Name

Quiz

Consider the function $f(x) = \frac{1}{x^2}$ with x > 0 and its graph.

1. Show that the area A under the graph and above the interval $[1, \infty)$ of the x-axis is finite even though it has infinite extent. In fact show that $A = \lim_{c \to +\infty} \int_{1}^{c} \frac{1}{x^2} dx = 1$.

2. Show that the area of infinite extent under the graph and above the interval (0, 1] given by the improper integral $\lim_{c\to 0} \int_c^1 \frac{1}{x^2} dx$ is infinite.