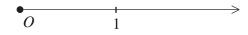
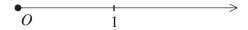
## Quiz

## Name

**1.** Use the polar function  $r = f(\theta) = \frac{1}{\sin \theta}$  and its graph to evaluate the integral  $\int_{\frac{\pi}{6}}^{\frac{\pi}{2}} \frac{5}{\sin^2 \theta} d\theta$ . Illustrate the meaning of the integral on in the polar plane below.



**2.** In the context of Problem 1 evaluate the integral  $\int_{\frac{\pi}{6}}^{\frac{\pi}{2}} \sqrt{f(\theta)^2 + f'(\theta)^2} \, d\theta$ . Illustrate the meaning of this integral on in the polar plane below.



**3.** Consider the equiangular spiral in the polar plane given by  $r = f(\theta) = e^{\theta}$  with  $\theta \ge 0$ . Consider the first two complete revolutions of the spiral and compute the total length, first "on the nose", then by providing a numerical estimate.