

POD 15

①

$$q_{12} = \frac{\sigma(T_1^4 - T_2^4)}{\frac{1}{e_1} + \frac{1}{e_2} - 1} = \frac{\sigma(T_1^4 - T_2^4)}{\frac{2}{e} - 1}$$

$$\text{so } T_2^4 = -\left(\frac{2}{e} - 1\right) \frac{q_{12}}{\sigma} + T_1^4$$

If we have  $n$  layers

$$q = \frac{\sigma(T_1^4 - T_n^4)}{(n-1)\left(\frac{2}{e} - 1\right)} = q_{12}$$

$$\therefore T_{i+1}^4 = T_i^4 - \frac{(T_1^4 - T_n^4)}{n-1}$$

In space we also have the final layer emitting at  $q = \sigma T_n^4$  w/ no back radiation

$$\therefore e \sigma T_n^4 = \frac{\sigma(T_1^4 - T_n^4)}{(n-1)\left(\frac{2}{e} - 1\right)}$$

$$(n-1)e\left(\frac{2}{e} - 1\right) T_n^4 + T_n^4 = T_1^4$$

$$T_n^4 \left( (n-1)(2 - e) + 1 \right) = T_1^4$$

$$T_n = T_1 \left( \frac{1}{(1 + (2-e)(n-1))} \right)^{1/4}$$

(2)

so if  $e = 0.04$ ,  $n = 5$

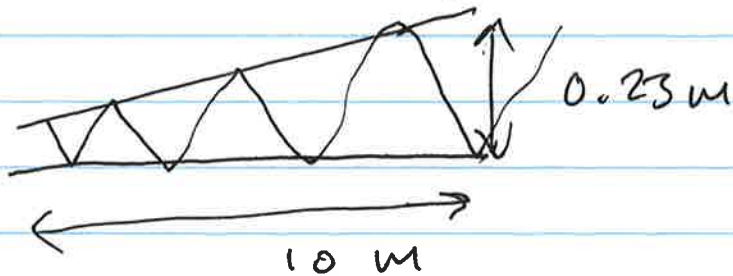
$$T_n = T_1 \left( \frac{1}{1 + 8 - 4e} \right)^{1/4} \approx T_1 \frac{1}{\sqrt{3}}$$

$$T_1 = 383^\circ\text{K}$$

$T_5 = 221^\circ\text{K}$  which matches their description. (max temp of layer 5)

This isn't good enough - which is why it's curved & open at edges!

Angle is ~~~~~  $\sim 0.9^\circ$  spread over  $\sim 10\text{m}$



so because  $e \sim 0.04$  bounces  $\sim 25$  times before absorbed

Thus the flux between each layer is reduced (some heat leaks out edge)

They report min. temp of layer 5 is  $36^\circ\text{K}$