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# Countergradient Heat Fluxes and The Impact of Soil Moisture on Katabatic Timing and Structure

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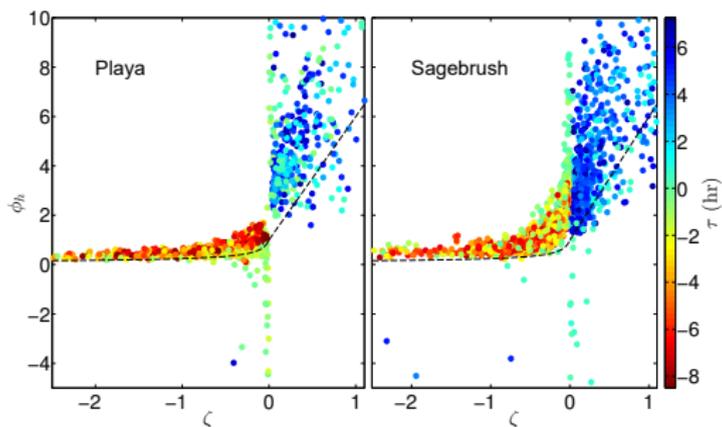
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# Countergradient Heat Flux Observations Near Sunset

## Introduction

- ▶ MOST and analogy to Fourier's law (K-Theory) invalid
- ▶ Occurs when time of flux reversal differs from time of gradient reversal
- ▶ Flux reversal may precede gradient reversal and vice-versa
- ▶ Blay-Carreras et al. (2014) observed the flux reversal preceding the gradient reversal by 30–80 min
- ▶ Study Objective: *Understand and predict the type and duration of the countergradient behavior*



# Countergradient Heat Flux Observations Near Sunset

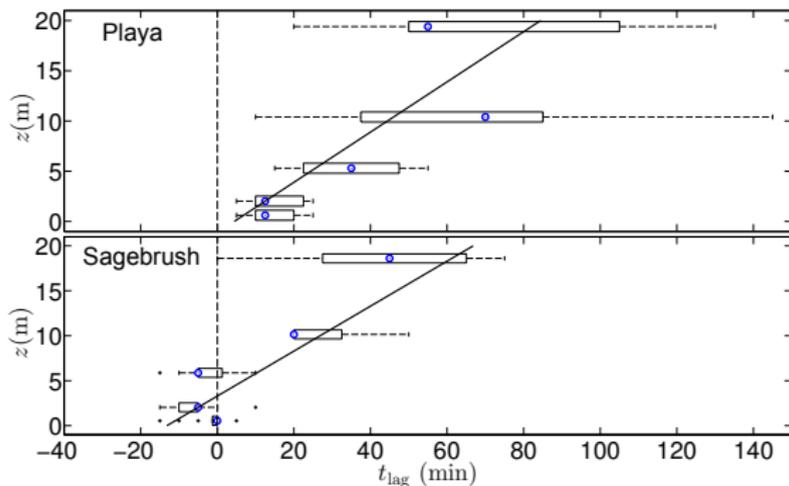
## Background and Definitions

- ▶ Paper accepted in *Boundary-Layer Meteorology* MATERHORN special issue, "Observations of near-surface heat-flux and temperature profiles through the early evening transition over contrasting surfaces"
- ▶ A study of quiescent, clear sky transitions with fully functional instrumentation
  - ▶ 8 days at Playa, 13 at Sagebrush
  - ▶ Individual and ensemble averaged statistics analyzed
- ▶ Timing variable definitions [min]
  - ▶ Time relative to net-radiative sunset:  $\tau \equiv t - t_{R_n=0}$
  - ▶ Time of persistent heat flux reversal:  $\tau_{\text{flux}}$
  - ▶ Time of persistent gradient reversal:  $\tau_{\text{grad}}$
  - ▶ Countergradient duration:  $t_{\text{lag}} \equiv \tau_{\text{flux}} - \tau_{\text{grad}}$

# Countergradient Heat Flux Observations Near Sunset

## Countergradient Duration

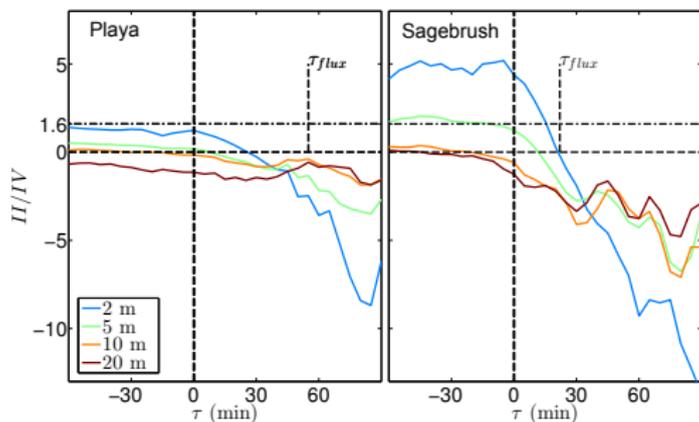
- ▶  $t_{\text{lag}} \equiv \tau_{\text{flux}} - \tau_{\text{grad}}$
- ▶ Hypothesis:  $t_{\text{lag}}(z) \approx -\frac{\partial \tau_{\text{grad}}}{\partial z}(z - z_{\text{ref}}) - t_{\text{lag}}(z_{\text{ref}})$
- ▶  $t_{\text{lag}} < 0 \rightarrow$  flux reversal *precedes* gradient reversal (Blay-Carreras et al., 2014)
- ▶  $t_{\text{lag}} > 0 \rightarrow$  flux reversal *follows* gradient reversal



# Countergradient Heat Flux Observations Near Sunset

## Heat Flux Budget

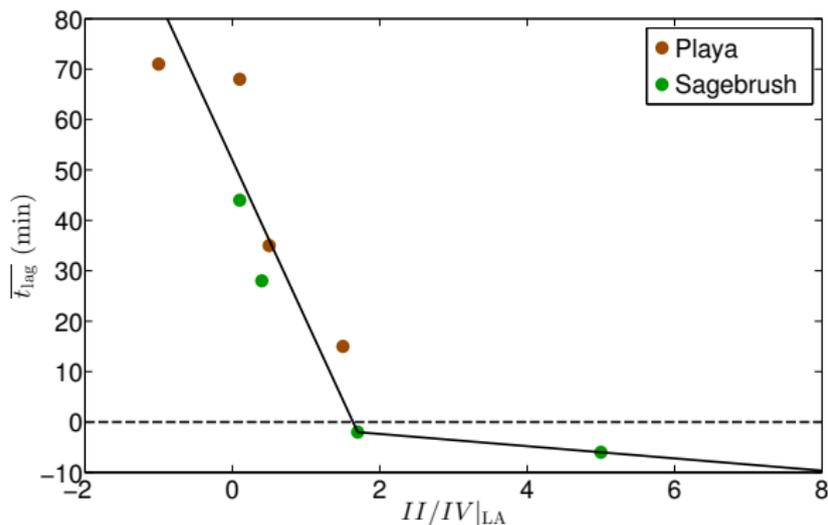
- ▶ Simplified Heat Flux Budget:
 
$$\underbrace{\frac{\partial \overline{w'\theta'}}{\partial t}}_I = \underbrace{-\overline{w'^2}}_{II} \underbrace{\frac{\partial \bar{\theta}}{\partial z}}_{III} - \underbrace{\frac{\partial (\overline{w'^2 \theta'})}{\partial z}}_{III} + \underbrace{\frac{g}{\bar{\theta}}}_{IV} \underbrace{\overline{\theta'}}_{V} - \underbrace{\frac{1}{\rho} \theta' \frac{\partial \rho'}{\partial z}}_{V}$$
- ▶ Hypothesis: Terms II (gradient) and IV (buoyant) dictate countergradient behaviour
- ▶ The ratio of II/IV evaluated in the late afternoon indicate the countergradient type and duration:  $\frac{II}{IV}|_{LA} > 1.6 \rightarrow t_{lag} < 0$  and  $\frac{II}{IV}|_{LA} < 1.6 \rightarrow t_{lag} > 0$



# Countergradient Heat Flux Observations Near Sunset

Late-Afternoon Gradient to Buoyant Production Ratio

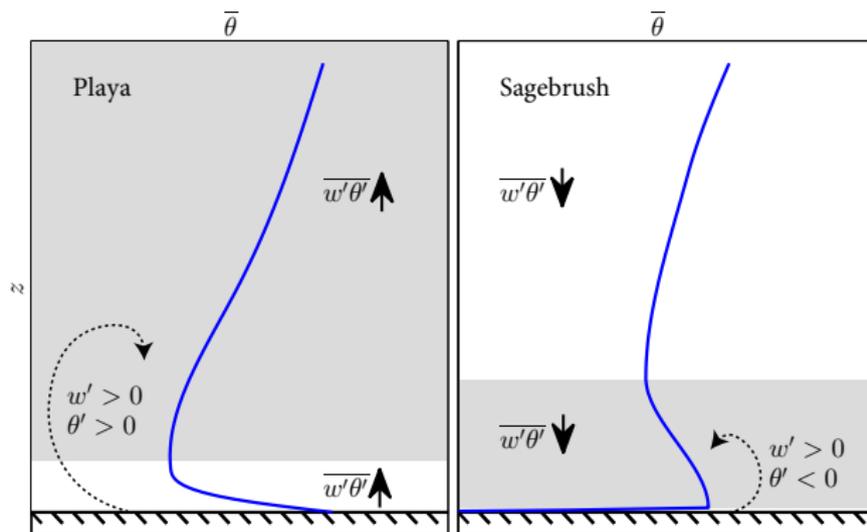
- ▶  $\overline{t_{lag}} > 0$  – well-defined by a linear fit
- ▶  $\overline{t_{lag}} < 0$  – Only 2 points
- ▶ Exact shape of the curve is unknown



# Countergradient Heat Flux Observations Near Sunset

## Idealized Schematic of Countergradient Behaviour

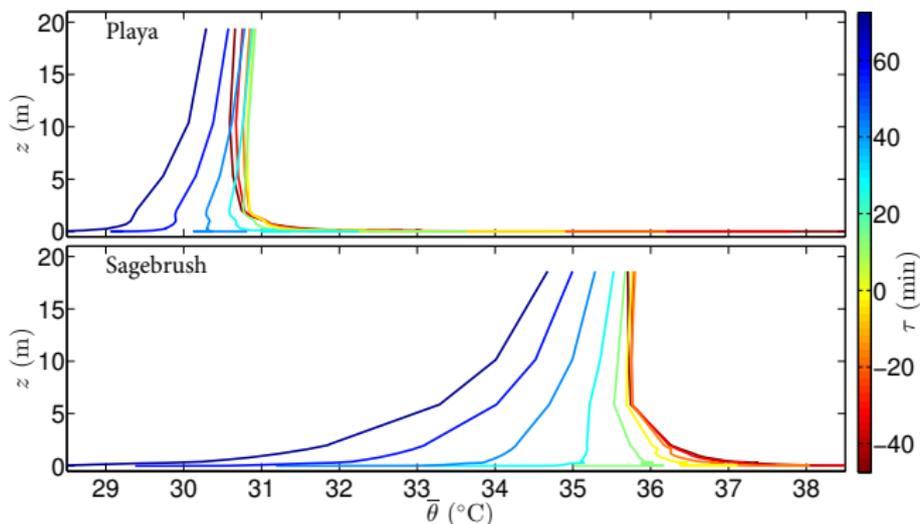
- ▶ Grey shading is a countergradient layer
- ▶ In both cases, the very near-surface flux is co-gradient
- ▶ Flux in countergradient layers is co-gradient with  $\frac{\partial \bar{\theta}}{\partial z} \Big|_{z=0}$



# Countergradient Heat Flux Observations Near Sunset

## Observed Countergradient Behaviour

- ▶ High density temperature with IR surface temperature
- ▶ Cyan curve shows Playa countergradient behaviour
- ▶ Green and cyan curves show Sagebrush countergradient behaviour



# Effect of Soil Moisture on Katabatic Flow

## Background

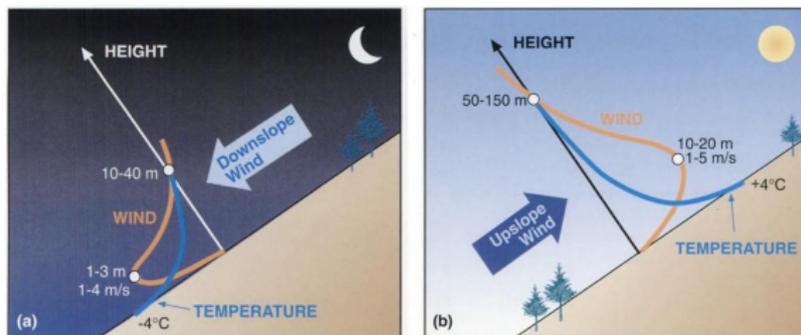


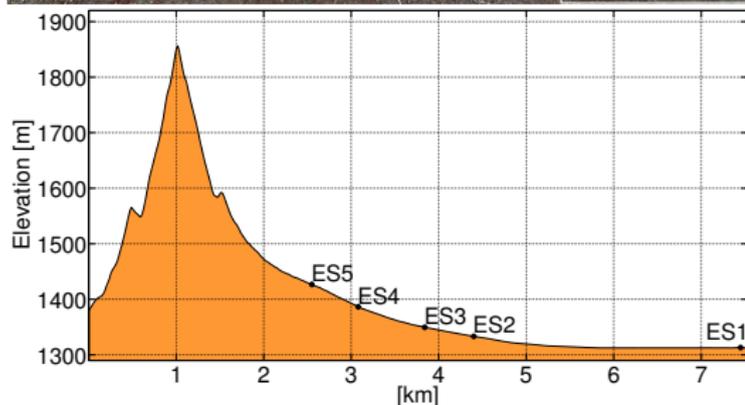
Figure: Taken from Whiteman (2000)

- ▶ Driven by horizontal temperature gradients between valley air mass and the slope
- ▶ Banta and Gannon (1995): From simulations, increased soil moisture retards katabatic flow
- ▶ Study Objective: *Observationally study the impact of increased soil moisture on katabatic development and structure; develop a simple model that incorporates soil moisture*

# Effect of Soil Moisture on Katabatic Flow

## Instrumentation

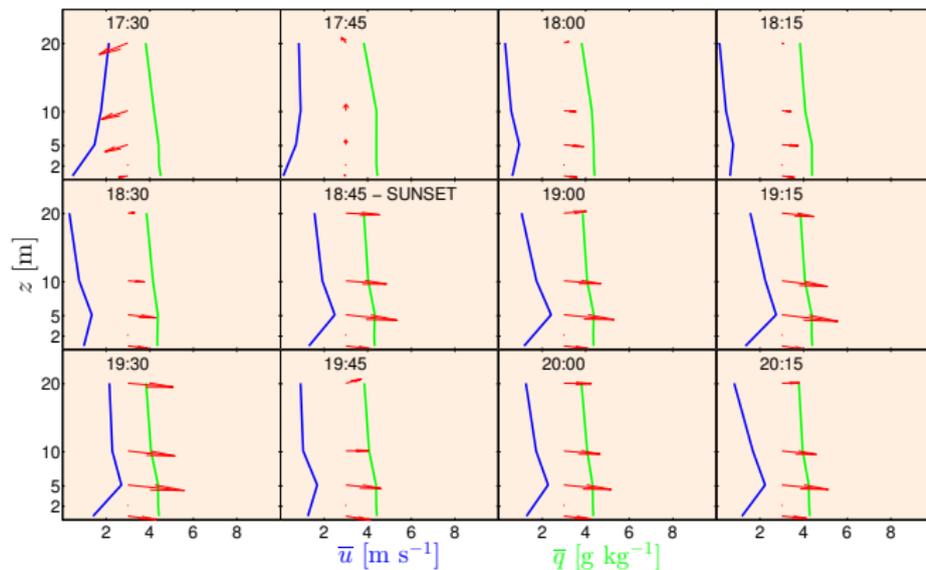
- ▶ Eastern Slope of Granite Peak
- ▶ Desert Steppe Vegetation
- ▶ Low soil moisture
- ▶ Anabatic/katabatic diurnal flow with frequent valley interaction
- ▶ Four 20 m + towers
- ▶ Sonic Anemometers at 5–8 levels
- ▶ Soil moisture and Solar Radiation observations at 6 locations throughout slope



# Effect of Soil Moisture on Katabatic Flow

## Low Soil Moisture Transition

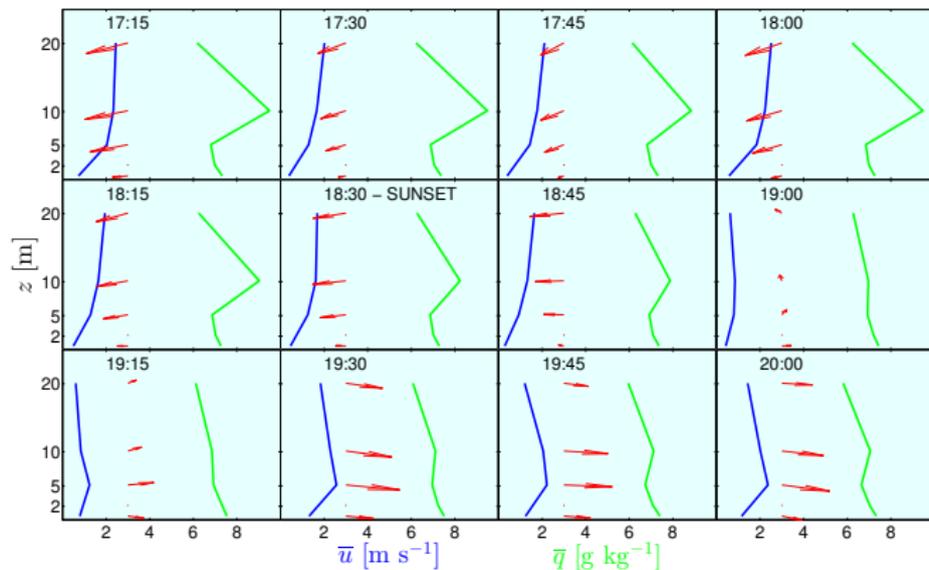
- ▶ 1 Oct. 2012 - Quiescent Synoptic Conditions
- ▶ Soil moisture at 5 cm:  $0.052 \text{ m}^3 \text{ m}^{-3}$
- ▶ Air moisture at 10 m:  $3.7 \text{ g kg}^{-1}$
- ▶ Katabatic flow develops at 18:00 MST, 45 min *before* sunset



# Effect of Soil Moisture on Katabatic Flow

## High Soil Moisture Transition

- ▶ 13 Oct. 2012 - "Quiescent" Synoptic Conditions
- ▶ Soil moisture at 5 cm:  $0.113 \text{ m}^3 \text{ m}^{-3}$
- ▶ Air moisture at 10 m:  $7.1 \text{ g kg}^{-1}$
- ▶ Katabatic flow develops at 19:15 MST, 45 min *after* sunset



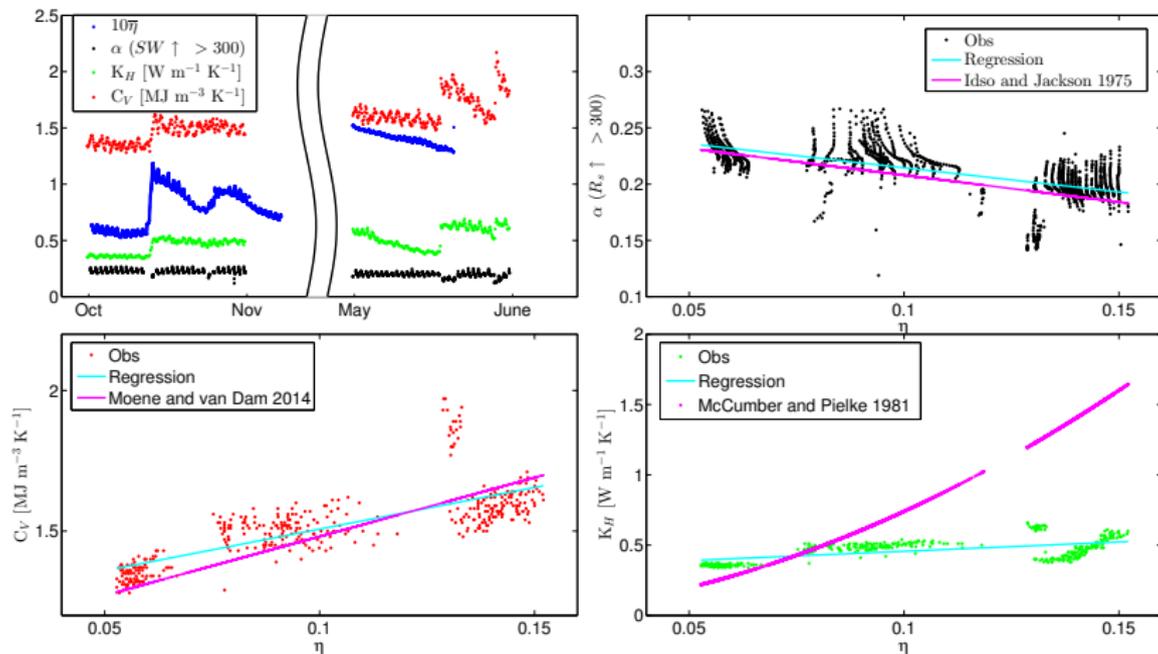
# Effect of Soil Moisture on Katabatic Flow

## Simple Model

- ▶ Model Objective: Use simple inputs to model SEB, katabatic timing and structure
- ▶ Surface Energy Budget
  - ▶  $SW \downarrow = S \cdot T_K \cdot \cos \hat{\theta}$  (Zhang and Anthes, 1982)
  - ▶  $LW \uparrow = \sigma T_0^4$
  - ▶  $LW \downarrow = \text{constant}$
  - ▶ Ground Heat Flux:  $H_G = C_v z_1 \frac{\partial \bar{T}}{\partial t} + K_H \frac{\partial T}{\partial z} |_{z=z_1}$  (Bailey et al., 2015)
  - ▶ Sensible and Latent Heat Flux from Penman-Monteith (Allen, 1998)
- ▶ Soil Properties
  - ▶ Albedo:  $\alpha = \eta_0(\alpha_{\text{dry}} - \alpha_{\text{sat}})/0.2 + \alpha_{\text{dry}}$  (Idso and Jackson, 1975)
  - ▶ Thermal Conductivity:  $K_H = \exp[-\log(\psi_s (\frac{\eta_s}{\eta})^b) + 2.7]$  (Mccumber and Pielke, 1981)
  - ▶ Soil Heat Capacity:  $C_v = (1 - \eta_s) * C_p + \eta C_w$  (Moene and van Dam, 2014)
- ▶ Katabatic Timing and Structure (Manins and Sawford, 1979)
  - ▶ Height:  $H = C_1(\sin \beta)^{2/3} s$
  - ▶ Velocity:  $U = C_2(\sin \beta)^{2/9} \left( -\frac{g}{\theta_{va}} \overline{w' \theta'_0} s \right)^{1/3}$
  - ▶ Temperature Deficit:  $\bar{d} = C_3(\sin \beta)^{-8/9} \left( -\frac{g}{\theta_{va}} \overline{w' \theta'_0} \right)^{2/3} s^{-1/3}$
  - ▶ Start time:  $\bar{u} \frac{\partial \bar{u}}{\partial x} \approx g \bar{d} \frac{\sin \beta}{\theta}$  (Hunt et al., 2003)

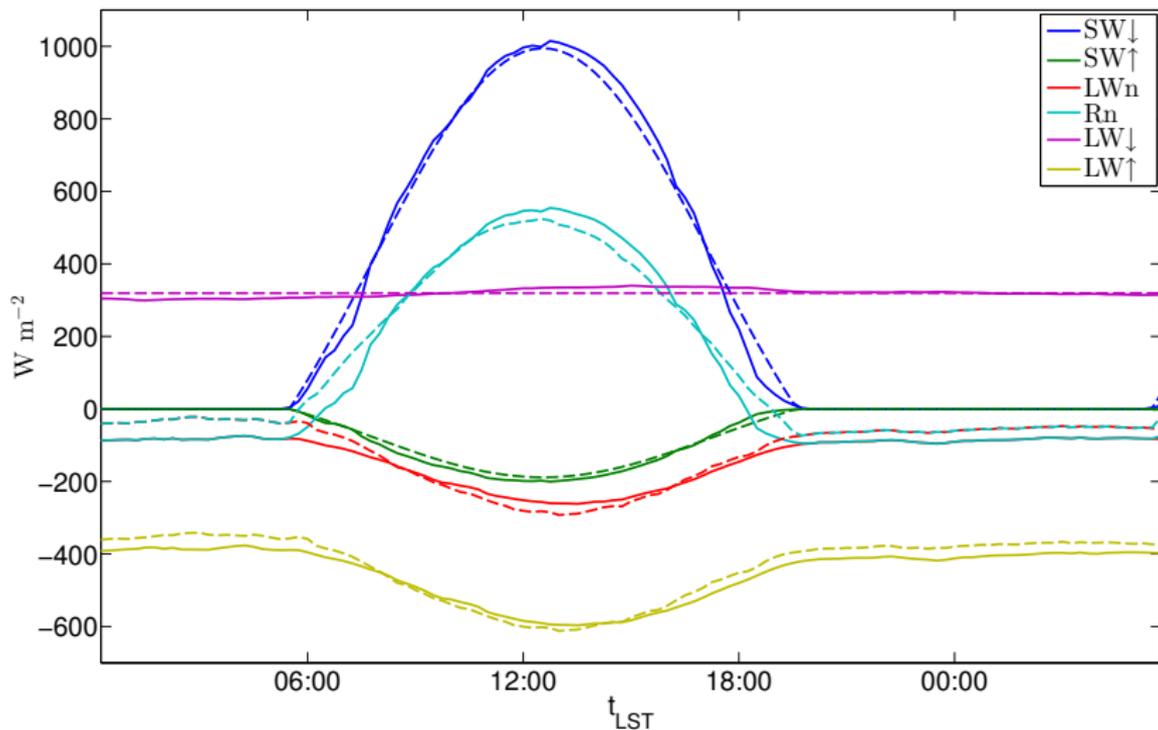
# Effect of Soil Moisture on Katabatic Flow

## Soil Properties



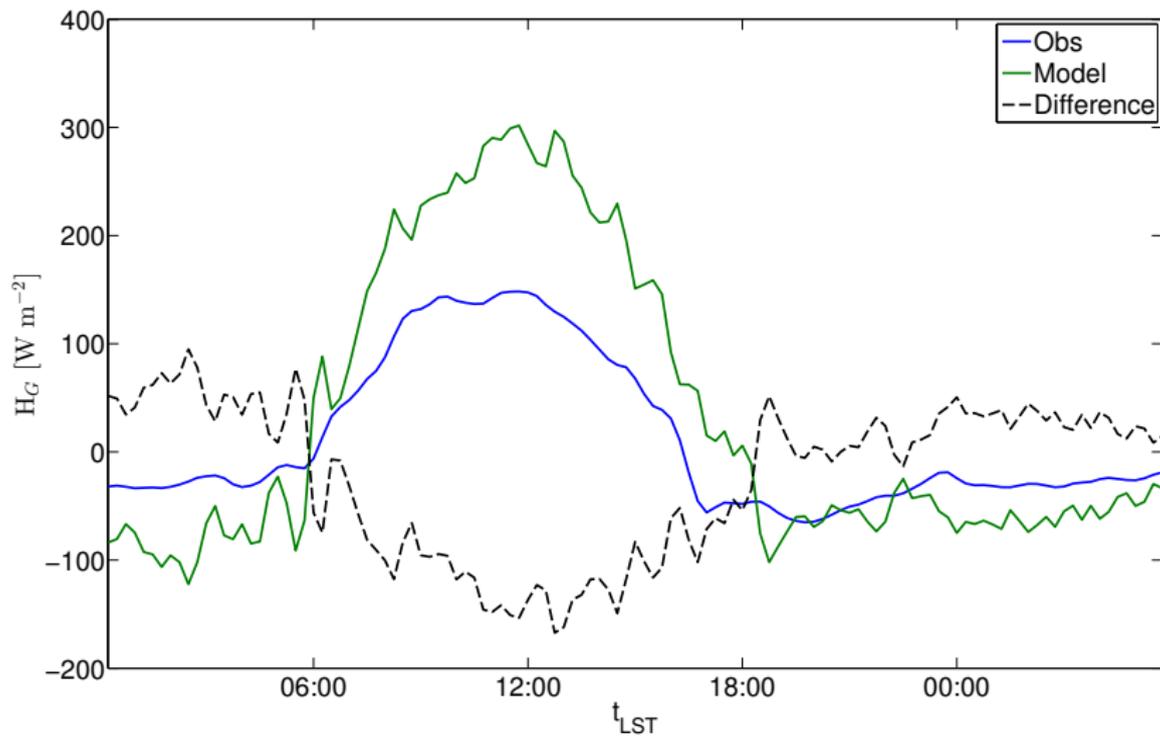
# Effect of Soil Moisture on Katabatic Flow

Radiation Balance: Dashed Line is Modeled



# Effect of Soil Moisture on Katabatic Flow

Ground Heat Flux



# Conclusions

- ▶ Countergradient Heat Flux Observations Near Sunset
  - ▶ Countergradient type and duration can be forecast by the ratio of gradient to buoyant production of sensible heat flux
  - ▶ Heat flux at all levels is co-gradient with  $\frac{\partial \bar{\theta}}{\partial z} |_{z=0}$ , local countergradient fluxes due to “residual” layers
- ▶ Effect of Soil Moisture on Katabatic Flow
  - ▶ Observations show a delay in katabatic development during moist transitions
  - ▶ Models accurately estimate the albedo and heat capacity of the soil as a function of soil moisture, the thermal conductivity model performs poorly
  - ▶ The radiation balance is accurately model but  $H_G$  is overestimated
  - ▶ There's still a lot of work to do!

Thank You!

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