

- **Decidable Languages:** Some TM exists which will accept any string w that is in L , and reject any string not in L . The TM always halts.
 - (p. 194) $A_{DFA} = \{ \langle B, w \rangle \mid B \text{ is a DFA that accepts } w \}$
 - (p. 195) $A_{NFA} = \{ \langle B, w \rangle \mid B \text{ is an NFA that accepts } w \}$
 - (p. 196) $A_{REG} = \{ \langle R, w \rangle \mid R \text{ is a regex that generates } w \}$
 - (p. 196) $E_{DFA} = \{ \langle A \rangle \mid A \text{ is a DFA where } L(A) = \Phi \}$
 - (p. 197) $EQ_{DFA} = \{ \langle A, B \rangle \mid A, B \text{ both DFAs \& } L(A) = L(B) \}$
 - (p. 198) $A_{CFG} = \{ \langle G, w \rangle \mid G \text{ is a CFG that generates } w \}$
 - (p. 199) $E_{CFG} = \{ \langle G \rangle \mid G \text{ is a CFG \& } L(G) = \Phi \}$
 - (p. 200) Every CFL is decidable
 - (Prob. 4.3) $ALL_{DFA} = \{ \langle A \rangle \mid A \text{ a DFA and } L(A) = \Sigma^* \}$
 - (Prob. 4.4) $A\epsilon_{CFG} = \{ \langle G \rangle \mid G \text{ a CFG that generates } \epsilon \}$
 - (Prob. 4.10) $INFINITE_{DFA} = \{ \langle A \rangle \mid A \text{ a DFA, } L(A) \text{ is infinite} \}$
 - (Prob. 4.11) $INFINITE_{PDA} = \{ \langle A \rangle \mid A \text{ a PDA, } L(A) \text{ is infinite} \}$

- **Undecidable Languages:** A decider does not exist.
 - (p. 202) $\text{HALT}_{\text{TM}} = \{\langle M, w \rangle \mid M \text{ is a TM that halts on } w\}$
 - (p. 207) $\text{A}_{\text{TM}} = \{\langle M, w \rangle \mid M \text{ accepts } w\}$
 - (p. 217) $\text{E}_{\text{TM}} = \{\langle M \rangle \mid M \text{ is a TM and } L(M) = \Phi\}$
 - (p. 218) $\text{REGULAR}_{\text{TM}} = \{\langle M \rangle \mid M \text{ a TM \& } L(M) \text{ is regular}\}$
 - (p. 219) $\text{L}_P = \{\langle M \rangle \mid M \text{ a TM such that } L(M) \text{ has property } P\}$
 - (p. 220) $\text{EQ}_{\text{TM}} = \{\langle M_1, M_2 \rangle \mid M_1, M_2 \text{ TMs, } L(M_1) = L(M_2)\}$
 - (p. 222) $\text{A}_{\text{LBA}} = \{\langle M, w \rangle \mid M \text{ an LBA that accepts } w\}$
 - (p. 223) $\text{E}_{\text{LBA}} = \{\langle M \rangle \mid M \text{ an LBA where } L(M) \text{ is empty}\}$
 - (p. 225) $\text{ALL}_{\text{CFG}} = \{\langle G \rangle \mid G \text{ is CFG where } L(G) = \Sigma^*\}$
 - (p. 228) $\text{PCP} = \{\langle P \rangle \mid P \text{ instance of Post Correspondence Problem}\}$

- **Recognizable Languages:** Some TM exists which can accept any string w that is in L , and will not accept any string not in L . No guarantees that TM will even halt for w not in L .
- **co-Turing Recognizable Languages:** a TM recognizer exists for the complement of the language
 - (Prob. 4.5) $\text{E}_{\text{TM}} = \{\langle M \rangle \mid M \text{ is a TM and } L(M) = \Phi\}$
- If L is both recognizable and co-Turing recognizable then it is decidable

- **Class P**: decidable by a 1-tape TM in poly time
 - (p. 287) **PATH** = $\{\langle G,s,t \rangle \mid G \text{ is directed graph } (V,E), \text{ with path from } s \text{ to } t\}$
 - (p. 289) **RELPRIME** = $\{\langle x,y \rangle \mid x,y \text{ relatively prime}\}$
 - (Prob. 7.8) **CONNECTED** = $\{\langle G \rangle \mid G \text{ is a connected undirected graph}\}$
 - (Prob. 7.9) **TRIANGLE** = $\{\langle G \rangle \mid G \text{ contains a triangle}\}$
 - (Prob. 7.10) **ALL_{DFA}**
 - (Prob. 7.13) **MODEEXP** = $\{(a,b,c,p) \mid \text{positive binary integers such that } a^b = c \pmod p\}$
 - (p. 290) Every context-free language is in P
- **Class NP**: Not in P but a poly time NTM exists (* in NP-Complete)
 - ***HAMPATH** = $\{(G,s,t) \mid G \text{ is graph with Hamiltonian path from } s \text{ to } t\}$
 - **COMPOSITES** = $\{x \mid x=pq, \text{ for } p,q>1\}$
 - ***CLIQUE** = $\{\langle G,k \rangle \mid G \text{ undirected graph with } k\text{-clique}\}$
 - ***SUBSET-SUM** = $\{\langle S,t \rangle \mid S = \{x_1, \dots, x_k\}\}$
 - ***SAT** = $\{\text{wff} \mid \text{wff is satisfiable}\}$
 - ***VERTEXCOVER** = $\{\langle G,k \rangle \mid G \text{ has a } k\text{-node vertex cover}\}$