

For LS coupling of identical particles, we have the restriction $L + S$ is even. The LS states are:

$$\begin{aligned}
(3s3s) &\rightarrow {}^1S && 1 \text{ substate} \\
(3p3p) &\rightarrow {}^1S, {}^3P, {}^1D && 1 + 9 + 5 = 15 \text{ substates} \\
(3d3d) &\rightarrow {}^1S, {}^3P, {}^1D, {}^3F, {}^1G && 1 + 9 + 5 + 21 + 9 = 45 \text{ substates} \\
(3s3d) &\rightarrow {}^1D, {}^3D && 5 + 15 = 20 \text{ substates}
\end{aligned}$$

For jj coupling of identical particles J is even. The jj coupled states are

$$\begin{aligned}
(3s_{1/2} 3s_{1/2}) &\rightarrow [0] && 1 \text{ substate} \\
(3p_{1/2} 3p_{1/2}) &\rightarrow [0] && 1 \text{ substate} \\
(3p_{1/2} 3p_{3/2}) &\rightarrow [1], [2] && 3+5= 8 \text{ substates} \\
(3p_{3/2} 3p_{3/2}) &\rightarrow [0], [2] && 1+5= 6 \text{ substates} \\
(3d_{3/2} 3d_{3/2}) &\rightarrow [0], [2] && 1+5= 6 \text{ substates} \\
(3d_{3/2} 3d_{5/2}) &\rightarrow [1], [2], [3], [4] && 3+5+7+9= 24 \text{ substates} \\
(3d_{5/2} 3d_{5/2}) &\rightarrow [0], [2], [4] && 1+5+9= 15 \text{ substates} \\
(3s_{1/2} 3d_{3/2}) &\rightarrow [1], [2] && 3+5= 8 \text{ substates} \\
(3s_{1/2} 3d_{5/2}) &\rightarrow [2], [3] && 5+7= 12 \text{ substates}
\end{aligned}$$

In either coupling scheme there are a total of 81 magnetic substates.

For LS coupling of identical particles, we have the restriction $L + S$ is even. As a first step, couple two particles

$$\begin{aligned}
(2s2s) &\rightarrow {}^1S && \text{even-parity} \\
(2s2p) &\rightarrow {}^1P, {}^3P && \text{odd-parity} \\
(2p2p) &\rightarrow {}^1S, {}^3P, {}^1D && \text{even-parity}
\end{aligned}$$

For an even parity 3-particle state couple two $2p$ states ($2p2p$) then couple the resulting state with the $2s$ ($(2p2p)[LS]2s$). The possible combinations are

$$\begin{aligned}
(2p2p) [{}^1S] 2s {}^2S &&& 2 \times 1 \text{ substates} \\
(2p2p) [{}^3P] 2s {}^2P &&& 2 \times 3 \text{ substates} \\
(2p2p) [{}^3P] 2s {}^4P &&& 4 \times 3 \text{ substates} \\
(2p2p) [{}^1D] 2s {}^2D &&& 2 \times 5 \text{ substates}
\end{aligned}$$

Total number of substates = 2+6+12+10=30

For jj coupling of identical particles J is even. The ($2p2p$) states are

$$\begin{aligned}
(3p_{1/2}3p_{1/2}) &\rightarrow [0] \\
(3p_{1/2}3p_{3/2}) &\rightarrow [1], [2] \\
(3p_{3/2}3p_{3/2}) &\rightarrow [0], [2]
\end{aligned}$$

Combining these with a $2s$ state leads to

$[(3p_{1/2} 3p_{1/2})[0] 2s_{1/2}] [1/2]$	2 substates
$[(3p_{1/2} 3p_{3/2})[1] 2s_{1/2}] [1/2] \& [3/2]$	2+4=6 substates
$[(3p_{1/2} 3p_{3/2})[2] 2s_{1/2}] [3/2] \& [5/2]$	4+6=10 substates
$[(3p_{1/2} 3p_{3/2})[0] 2s_{1/2}] [1/2]$	2 substates
$[(3p_{1/2} 3p_{3/2})[2] 2s_{1/2}] [3/2] \& [5/2]$	4+6=10 substates

Total number of substates = 2+6+10+2+10=30