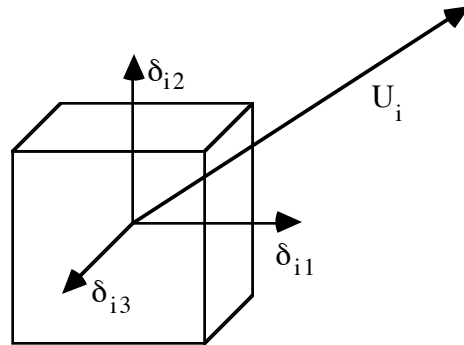


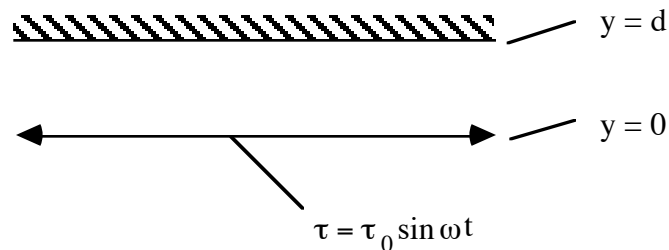
**CHEG 544 Transport Phenomena I
First Hour Exam**

Closed Books and Notes

1). (10 points) Using simple arguments based on the linearity of the creeping flow equations, prove that the drag on a cube under creeping flow conditions is the same regardless of its orientation relative to the direction of motion. (Hint: use the principle that a linear problem may be broken into the sum of several simpler problems)



2). (20 points) Consider the fluid confined within the gap of width d depicted below. If the plane $y=0$ is oscillated back and forth with some oscillatory **shear stress** $\tau = \tau_0 \sin \omega t$, solve for the asymptotic velocity distribution at large times ($\nu t / d^2 \gg 1$). You may leave your answer in the form $u = \text{Im}\{ f(y, t) \}$ where f is a complex function which you have explicitly obtained.



3). (20 points) Re-solve problem 2 for the case where the fluid is initially at rest ($u=0$ everywhere) and we look at the limits $\nu t / d^2 \ll 1$ and $\omega t \ll 1$. Note that in this limit the shear stress at the wall will be a linearly increasing function of time (i.e., $\tau \approx \tau_0 \omega t$) and the problem will admit a similarity transform. Obtain the similarity rule and similarity variable **in canonical form**, together with the resulting ODE **and boundary conditions**, but do not try to obtain an explicit solution. How does the velocity of the plane at $y=0$ vary with time?