

2.21 closed-loop Gain $A_v = -\frac{R_2}{R_1}$, one $R = 10\text{ k}\Omega$, the other $R \geq 10\text{ k}\Omega$.

(a) $A_v = -1\text{ V/V} = -\frac{R_2}{R_1} \Rightarrow R_1 = R_2 = 10\text{ k}\Omega$

(b) $A_v = -2\text{ V/V} = -\frac{R_2}{R_1} \Rightarrow R_1 = 10\text{ k}\Omega, R_2 = 20\text{ k}\Omega$

(c) $A_v = -0.5\text{ V/V} = -\frac{R_2}{R_1} \Rightarrow R_1 = 20\text{ k}\Omega, R_2 = 10\text{ k}\Omega$

(d) $A_v = -100\text{ V/V} = -\frac{R_2}{R_1} \Rightarrow R_1 = 10\text{ k}\Omega, R_2 = 1\text{ M}\Omega$

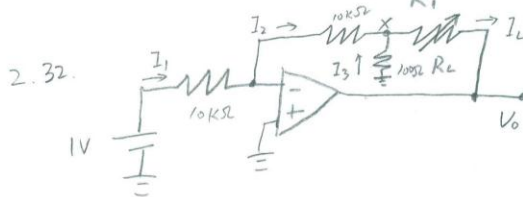


Fig. 1.

a. $I_1 = \frac{1\text{ V}}{10\text{ k}\Omega} = 0.1\text{ mA}$

$I_2 = I_1 = 0.1\text{ mA}$

$I_3 \times 100\Omega = I_2 \times 10\text{ k}\Omega \Rightarrow I_3 = 10\text{ mA}$

$-V_x = I_3 \times 100\Omega \Rightarrow V_x = -1\text{ V}$

$I_L = I_2 + I_3 = 10.1\text{ mA}$

b. $R_{L, \max} = \frac{V_x - V_{0, \min}}{I_L} = 1188\Omega$

c. $100\Omega \leq R_L \leq 1\text{ k}\Omega$

$I_L = I_2 + I_3 = 10.1\text{ mA}, V_x = -1\text{ V}$

$V_o = V_x - R_L \cdot I_L$, linear relationship.

when $R_L = 100\Omega$, $V_o = -2.01\text{ V}$ & when $R_L = 1\text{ k}\Omega$, $V_o = -11.1\text{ V}$

$\Rightarrow -11.1\text{ V} \leq V_o \leq -2.01\text{ V}$.

2.46. $v_i = v = V_o = R \cdot i \Rightarrow R = \frac{V}{i} = \frac{10\text{ V}}{0.1\text{ mA}} = 100\text{ k}\Omega$

i only depends on v and R . The meter resistance does NOT affect it.

2.51.

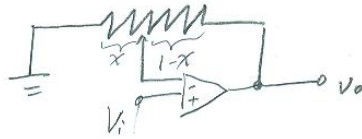


Fig 2 (a)

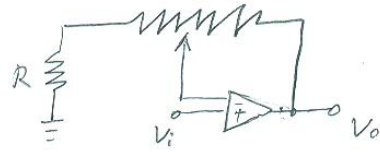


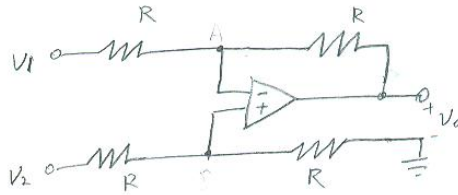
Fig 2 (b)

In Fig 2(a), $\frac{V_o}{V_i} = 1 + \frac{1-x}{x} = \frac{1}{x}$, $0 \leq x \leq 1 \Rightarrow 1 \leq \frac{V_o}{V_i} \leq \infty$

In Fig 2 (b), we add a resistor \$R\$, $\frac{V_o}{V_i} = 1 + \frac{(1-x) \times 10k\Omega}{x \times 10k\Omega + R}$

when $\frac{V_o}{V_i} \Big|_{\max} = 11$ $x=0$. $\frac{V_o}{V_i} = 1 + \frac{10k\Omega}{R} \Rightarrow R = 1k\Omega$

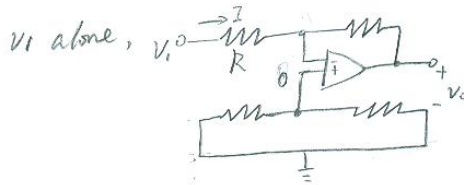
2.62.



$V_+ = V_-$

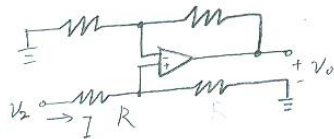
$\Rightarrow V_1 + \frac{V_o - V_1}{2} = \frac{V_2}{2} \Rightarrow V_o = V_2 - V_1$

or $\frac{V_o}{V_2 - V_1} = \frac{R_2}{R_1} = \frac{R}{R} = 1 \Rightarrow V_o = V_2 - V_1$



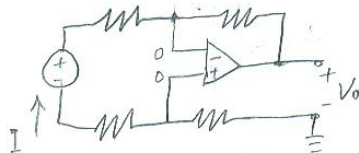
$R_i = \frac{V_1}{I} = R$

V_2 alone,



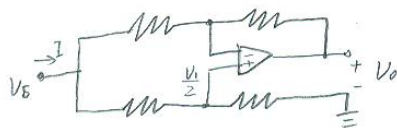
$R_i = \frac{V_2}{I} = 2R$

V_s between V_1 & V_2



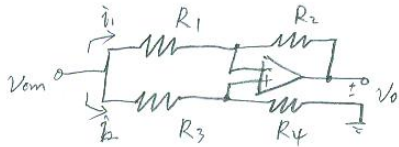
$R_i = \frac{V}{I} = 2R$

V_s connected to both V_1 and V_2



$R_i = \frac{V}{I} = R$

2.63



$$V_+ = V_- = V_{cm} \frac{R_4}{R_3 + R_4}$$

$$i_2 = \frac{V_{cm}}{R_3 + R_4}$$

$$i_1 = \frac{V_{cm} - V_-}{R_1} = \frac{V_{cm} - \frac{V_{cm} R_4}{R_3 + R_4}}{R_1} = V_{cm} \left(\frac{1}{R_1} - \frac{R_4}{R_1(R_3 + R_4)} \right)$$

$$\frac{R_1}{R_2} = \frac{R_3}{R_4} \Rightarrow \frac{R_4}{R_3 + R_4} = \frac{R_2}{R_1 + R_2} \Rightarrow i_1 = V_{cm} \left(\frac{1}{R_1} - \frac{R_2}{R_1(R_1 + R_2)} \right)$$

$$= V_{cm} \cdot \frac{R_1 + R_2 - R_2}{R_1(R_1 + R_2)} = \frac{V_{cm}}{R_1 + R_2}$$

$$i = i_1 + i_2 = \frac{V_{cm}}{R_1 + R_2} + \frac{V_{cm}}{R_3 + R_4} = V_{cm} \left(\frac{1}{R_1 + R_2} + \frac{1}{R_3 + R_4} \right)$$

$$\Rightarrow \frac{1}{R} = \frac{1}{R_1 + R_2} + \frac{1}{R_3 + R_4} \Rightarrow (R_1 + R_2) \parallel (R_3 + R_4)$$

2.73 (a) Gain $A_v = 1 + \frac{R_2}{R_1} = 101$

If the op amps saturate at $\pm 14V$ $-14V \leq V_o \leq 14V \Rightarrow \frac{-14}{101} \leq V_{icm} \leq \frac{14}{101}$

$$\Rightarrow -0.14V \leq V_{icm} \leq 0.14V$$

(b) In Fig 2.20 b, V_- for A_1 and A_2 is the same, so no current flow through $2R_1$.

$\Rightarrow V_o$ for A_1 & A_2 is the same as V_{icm}

$$-14V \leq V_o \leq 14V \Rightarrow -14V \leq V_{icm} \leq 14V$$

Compared with Fig 2.20 a, the circuit in Fig 2.20 b allow for bigger range of V_{icm} .

2.83 $R_m = R = 20\text{ k}\Omega$, $\omega = 2\pi \times 10\text{ kHz}$.

$$|T| = \frac{1}{\omega RC} = 1 \Rightarrow C = \frac{1}{2\pi \times 10\text{ kHz} \times 20\text{ k}\Omega} = 0.796\text{ nF}$$

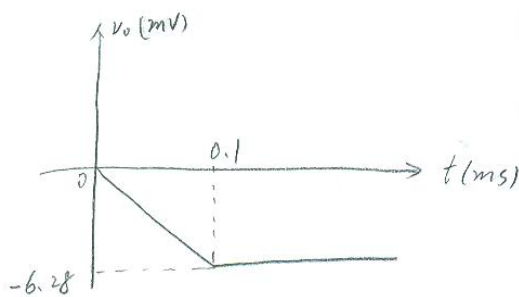
$$\frac{v_o}{v_i} = \frac{R_F / R}{1 + sCR_F}$$

the finite DC gain is $-\frac{R_F}{R}$

$$40\text{ dB} = 100\text{ V/V} \Rightarrow -\frac{R_F}{R} = -100\text{ V/V} \Rightarrow R_F = 100 \times 2\text{ k}\Omega = 200\text{ k}\Omega$$

The corner frequency is $\frac{1}{CR_F} = \frac{1}{0.796\text{ nF} \times 200\text{ k}\Omega} = 628\text{ Hz}$

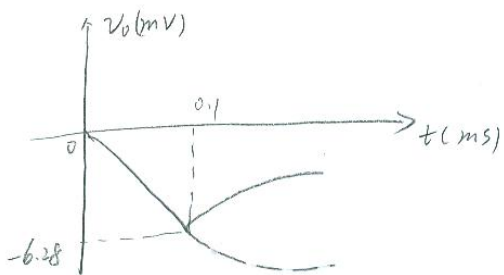
(a) Without R_F



$$v_o(t) = \frac{-1}{RC} \int_0^t 1 dt = -62.8t \quad 0 \leq t \leq 0.1\text{ ms}$$

$$v_o(0.1) = -6.28\text{ mV}$$

(b) with R_F



$$v_o(t) = v_o(\infty) (1 - e^{-t/CR_F})$$

$$v_o(\infty) = -1 \times R_F = -\frac{1\text{ V}}{20\text{ k}\Omega} \times 200\text{ k}\Omega = -100\text{ V}$$

$$v_o(t) = -100 (1 - e^{-t/1.6})$$

2.88. $\frac{v_o}{v_i}(s) = -sRC = -s \times 0.01 \times 10^{-6} \times 10 \times 10^3 = 10^{-4}s$

$$\frac{v_o}{v_i}(j\omega) = -j\omega \times 10^{-4} \Rightarrow \left| \frac{v_o}{v_i} \right| = \omega \times 10^{-4} = 10^4 \text{ rad/s} \times 10^{-4} = 1$$

For $10f_0$, $\left| \frac{v_o}{v_i} \right| = 10$, 10V peak to peak
 $\phi = 90^\circ$ $f = 1.59\text{ kHz}$

$$\Rightarrow v_o(t) = -5 \sin(\omega t + \phi) = -5 \sin(10^5 t + 90^\circ)\text{ V}$$