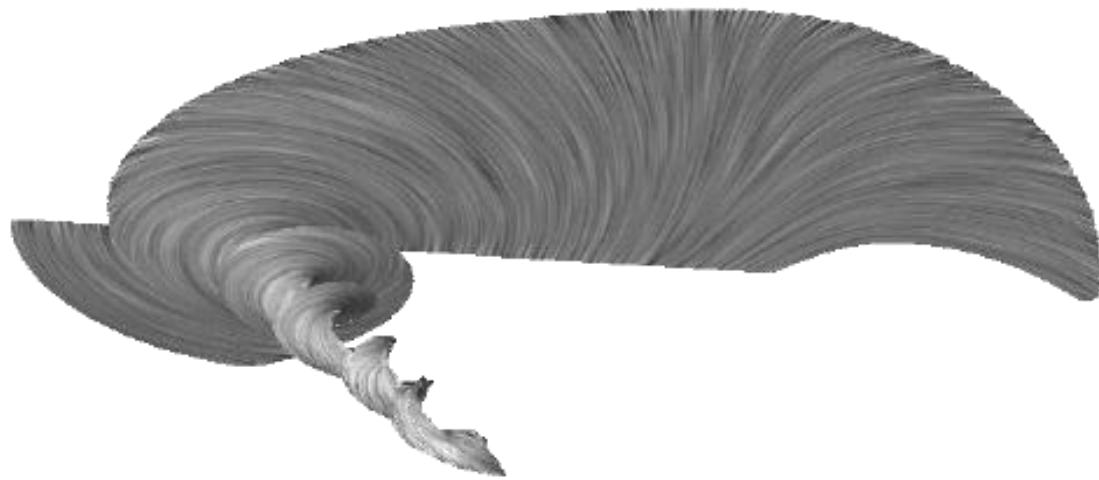
# 2.5D LIC



# On Pathsurfaces



# On Pathsurfaces

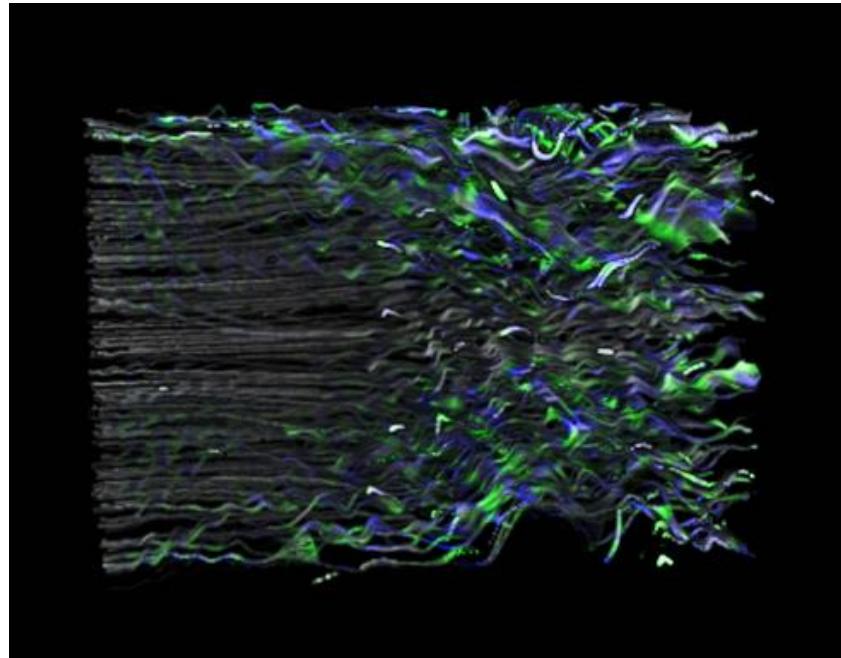


# Effective Visual Representation

- Perceptual issues for 3D LIC and texture advection
  - Spatial perception: Orientation, depth
  - Clutter
  - Occlusion

# Improved Rendering

- Improve spatial perception [Interrante, Grosch 1997]
  - Illumination
  - Halos
  - Depth cues
  - Line continuity



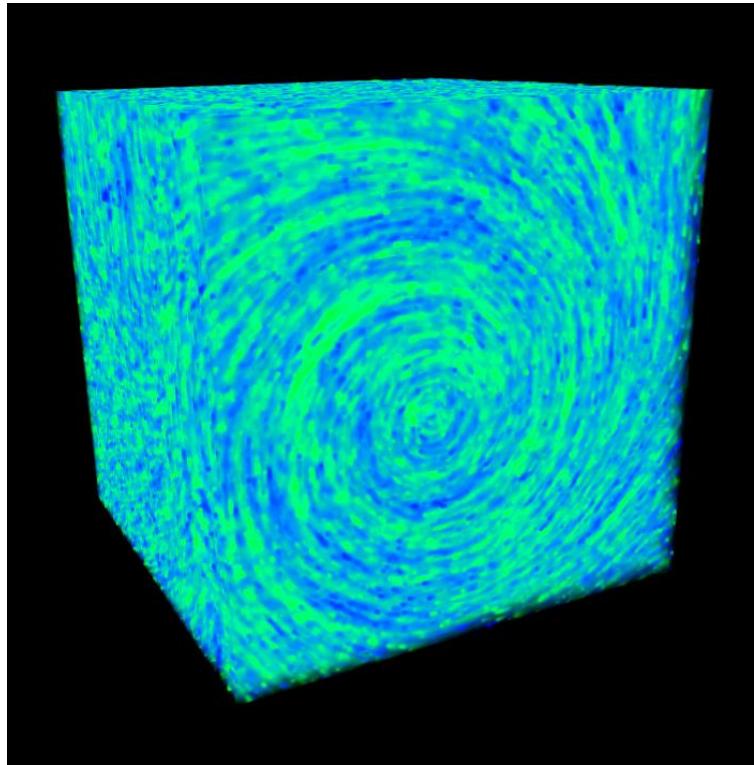
[Courtesy of Interrante, image reprinted from Weiskopf, Erlebacher 2005]

# Spatial Perception

- Technical solution:  
**Real-time volumetric illumination**  
[Weiskopf et al. 2007], [Falk, Weiskopf 2008]
  - On-the-fly computation of gradients
  - Various illumination models (Phong, cool/warm, halos)
  - Tangent-based illumination

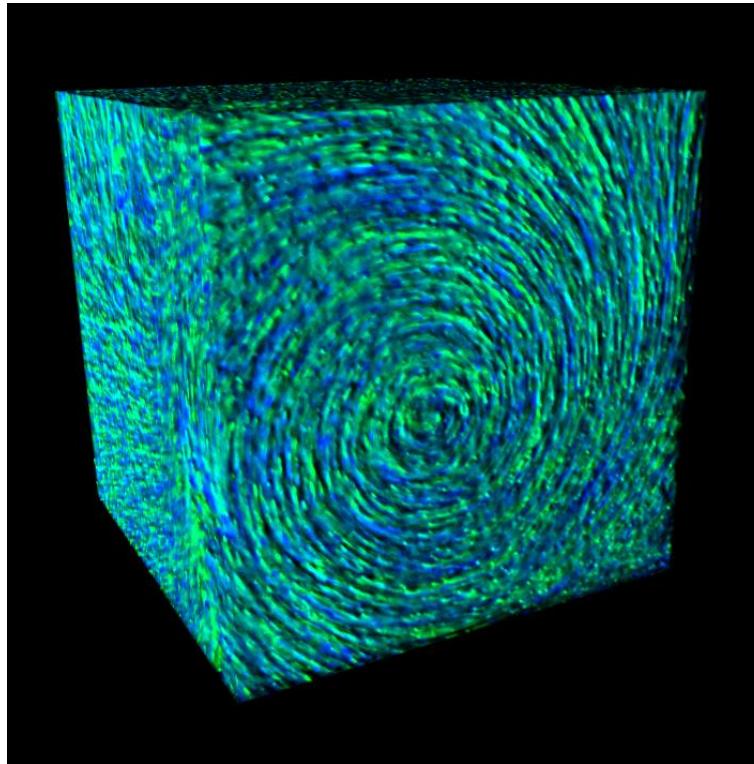
# Spatial Perception

- No illumination



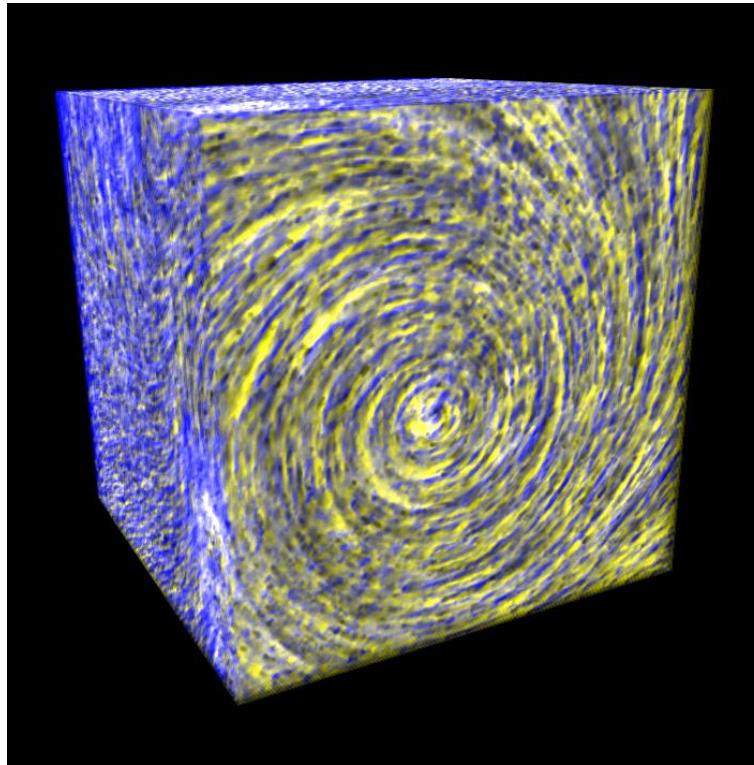
# Spatial Perception

- Phong  
illumination



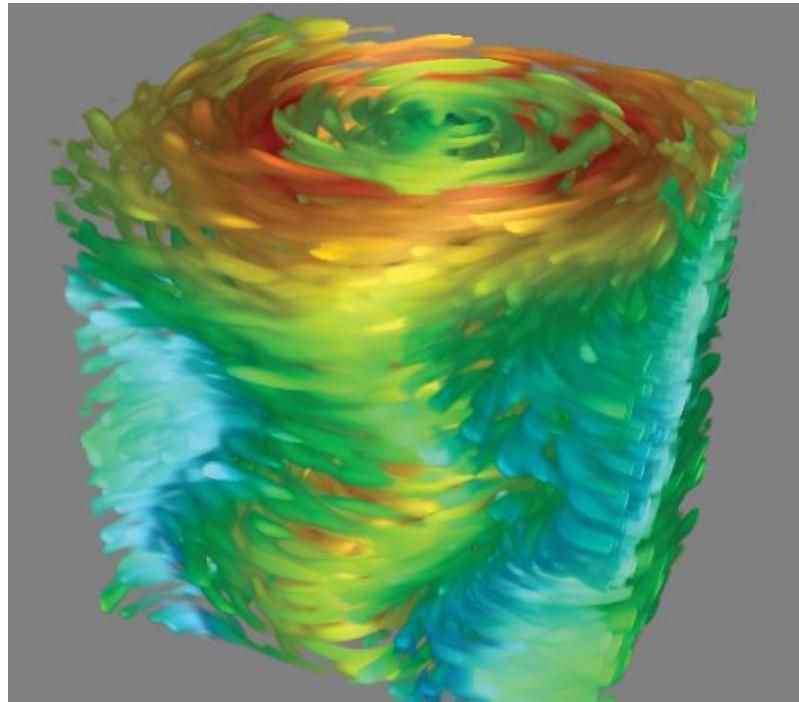
# Spatial Perception

- Cool/warm



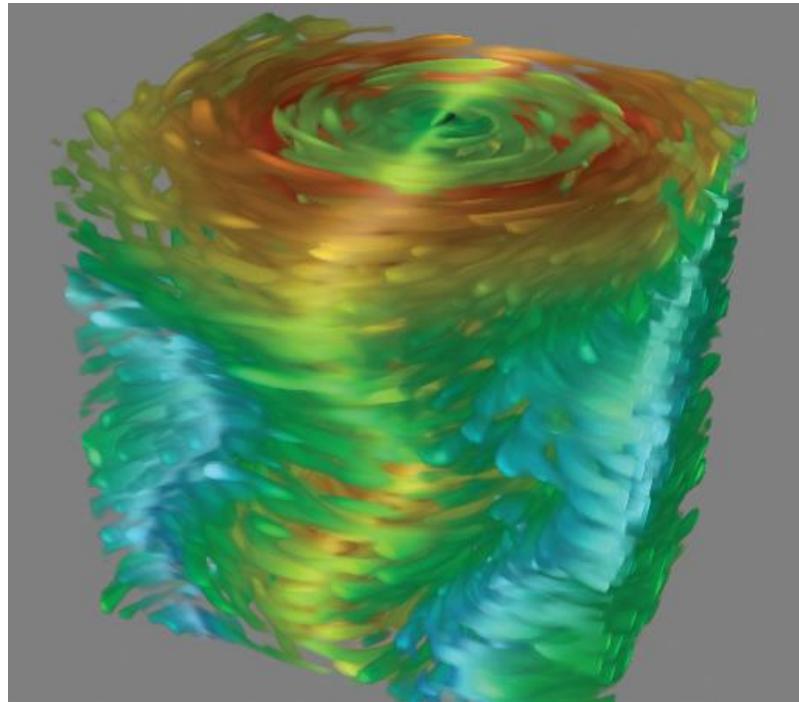
# Codimension-2 Illumination

- Illuminated streamlines:  
no gradients computed



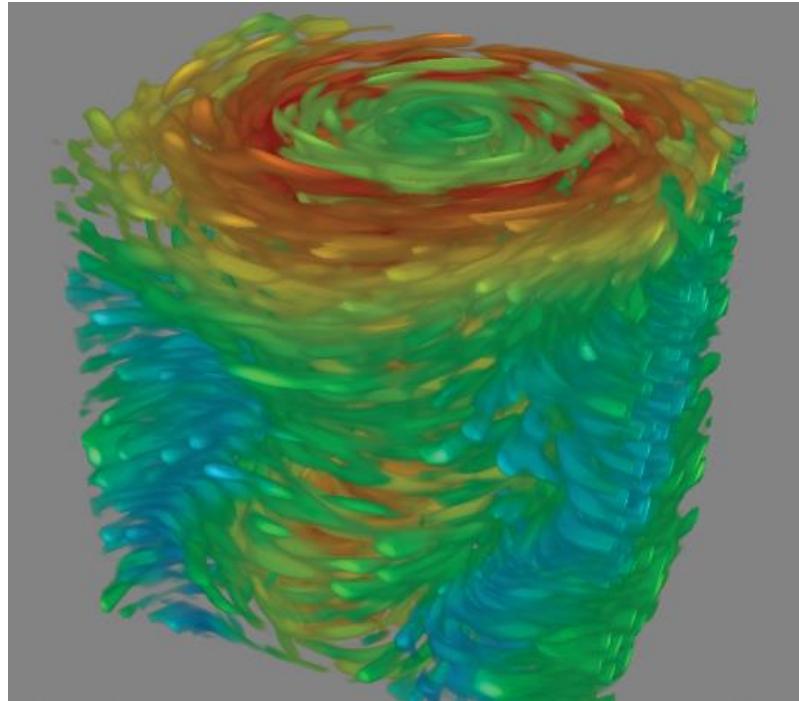
# Codimension-2 Illumination

- Alternative codimension-2 illumination model (Mallo)



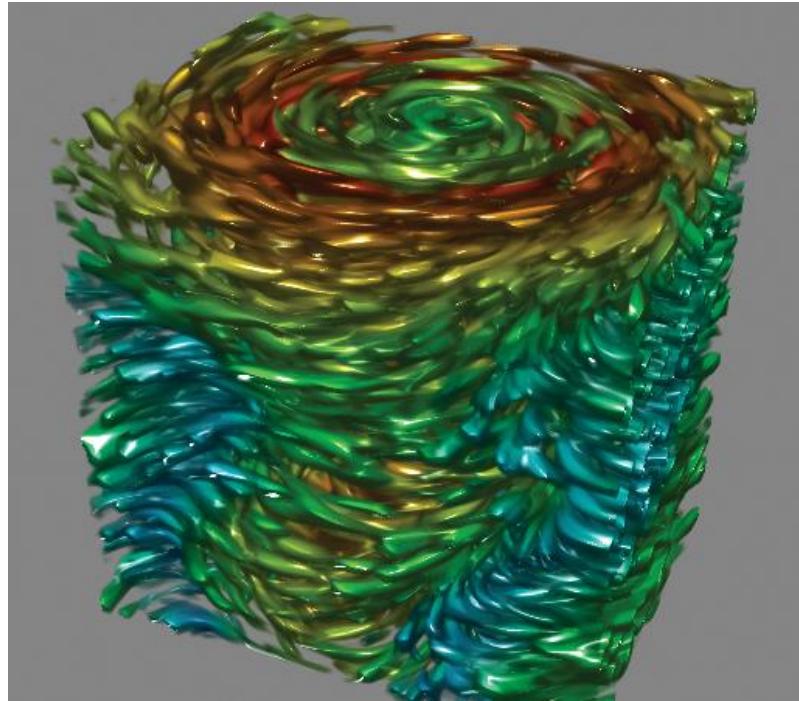
# Codimension-2 Illumination

- Comparison:  
without illumination

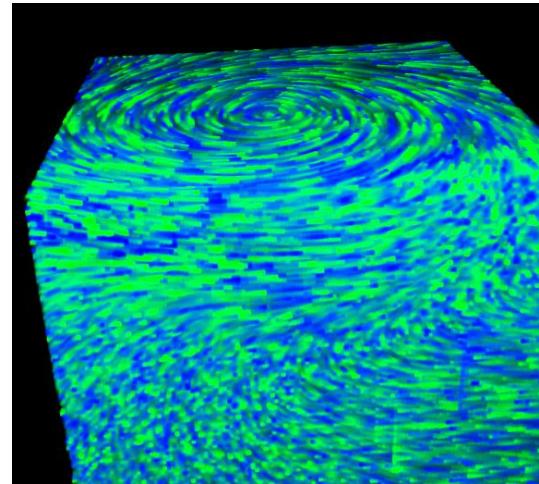


# Codimension-2 Illumination

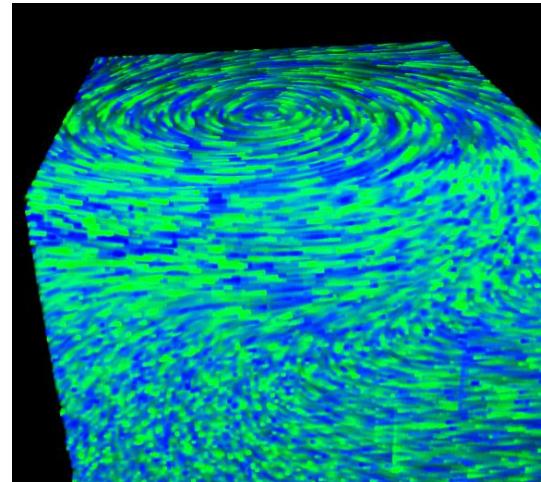
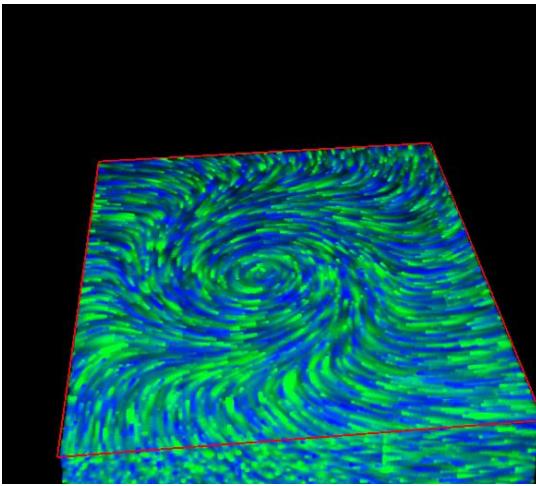
- Comparison:  
gradient-based illumination



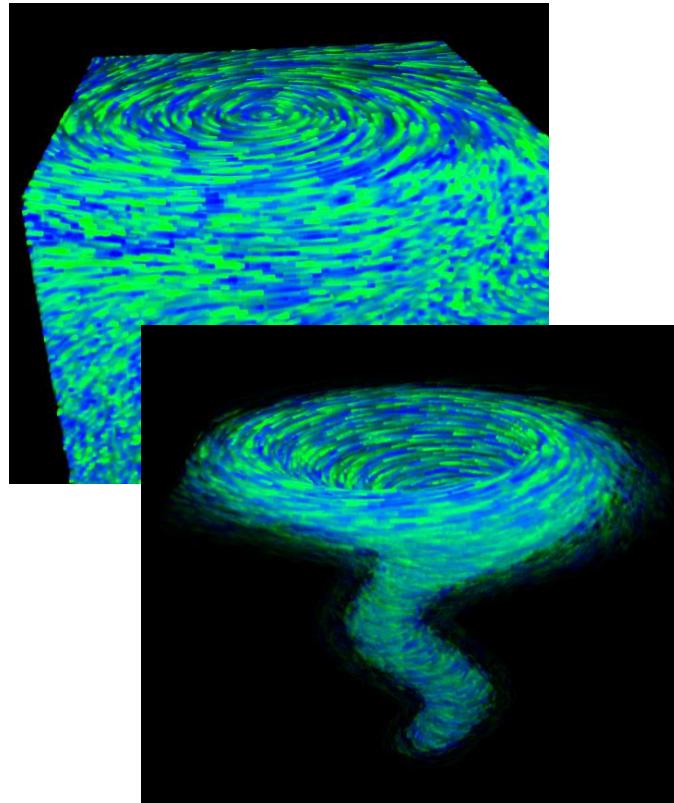
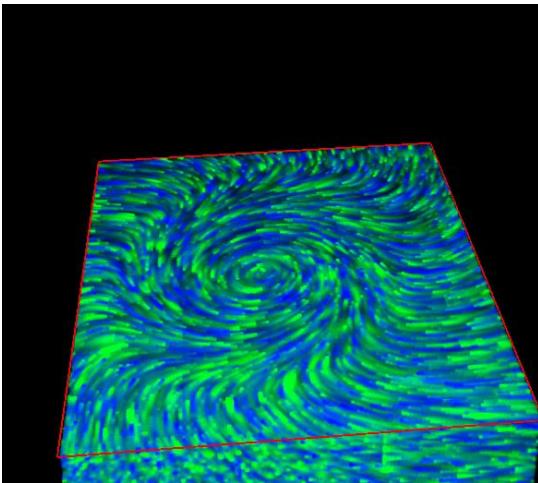
# Clutter and Occlusion



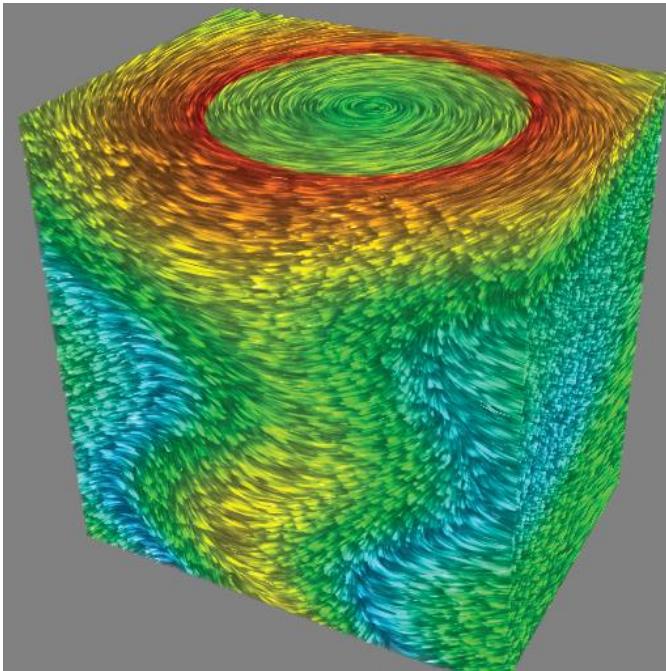
# Clutter and Occlusion



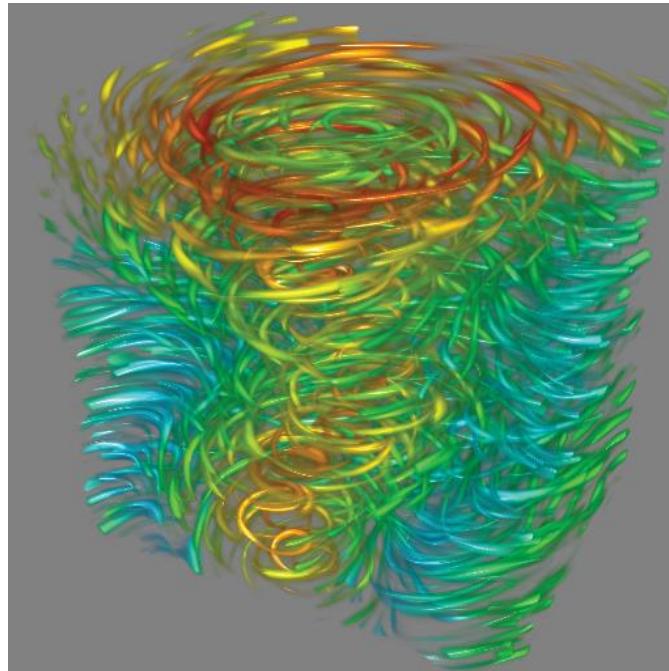
# Clutter and Occlusion



# Different Noise Models: “Seeding”

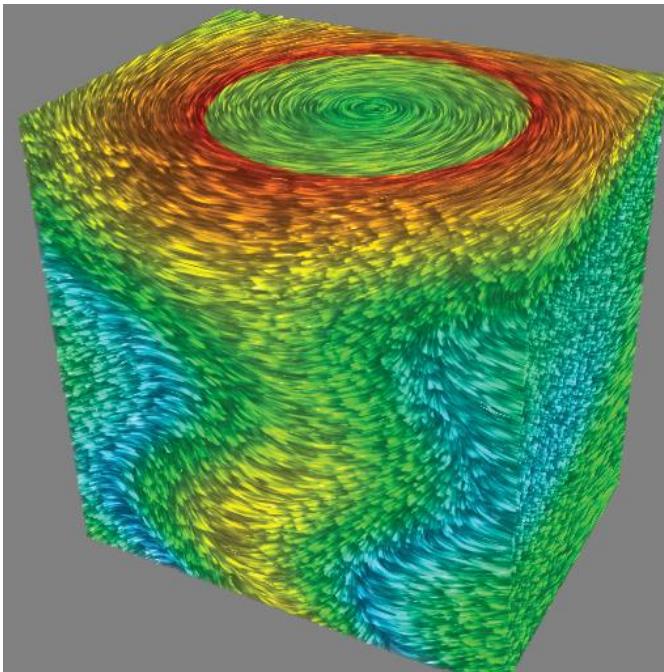


Dense (white noise)

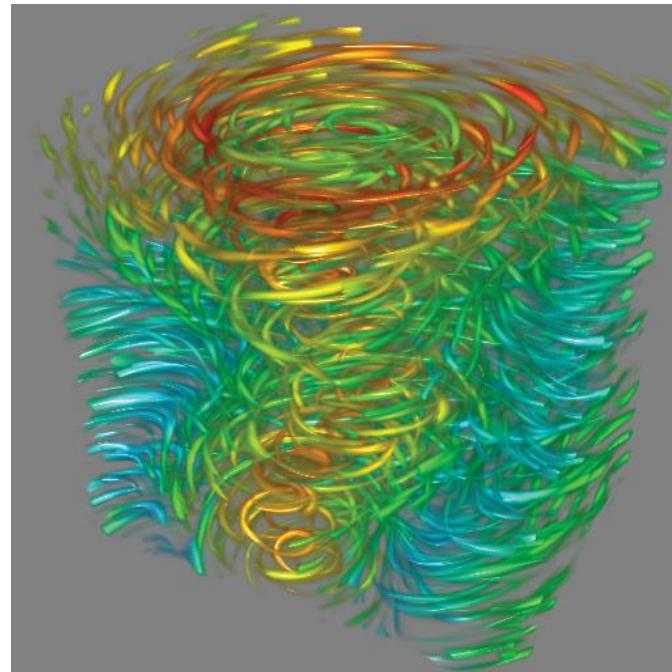


Sparse noise

# Different Noise Models: “Seeding”



Dense (white noise)

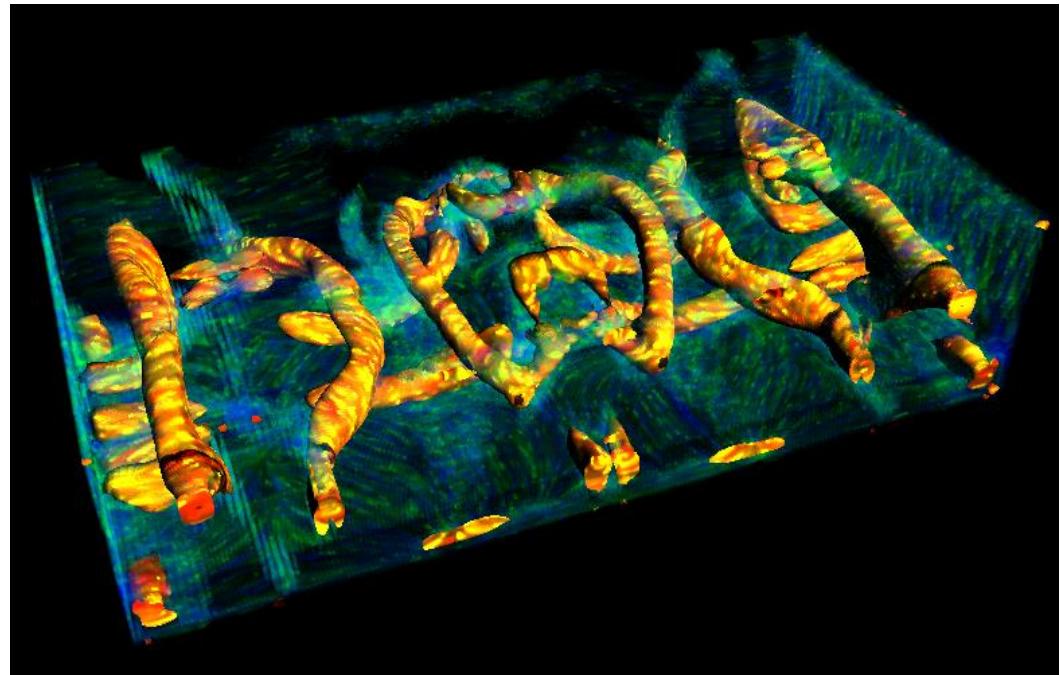


Sparse noise

see from before: Streamlines in 3D: Techniques beyond Seed Placement

# Flow Feature Extraction

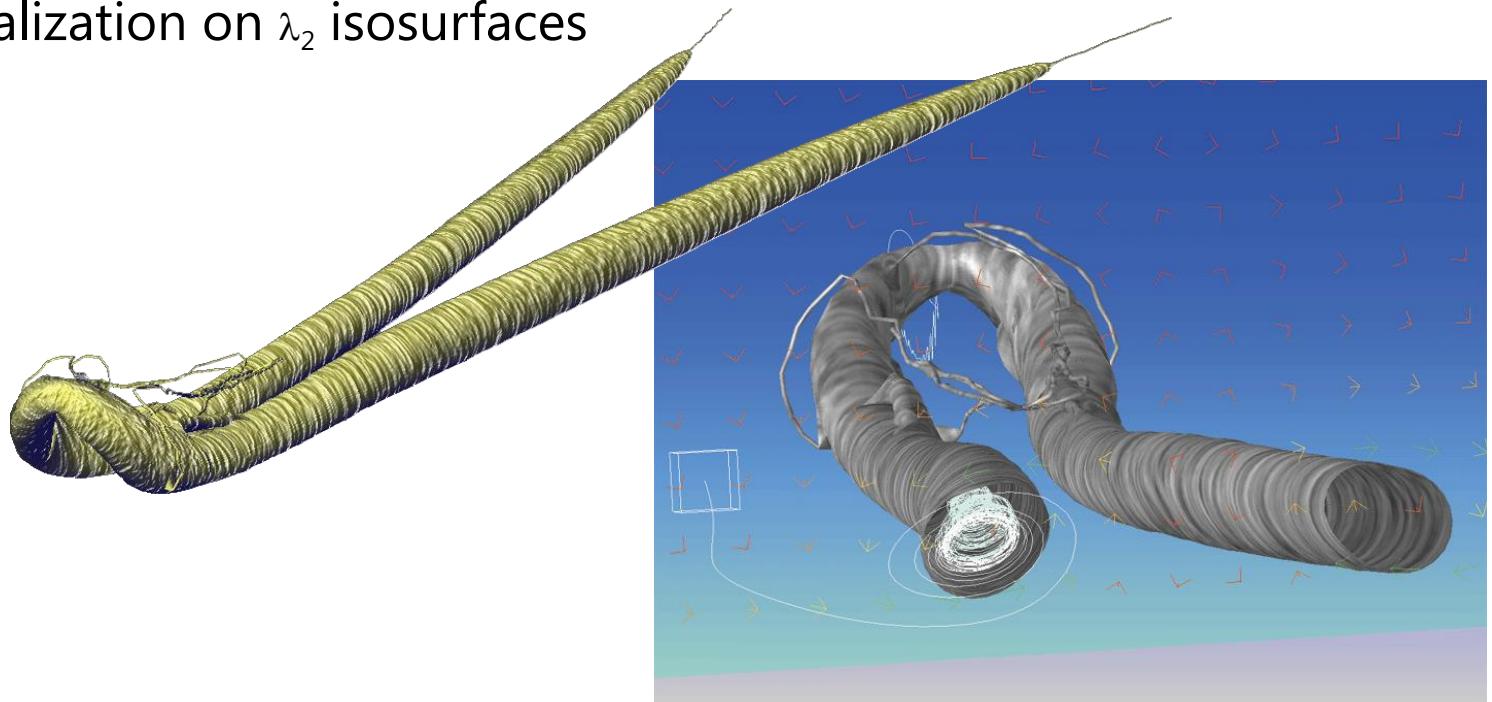
- 3D interest function
  - Domain knowledge
  - Interactive exploration



Vortex extraction  
with  $\lambda_2$

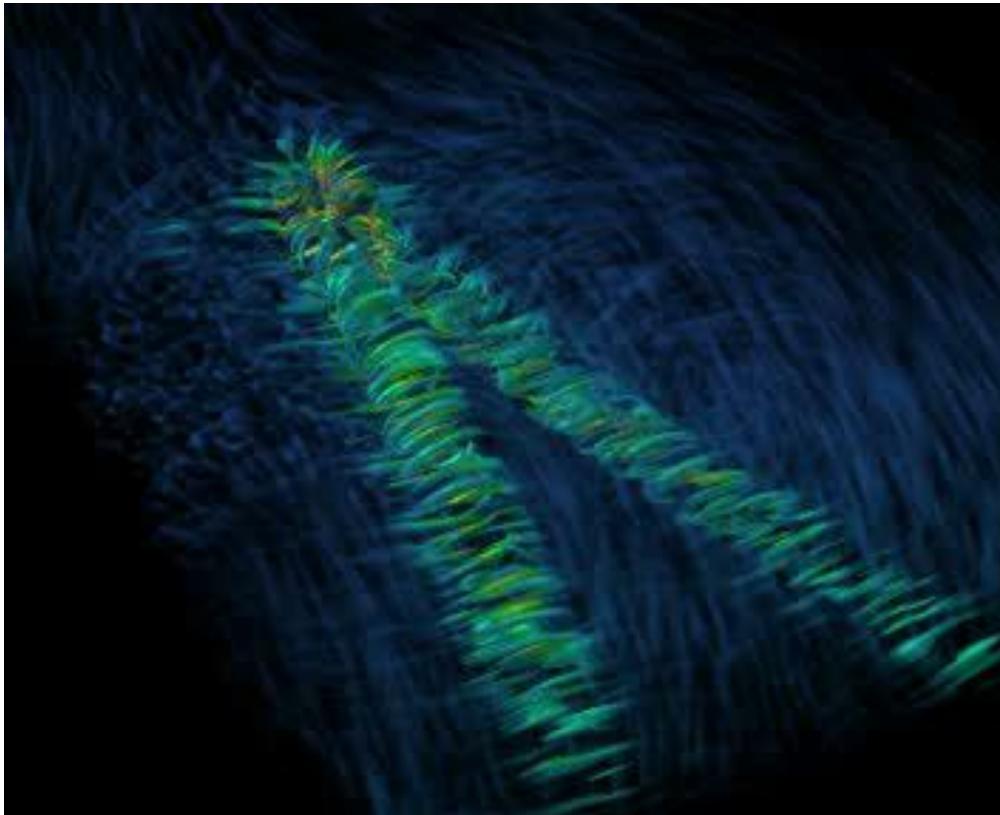
# Flow Feature Extraction

- 2.5D visualization on  $\lambda_2$  isosurfaces



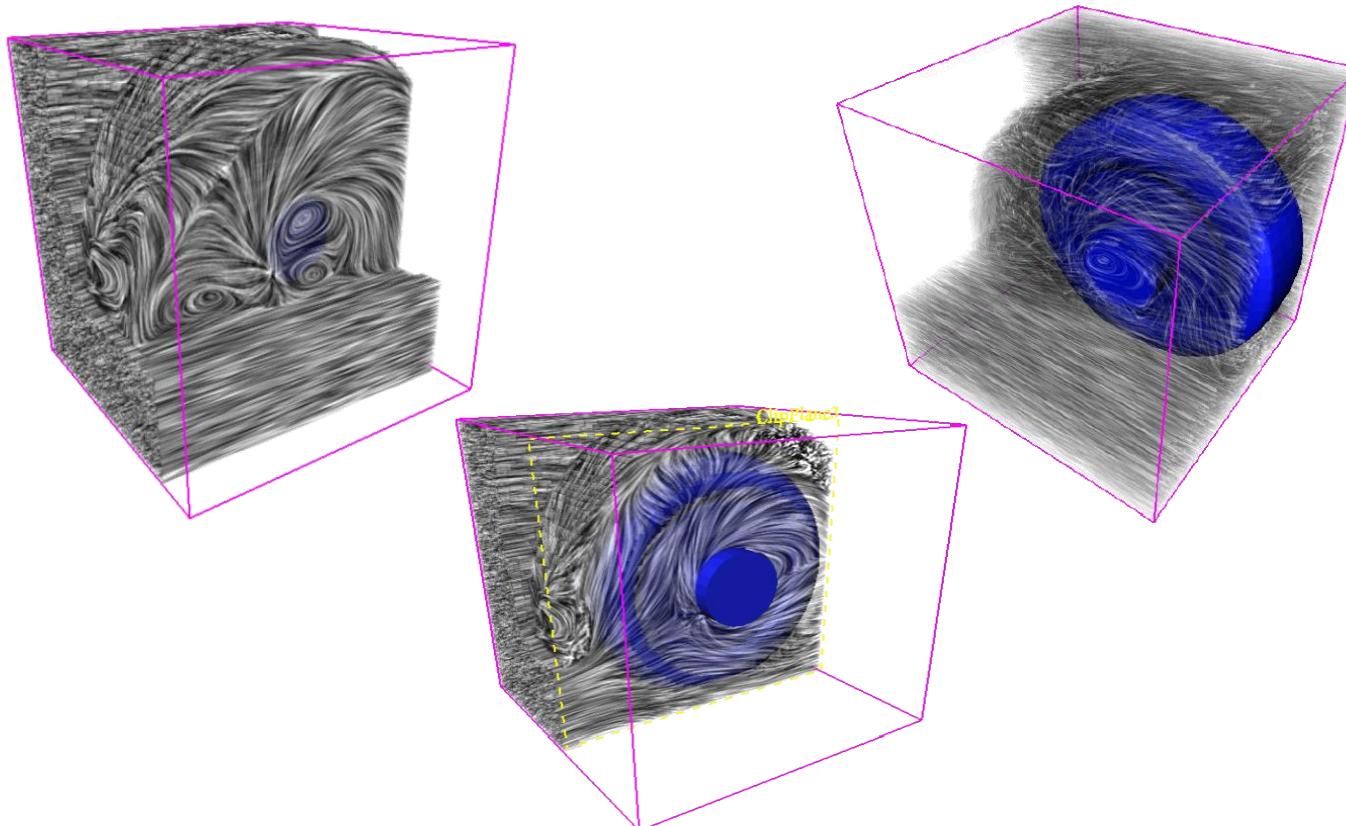
# Flow Feature Extraction

- 3D LIC with  $\lambda_2$  feature enhancement



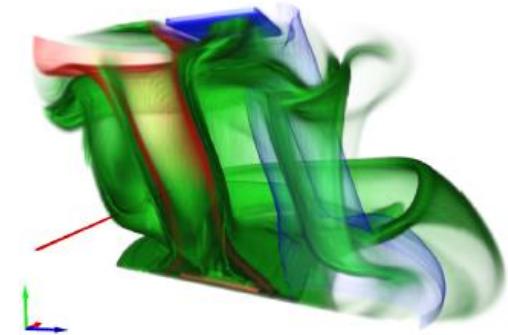
[Falk, Weiskopf 2008]

# Clipping and Semi-Transparency

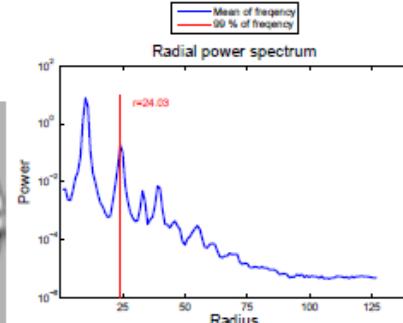
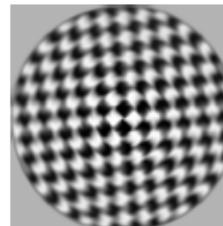


# Outlook: Topics Not Covered Here

- Physically oriented dye advection
  - Advection and diffusion [Karch et al. 2012]
- Numerical quality of dye and texture advection
  - Level-set and particle level-sets [Weiskopf 2004b], [Cuntz et al. 2008]
  - WENO schemes [Karch et al. 2012]
  - Higher-order and BFECC advection [Netzel et al. 2012]
- Quality of filtering
  - Frequency analysis: low-pass filter characteristics [Netzel et al. 2012] , [Weiskopf 2009]



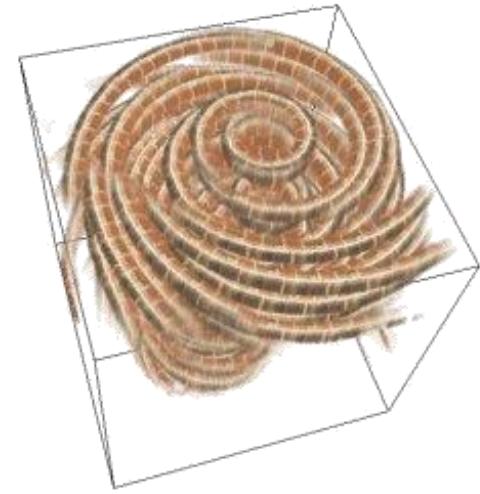
[Karch et al. 2012]



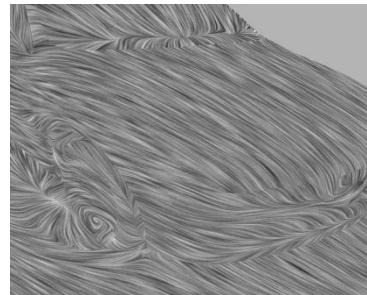
[Netzel et al. 2012]

# Outlook: Topics Not Covered Here

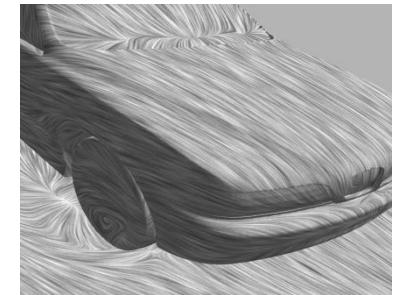
- Relationship to dense geometric curves and hybrid techniques [Verma et al. 1999], [Weiskopf et al. 2005]
- Control of rendering styles
  - Chameleon system [Li et al. 2003]
- Non-uniform grids and higher-order reconstruction
- Perceptual graphics
  - Texture, color, motion perception [Bachthaler, Weiskopf 2008], [Weiskopf 2004a]



[Li et al. 2003]



[Weiskopf 2004a]

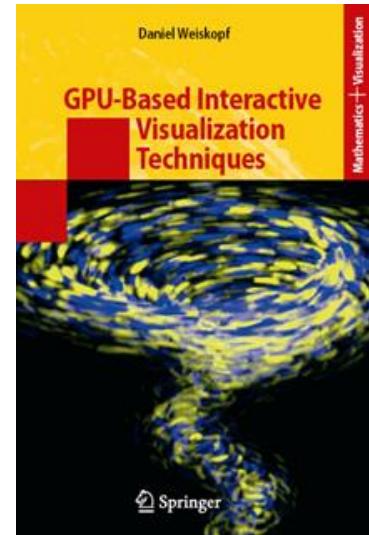


# Conclusion

- Texture-based vector field visualization
  - Flexible, widely applicable
  - Fast
- Components
  - Transport mechanism
  - Visual representation and rendering
  - Visualization quality

# Further Material

[www.vis.uni-stuttgart.de/texflowvis](http://www.vis.uni-stuttgart.de/texflowvis)



# References

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- [Karch et al. 2012] G. Karch, F. Sadlo, D. Weiskopf, C.-D. Munz, T. Ertl: Visualization of advection-diffusion in unsteady fluid flow. *Computer Graphics Forum* 3, 1105-1114, 2012.
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- [Netzel et al. 2012] R. Netzel, M. Ament, M. Burch, D. Weiskopf. Spectral analysis of higher-order and BFECC texture advection. *Proc. VMV*, 87-94, 2012.
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