Discrete probability models

Math 30530, Fall 2013

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This was 17th century (Fermat, Pascal) definition of probability