Quiz Name

1. Let y = f(x) be a function defined over an interval  $a \le x \le b$ . Describe (in mathematical notation) the process that provides the meaning of the definite integral  $\int_a^b f(x) \, dx$  by interpreting it as a sum of n terms where n is a huge number. (Do so "in the abstract" without making use of graphs, or rectangles, and without mentioning areas or the fundamental theorem of calculus.)

**2.** Approximate  $\int_0^6 (40 - x^2) dx$  by carrying out this process with the small number n = 6. Use the Fundamental Theorem of Calculus to determine the precise value. Sketch the graph of the function involved.