

b) Dual problem: Minimize  $9y_1 + 54y_2$   
 Subject to  $4y_1 + y_2 \geq 3$   
 $-y_1 + 2y_2 \geq -4$   
 $6y_1 - y_2 \geq 5$   
 $y_1 \geq 0, y_2$  unrestricted

Dual solution:  $y_1 = \frac{10}{9}$   
 $y_2 = -\frac{13}{9}$

Check feasibility:  $4\left(\frac{10}{9}\right) - \frac{13}{9} = 3 \geq 3 \checkmark$   
 $-\frac{10}{9} - \frac{26}{9} = -4 \geq -4 \checkmark$   
 $6\left(\frac{10}{9}\right) + \frac{13}{9} = \frac{73}{9} \geq 5$   
 $y_1 = \frac{10}{9} \geq 0 \checkmark$

Check optimality:  $9\left(\frac{10}{9}\right) + 54\left(-\frac{13}{9}\right) = -68,$

which is optimum value of primal

[ From final tableau, +68 is optimal of  
 problem of minimizing  $-(3x_1 - 4x_2 + 5x_3)$ ,  
 so -68 is optimal of problem of  
 Maximizing  $3x_1 - 4x_2 + 5x_3$  ]