## Math 30710 Assignments, Spring 2023

Reading should be completed before class on the given date.
Be careful to justify your solution when a homework problem calls for it. Assignments are due on FRIDAYS unless otherwise specified. As long as we are holding class in the classroom, physical assignments will be collected in class. If we have to go online, instructions will be given at that time for turning in your work. The future, as-yet unassigned assignments below are subject to revision.

| Date | Section/Topic | Reading (page numbers) | Problems | Due |
| :---: | :---: | :---: | :---: | :---: |
| 1/18/23 | 0. Sets and relations | 1-8 | $\begin{aligned} & \S 0: \# 3,5,7,11,12,13,15, \\ & 16,17,25,28,31,32 \end{aligned}$ | 1/27/23 |
| $\begin{aligned} & 1 / 20 / 23, \\ & 1 / 23 / 23 \end{aligned}$ | 1. Introduction | 11-18 | $\begin{aligned} & \S 1: \# 3,7,11,13,19,23, \\ & 29,33,35,37,39,40 \end{aligned}$ | 1/27/23 |
| 1/25/23 | 2. Binary operations | 20-25 | §2: \#2-8, 12, 14-18, 23, 24 | 2/3/23 |
| 1/27/23 | 3. Isomorphisms | 28-34 | $\begin{aligned} & \S 3: \# 1,2-4,6-7,17,20-23, \\ & 26-29 \end{aligned}$ | $2 / 3 / 23$ |
| 1/30/23 | 4. Groups | 36-43 | $\begin{aligned} & \S 4: ~ \# 1-3,7,10,11-13,19 \\ & 22,23,25 \end{aligned}$ | 2/10/23 |
| 2/1/23 | 4/5. Groups/subgroups | 43-45, 49-52 | $\begin{aligned} & \S 4: \# 26-28,31-33 ; \S 5: 1,2, \\ & 5,11-12,14 \end{aligned}$ | 2/10/23 |
| 2/3/23 | 5. Subgroups | 53-55 | $\begin{aligned} & \S 5: \# 20,22,23,26,36,39 \\ & 42,44,53,54 \end{aligned}$ | 2/10/23 |
| 2/6/23 | 6. Cyclic groups | 59-65 | $\begin{aligned} & \S 6: \# 1,5,11,14,15,17, \\ & 20,21,22,25,30,31,32 \\ & \hline \end{aligned}$ | 2/17/23 |
| $\begin{aligned} & \hline 2 / 8 / 23, \\ & 2 / 10 / 23 \\ & \hline \end{aligned}$ | 6. Cyclic Groups |  | §6: \#36, 37, 38, 42, 44, 49; | 2/17/23 |
| $\begin{aligned} & 2 / 13 / 23, \\ & 2 / 15 / 23 \\ & \hline \end{aligned}$ | 7. Generators and Cayley digraphs | 68-72 | $\begin{aligned} & \S 7: \# 1,6,7,9,10,16,17 \\ & 18,19 \text { (Hint: see } \# 9) \end{aligned}$ | 2/24/23 |
| 2/15/23 | 8. Permutation groups | 75-81 | $\begin{aligned} & \S 8: \# 1,5,6,8,10,11,17, \\ & 18,23,24 \end{aligned}$ | 2/24/23 |
| 2/17/23 | 8. Permutation groups, Cayley's theorem | 81-83 | $\begin{aligned} & \S 8: \# 30,31,35,39,41,43, \\ & 47 \end{aligned}$ | 2/24/23 |
| 2/20/23 | Proof of Cayley's theorem |  | - | - |
| 2/22/23 | 9. Orbits, cycles, even and odd permutations, alternating groups | 87-93 | - | - |
| 2/24/23 | 9. Orbits, cycles, even and odd permutations, alternating groups |  | $\begin{aligned} & \S 9: \# 1,6,7,10,13,14,15 \\ & 19-23,29,34 \end{aligned}$ | 3/10/23 |
| 2/27/23 | Review | - | - | - |
| $3 / 1 / 23$ | Exam 1 | Includes all material in sections 1-8 and 1st part of $\S 9$. | - | - |
| $3 / 3 / 23$ | 9. Orbits, cycles, even and odd permutations, alternating groups | - | - | - |
| 3/6/23 | 10. Cosets | 96-100 | $\begin{aligned} & \S 10: \# 1-4,6-7,12,13,15 \\ & 19,20-24 \end{aligned}$ | 3/24/23 |
| 3/8/23 | 10 Lagrange's Theorem | 100-101 | §10: \#27, 30-34, 37, 41, 43 | 3/24/23 |
| 3/10/23 | 11. Products | 104-110 | Get started on §11 HW | - |
| $3 / 20 / 23$ | 11. Finite abelian groups | 104-110 | $\begin{aligned} & \S 11: \# 1,2,7,8,9,13,14, \\ & 18,20,24,32,36,46,47 \end{aligned}$ | 3/31/23 |
| 3/22/23 | 13. Homomorphisms | 125-129 | $\begin{aligned} & \S 13: \# 1-5,9,10,16,17,22 \\ & 24,25,28,29 \end{aligned}$ | 3/31/23 |


| $3 / 24 / 23$ | 13. Homomorphisms | 129-133 | $\begin{aligned} & \S 13: \# 32,33,34,39,42,47, \\ & 48,49,52 \end{aligned}$ | 3/31/23 |
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| 3/27/23 | 14. Factor groups | 135-139 | §14: \#1, 2, 7, 9, 10 | 4/14/23 |
| 3/29/23 | 14. Factor groups | 139-141 | $\begin{aligned} & \S 14: \# 17,18,20,23 a-d, 24, \\ & 30 \end{aligned}$ | 4/14/23 |
| $3 / 31 / 23$ | 14. Factor groups summary | 135-141 | - | - |
| 4/3/23 | 15. Factor groups/Simple groups | 144-148 | §15: \#1-5, 19, 28 | 4/14/23 |
| $\begin{aligned} & 4 / 5 / 23, \\ & 4 / 12 / 23 \\ & \hline \end{aligned}$ | 15. Factor groups/Simple groups | 149-151 | §15: \#30, 31, 34 | 4/14/23 |
| 4/14/23 | 18. Rings and Fields | 167-170 | $\begin{aligned} & \S 18: \# 3,5,7,9,11,14,15, \\ & 16,17,19 \end{aligned}$ | 4/28/23 |
| 4/17/23 | Review |  |  |  |
| 4/19/23 | Exam 2 | Covers $\S \S 9,10,11,13$, 14, 15 |  |  |
| 4/21/23 | 18. Rings and Fields | 171-174 | $\begin{aligned} & \S 18: \# 20,22,23,24,25,27 \text {, } \\ & 28,33,37,38 \end{aligned}$ | 4/28/23 |
| 4/24/23 | $24 / 19$ <br> Quaternions/Domains | 177-179, 224-226 | §19: \#1-4, §24: 4-7 | 4/28/23 |
| $\begin{aligned} & 4 / 26 / 23, \\ & 4 / 28 / 23 \end{aligned}$ | 19. Domains | 177-182 | $\begin{aligned} & \S 19: \# 5,7,9,11,12,14 \\ & 15-18,23,29 \end{aligned}$ | not collected, but do them! |
| 4/28/23 | 20. Fermat's and Euler's theorems | 184-189 | §20: \#1-10 | not collected, but do them! |
|  | 20. Fermat's and Euler's theorems (cont.) |  |  |  |
|  | 21. Field of Quotients | 190-196 | §21: \#1, 2, 4, 5, 6-11 |  |
|  | 22. Polynomials | 198-207 | $\begin{aligned} & \S 22: \# 1,2,6,7,9,13,17 \\ & 22,23,25 \end{aligned}$ |  |
|  | 23. Factorization | 209-214 | §23: \#2, 4, 6, 8, 9, 11, 13 |  |
|  | 23. Factorization (cont.); <br> 26. Ideals | 209-218 | $\begin{aligned} & \S 23: \# 14,16,18,20,21,25 \\ & 26,27,28 \end{aligned}$ |  |
| 5/1/23 | 26. Ideals, Factor rings | 237-243 | §26: \#3, 4, 17 | not collected, but do them! |
|  | Factor rings, finite fields |  |  |  |
|  | Applications to geometry |  |  |  |
|  | 29. Field extensions, 31. <br> Algebraic extensions | 265-272, 283-286 | $\begin{aligned} & \S 29: \# 1,3,9,10,11,13 \\ & \S 31: 1-6 \end{aligned}$ |  |
|  | 32. Geometric constructions | 293-299 |  |  |

