

GSTS Exercises - Orthogonal Calculus

4/4/2019

1. Prove $\Theta BO(-)^3 \simeq \Omega^2 \mathbf{mo}(3)$ where $\mathbf{mo}(3)$ is the $\mathbb{Z}/3$ - Moore spectrum.
2. Show $\Theta BTop(-)^{-1} \simeq \mathbf{A}(\ast)$ where $\mathbf{A}(\ast)$ is Waldhausen's A -theory of a point.
3. Show $(\Theta S^{(-)})^{(n)} \simeq O(n)_+ \wedge_{\Sigma_n} \partial_n (Id_{Top\ast})$.
4. Define $\sigma^{(ad)} : E^{(2)}(V) \rightarrow \Sigma^2 E^{(2)}(\mathbb{R} \oplus V)$.
5. Show that $E^{(2)}(V) \rightarrow E(V) \rightarrow \underset{0 \neq U \subset \mathbb{R}^{n+1}}{\text{holim}} E(U \oplus V)$ is a fiber sequence.
6. If E is polynomial of degree 2, show that it takes

$$\begin{array}{ccc}
 V_0 & \longrightarrow & V_1 \\
 \downarrow & & \downarrow \\
 V_2 & \longrightarrow & V_1
 \end{array}$$

to a pullback diagram (???)

7. Show that $BO(V) \rightarrow \underset{0 \neq U \subset \mathbb{R}^{n+1}}{\text{holim}} E(U \oplus V)$ is an equivalence.
8. Sketch construction of $T_n E$.
9. Think about the $O(n)$ - action on $\Theta E^{(n)}$.
10. Given a computational example of the $O(n)$ - action on $\Theta E^{(n)}$.