

Rational Homotopy Theory Seminar

Week 9 Problems

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1. Homotoping f, ω, η in the second definition of the Hopf invariant doesn't change " $H(f)$ ". Hint: use Stokes theorem.
2. Define $B = S^3 \setminus K$ where K is the Borromean rings.
 - (a) Compute H^*B as a group
 - (b) Find a minimal model for B . Interpret the products in the minimal model using cup product.
 - (c) Interpret these elements in terms of God
3. Varying choices in the definition of the Massey product changes $\langle x, y, z \rangle$ by an element in $\{xH^*(\mathcal{M}) + zH^*(\mathcal{M})\}$.