

Discrete Random Variables

Math 30530, Fall 2013

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- Think of random variable as a tool to focus on what's important about the outcome of an experiment