Consider the function $f(x)=\frac{1}{x^{2}}$ with $x>0$ and its graph.

1. Show that the area $A$ under the graph and above the interval $[1, \infty)$ of the $x$-axis is finite even though it has infinite extent. In fact show that $A=\lim _{c \rightarrow+\infty} \int_{1}^{c} \frac{1}{x^{2}} d x=1$.
2. Show that the area of infinite extent under the graph and above the interval $(0,1]$ given by the improper integral $\lim _{c \rightarrow 0} \int_{c}^{1} \frac{1}{x^{2}} d x$ is infinite.
