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## Improved range image segmentation by analyzing surface fit patterns

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### 8 Abstract

9 We propose a new approach to range image segmentation of planar and curved surface  
10 scenes. Our method is mainly an extended design of an existing algorithm, which was guided  
11 by a framework of performance evaluation. We choose the range segmentation algorithm  
12 developed by Jiang and Bunke as our baseline algorithm, which is fast and has shown rela-  
13 tively high performance in several experimental performance evaluation studies. We analyze  
14 the types of errors made by the algorithm, propose design modifications to decrease the error  
15 rate, and experimentally verify that the new approach achieves statistically significant perfor-  
16 mance improvement. Whereas the baseline algorithm applies the edge-linking uniformly to all  
17 edge pixels to segment a region, the modified algorithm selects high potential edge areas in the  
18 region by analyzing the surface fit pattern and gives priority of edge-linking to those areas.  
19 The contributions of this work are (1) an improved algorithm for segmentation of range  
20 images of both planar and curved surface scenes, and (2) a demonstration of using empirical  
21 performance evaluation to guide algorithm design and modification to achieve better  
22 performance.

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24 *Index terms:* Range image; Segmentation; Performance evaluation

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## 26 1. Introduction

27 Many algorithms have been presented for range image segmentation, and some of  
28 them have undergone experimental comparisons [7,16,9,15], and novel approaches  
29 have been presented to get better performance. Jiang and Kuhni [12] presented a  
30 contour closure algorithm for better performance in edge-based region segmenta-  
31 tion. Cinque [5] used genetic algorithms for optimal setting of range segmentation  
32 algorithm parameters. Bellon and Silva [1] presented an improvement by using an  
33 edge detection technique. Other various techniques [3,4,13] have also been used  
34 for better range segmentation.

35 We present an improved version of a range image segmentation algorithm origi-  
36 nally developed at the University of Bern (UB) [11], which uses an edge-based ap-  
37 proach and is applicable to both planar and curved surface scenes. The UB  
38 algorithm has shown dominance both in performance and speed in an experimental  
39 comparison [16]. The basic strategy of the algorithm is to start from coarse initial  
40 segmentation based on edges of the range image and to proceed to further refine-  
41 ment. Since a typical edge extraction has “gaps” along true edges, most initial re-  
42 gions are under-segmented and need to be split into smaller ones. For each region,  
43 the baseline algorithm hypothesizes a quadratic surface. If the amount of surface  
44 fit error is greater than a predefined threshold, the region is recursively split until  
45 every sub-region satisfies its own surface hypothesis. The splitting is achieved by  
46 linking edge segments inside the region, and the linking is achieved by dilating every  
47 edge pixel of the region.

48 When splitting a region, the baseline algorithm discards all qualitative and quan-  
49 titative information regarding the surface fit errors, and depends only on the binary  
50 edge map. Our improved approach focuses on how to use the surface fit errors to  
51 better split the initial under-segmented regions. We define three prominent patterns  
52 of surface fit error which are frequent in failed surface hypotheses and are useful in  
53 determining proper splitting actions. The experiment was performed by utilizing a  
54 range image segmentation evaluation framework [14] and the improvement of per-  
55 formance was verified by statistical significance tests.

56 The remaining sections of this paper are organized as follows. Section 2 explains  
57 how the baseline range image segmentation algorithm works and how it was trained  
58 for our experiments. Section 3 analyzes the drawback of the baseline algorithm and  
59 introduces new methods to make improvement. Section 4 briefly describes the eval-  
60 uation framework that we employ for comparing the baseline and the improved  
61 algorithms. Section 5 shows the results of both algorithms and compares them,  
62 and Section 6 summarizes our work and introduces topics to be addressed in future  
63 work.

## 64 2. The baseline algorithm

65 The UB algorithm is a fast range segmentation algorithm that is based on edge  
66 detection along scan lines. By dealing with curve segments as the data primitives,

67 it reduces the amount of data, thus obtaining its speed. The algorithm consists of  
68 three steps: edge extraction, edge grouping, and post-processing, each of which will  
69 be explained in the following subsections.

70 *2.1. Edge extraction*

71 The edge extraction method used in the UB algorithm is described in [10]. The  
72 edge detector scans the range image along four directions: horizontal, vertical, and  
73 two diagonals. Each scanned line is a three-dimensional curve. Partitioning each  
74 scan line into quadratic curve segments is performed by using the classical line fitting  
75 algorithm [6]. The end points of these segments are viewed as the potential edge  
76 points. The edge strength of the edge candidates are evaluated by computing the  
77 height difference (jump edges) and the angle difference (crease edges) between two  
78 adjacent curve segments. Each potential edge pixel can be assigned up to four edge  
79 strength values of each type from the four scan lines passing through the pixel (Fig.  
80 1). Among these edge strength values, the maximum values are taken to define the  
81 overall edge strength of each edge type (jump or crease). Finally, the candidate edge  
82 pixel is determined as an edge point if at least one type of edge strength is greater  
83 than the corresponding threshold value.

84 *2.2. Edge grouping*

85 For best segmentation performance, the edge that matches the region boundary  
86 should be a closed contour. But, due to noise in the raw image and other reasons,

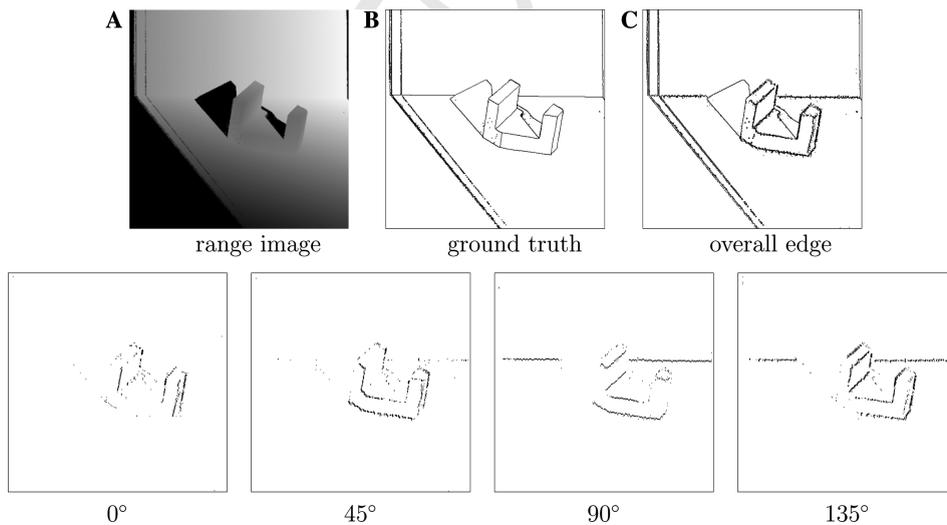


Fig. 1. Edge extractions along four scan directions. In the overall edge map, edges created due to shadow regions are also drawn.

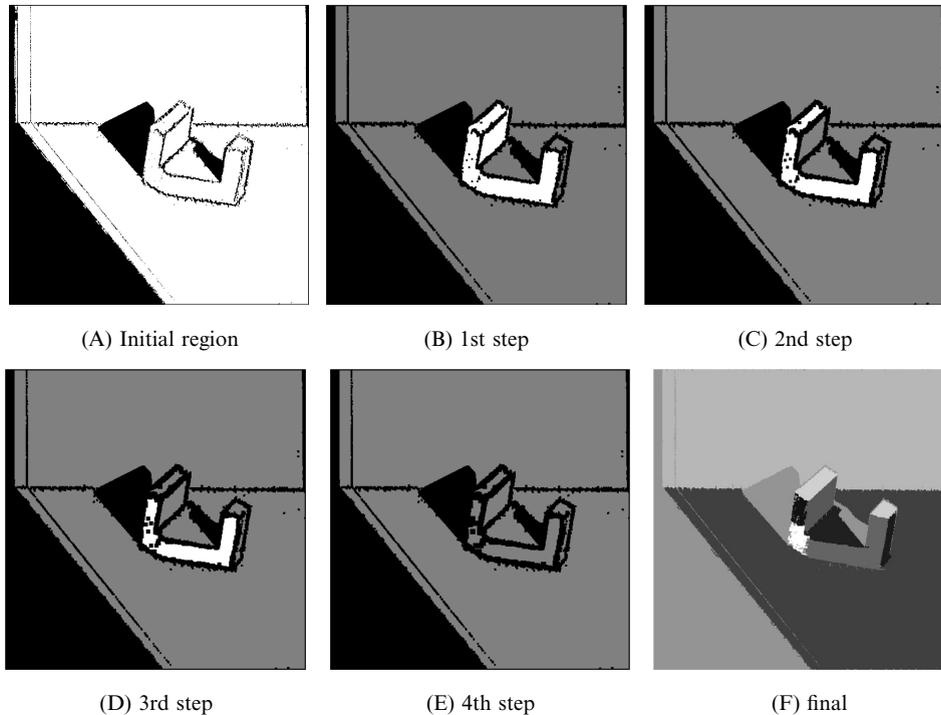


Fig. 2. Region splitting (edge grouping) of the baseline algorithm. (A) The incomplete edge extraction from Fig. 1 causes a large initial under-segmented region (white). (B–D) Each step splits the under-segmented region (white). (E) Splitting is finished. (F) After the post-processing, eroded pixels are recovered to adjacent regions.

87 it is common that the true edges are not in the form of closed contours. After the  
 88 edge detection is completed, the algorithm performs the connected component label-  
 89 ing to generate the initial segmentation. Since the true edges are not fully connected  
 90 at the initial step, the initial segmentation result tends to have a high ratio of under-  
 91 segmented regions.

92 The UB algorithm makes a surface hypothesis on each segmented region and tests  
 93 the hypothesis by calculating the fitting error between the segmented region and the  
 94 hypothesized surface. If the surface fit errors (RMSE and average) of a region are  
 95 less than predefined thresholds ( $T_a^c$  and  $T_r^c$  for curved surface, or  $T_a^p$  and  $T_r^p$  for planar  
 96 surface scenes, discussed later), then the region is accepted as the final segmentation;  
 97 otherwise the algorithm splits the region into subregions. The process is performed  
 98 recursively until all the subregions either pass the surface hypothesis or get smaller  
 99 below the predefined minimum size, which is one of the algorithm parameters.

100 The specific region splitting method used by the baseline algorithm is as follows.  
 101 The algorithm dilates all the edge pixels inside the region—including the region  
 102 boundary—in order to fill the gaps between the true edge segments. After each dila-  
 103 tion step, new surfaces are computed for the newly shaped regions (Fig. 2). Note that

104 surface fit error tends to get smaller as the area gets smaller, especially on curved sur-  
 105 faces. The edge dilation scheme is purely based on the binary edge map of the region.  
 106 Therefore, the scheme requires that the binary edge map is of reasonable quality.  
 107 Otherwise, linking of false edges (in a dense edge map) or excessive dilation of edges  
 108 (in a sparse edge map) will occur.

### 109 2.3. Post-processing

110 After the edge grouping is completed, a post-processing is performed to process  
 111 unlabeled pixels so far. The unlabeled pixels include those that were eroded in the  
 112 process of edge dilation. Such pixels are merged to an adjacent region as long as  
 113 the fit error after the merging is tolerable. Less strict values are set for the surface  
 114 fit error thresholds:  $T_a^p \times T_f^p$  or  $T_a^c \times T_f^c$ . Figs. 2E and F shows before and after  
 115 of the post-processing.

### 116 2.4. Training

117 The UB algorithm has a total of 10 parameters as shown in Table 1. Parameters  
 118  $T_g$ ,  $T_j$ , and  $T_c$  are used in the edge extraction step, and parameters  $T_r^p$ ,  $T_r^c$ ,  $T_a^p$ ,  $T_a^c$ , and  
 119  $T_s$  are related to surface approximation, thus used in the edge grouping step. The  
 120 remaining parameters  $T_f^p$  and  $T_f^c$  are used in the post-processing step and specify  
 121 how the parameters  $T_a^p$  and  $T_a^c$ , respectively, can be relaxed in merging the unlabeled  
 122 pixels.

123 As it is impractical to train the algorithm over all the parameters because of the  
 124 computational load of training, we selected the most four significant parameters in  
 125 training: a set of ( $T_g$ ,  $T_j$ ,  $T_s$ , and  $T_c$ ) for the ABW images and another set of ( $T_g$ ,  
 126  $T_j$ ,  $T_c$ , and  $T_r^c$ ) for the Cyberware images. A total of 69,400 executions of the baseline  
 127 algorithm (65 CPU hours on a Sun Fire 880) were performed in training the algo-  
 128 rithm over the 10 ABW training sets and 78,300 executions (48 h on a Sun Fire  
 129 880) in training the algorithm over the 10 Cyberware training sets.

Table 1  
Parameters of university of bern segmenter

Name	Description
$T_g$	Max. distance between scan line and quadratic curve fit
$T_r^p$	Planar surface approximation RMS error: $\sqrt{\sum \text{error}^2 / \text{RegionSize}}$
$T_r^c$	Curved surface approximation RMS error: $\sqrt{\sum \text{error}^2 / \text{RegionSize}}$
$T_a^p$	Planar surface approximation average error: $\sum  \text{error}  / \text{RegionSize}$
$T_a^c$	Curved surface approximation average error: $\sum  \text{error}  / \text{RegionSize}$
$T_j$	Threshold of jump edge strength
$T_c$	Threshold of crease edge strength
$T_s$	Minimum number of pixels of a legitimate region
$T_f^p$	Tolerance of $T_a^p$ in the post processing
$T_f^c$	Tolerance of $T_a^c$ in the post processing

### 130 3. Improvement

131 Getting correctly closed edges is important for the UB algorithm to achieve a suc-  
132 cessful segmentation. The algorithm assumes that a moderately well extracted edge  
133 map is given initially and refines the initial segmentation by subsequent edge linking  
134 procedures. One thing to note here is that in the UB algorithm the surface hypothesis  
135 is performed for every region, but the qualitative result of the hypothesis is not used  
136 at all in handling the failed surface hypothesis. That is, the surface fit is used only to  
137 pick up the under-segmented regions, and refining those under-segmentations is per-  
138 formed without knowing *how* the surface fits the region.

139 For better edge linking, a new adaptive contour closing algorithm that uses a  
140 direction-guided edge grouping approach has recently been presented by Jiang [8].  
141 It also assumes that no other information is given except for the binary edge map  
142 of the scene. In other words, the approach is considered as a stand-alone edge group-  
143 ing algorithm rather than a component of a segmentation algorithm. As mentioned  
144 in the paper, its performance is highly dependent on the edge shapes and the result of  
145 contour closing is not successful in some cases. Besl and Jain [2] designed an algo-  
146 rithm that starts from coarse segmentation initially created by using surface curva-  
147 ture sign labeling and refines it by an iterative region-growing that is based on the  
148 surface fitting errors.

149 In this paper we present a new approach to improve the segmentation perfor-  
150 mance of the UB algorithm by using the surface fit error information in determining  
151 edge linking. The new approach is focused on the second step of the baseline algo-  
152 rithm, that is, *edge grouping*; other components of the original algorithm, such as  
153 edge extraction and post-processing, remain untouched.

#### 154 3.1. Surface fit error map

155 The main potential drawback of the baseline algorithm is the unnecessary ero-  
156 sion of non-edge regions in the process of edge linking. Whenever the surface  
157 hypothesis fails, which means that a region turns out to be under-segmented,  
158 the baseline algorithm tries to split the region by linking the gaps between edge  
159 segments. The linking is performed by dilating all the edge pixels of the region  
160 including the boundary. In many cases, when the edge segments are disconnected  
161 only by several pixels and noise level is low, the algorithm produces very reliable  
162 and fast splitting results. In many other cases, however, this simple scheme causes  
163 several problems. When the edge map is too dense, many false edge points tend  
164 to be linked together, creating unwanted false edge contours. This results in over-  
165 segmentation, or more severely when the partitions are too small, missed regions  
166 in the final output (Fig. 3). On the other hand, when the edge map is too  
167 sparse—few edge pixels exist except for the boundary of the region—linking  
168 the edge segments takes repeated steps of edge dilation, shrinking the region as  
169 a result of excessive inward erosion from boundary edges, which sometimes is  
170 not able to be recovered even by the post-processing of the baseline algorithm  
171 (Fig. 4). In both cases, it is very likely to miss part of the region. Setting proper

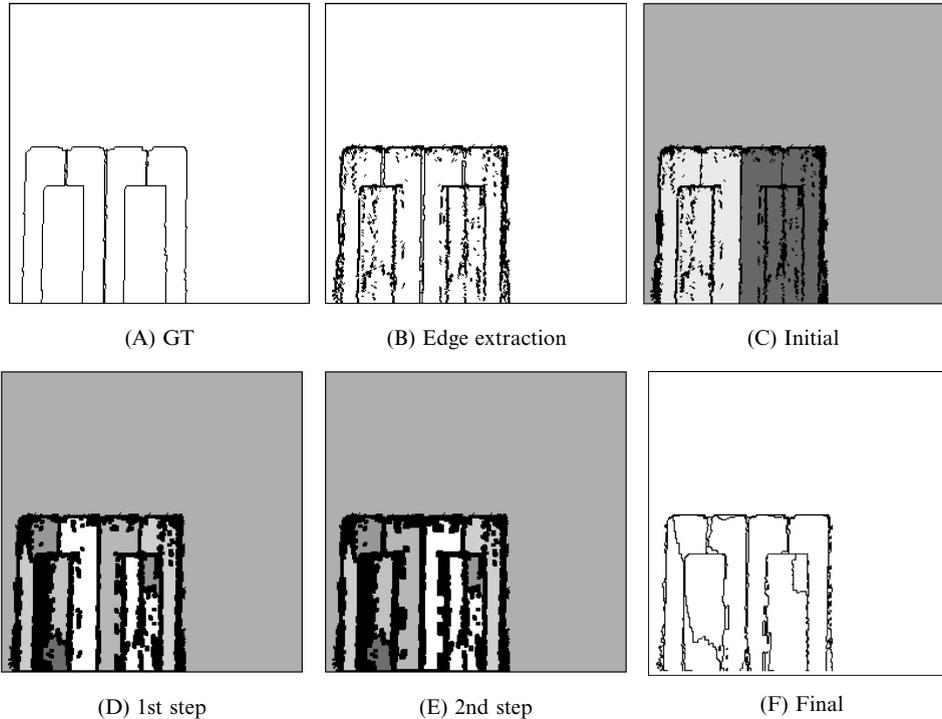


Fig. 3. Over-segmentation example of the baseline algorithm. Due to the dense edge map, noisy edge pixels are linked together, creating false contours. (C-E) Different intensities imply different regions.

172 values for the two edge-related thresholds ( $T_j$  and  $T_c$ ) may help prevent these  
173 cases, but the threshold values usually have to be set over a number of training  
174 images of various scene quality.

175 The main idea of our improvement is to dilate edge pixels of an under-seg-  
176 mented region selectively, and the selection is based on how the hypothesized  
177 surface patch fits the region. We can categorize several patterns of surface  
178 hypothesis failure, for each of which we prescribe different action. Whenever  
179 the surface fit is made to a region, we build a surface fit error map of the region  
180 that represents the surface fit error amount of each pixel. For simpler represen-  
181 tation, we assign grey-level value (0-255) to the fit error. That is, we assign *black*  
182 (=0) if  $f(x,y) - z(x,y) \geq 2 * avgerr$ , *white* (=255) if  $z(x,y) - f(x,y) \geq 2 * avgerr$ ,  
183 where  $f(x,y)$  is the surface point,  $z(x,y)$  is the region point, and  $avgerr$  is the  
184 average surface fit error value of the region. Other fit error values in between  
185 are scaled into *grey*, so that grey-level 127 means zero fit error. The extreme  
186 fit error areas, *black* and *white*, will play a major role in the following subsec-  
187 tions. Given an under-segmented region, instead of blindly dilating edge pixels,  
188 our new approach takes following three levels of action depending on the surface  
189 fit patterns:

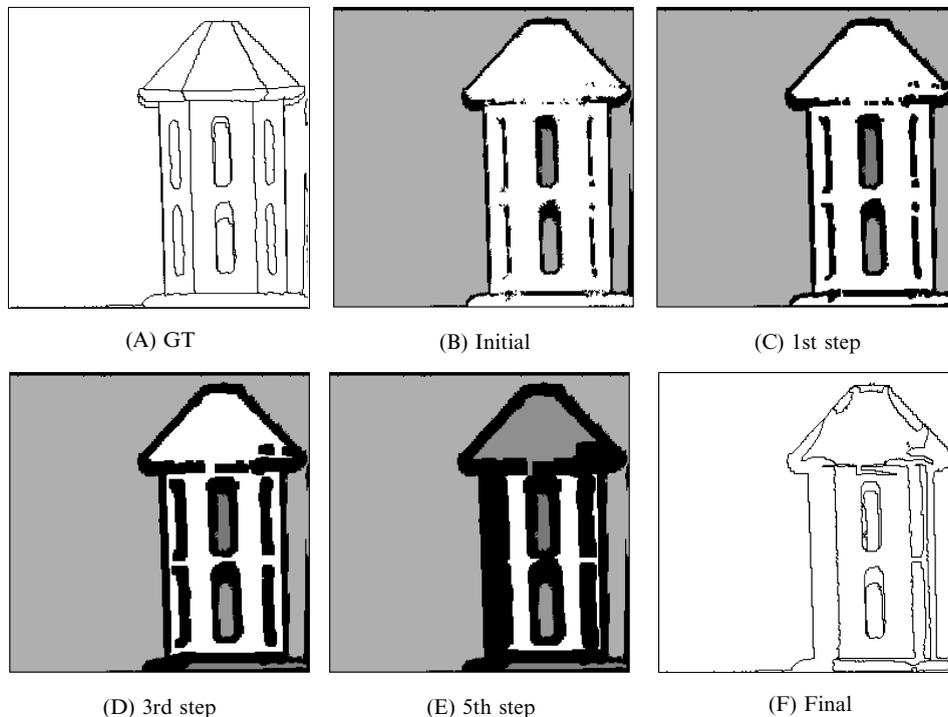


Fig. 4. Under-segmentation and missed region example of the baseline algorithm. Due to the sparse edge map, edge grouping is performed repeatedly, resulting in severe erosion of the initial region. Splitting is not successful and several regions are missed.

- 190 • *Direct split*. Whenever two opposite extreme areas (black and white) are adjoining,  
 191 ing, a border line is created along the zero-crossing line regardless of the existence  
 192 of edge points.
- 193 • *Forced split*. Whenever an extreme area itself (black or white) splits the region,  
 194 forced erosion is performed on that area until the split is accomplished.
- 195 • *Selective linking*. If the region has not been split at the two levels above, edge dila-  
 196 tion is performed only on the areas with high fit error.

197

### 198 3.2. *Direct split*

199 It is not guaranteed that the very strong candidate of an edge is fully connected in  
 200 the edge map. There are several possible reasons: too strict edge threshold, noisy in-  
 201 puts, or real disconnections of edge at some level. The surface fit error values around  
 202 these disconnected high jump edges have patterns in which an area of highly negative  
 203 (black) fit error is adjacent to an area of highly positive (white) fit error (Fig. 5C).  
 204 Thus, it is intuitive to separate these areas no matter how many edge points already  
 205 exist in the area. For each under-segmented region, all adjoining extreme areas with

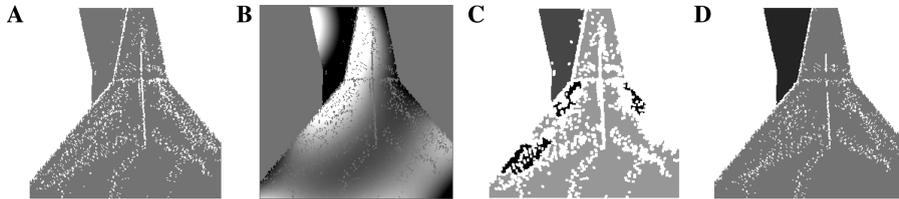


Fig. 5. Comparison of blind edge linking and direct split. (A) An under-segmented region. Due to incomplete edge detection, the upside-down funnel and the small triangular planar background are connected. (B) Surface fit error map of the region. Two extreme areas with opposite signs are adjoining in the upper part of the region. (C) Result of blind edge linking by the baseline algorithm. The funnel and background are detached, but the funnel is over-segmented at this early step. (D) Result of direct split. The funnel and the background are detached without any side-effects.

206 opposite signs (*black* and *white*) should be separated. As shown in Fig. 5, the split is  
 207 done successfully and other irrelevant edge points remain intact, saving non-edge  
 208 pixels from erosion.

### 209 3.3. Forced split

210 In general, crease edges are harder to extract than jump edges. The surface fit er-  
 211 ror values around the true crease edges also have patterns in which an area of ex-  
 212 treme fit error (negative or positive) traverses the region. To determine the true  
 213 crease edge region, we test every extreme area to see whether it really splits the re-  
 214 gion. After deleting the area temporarily from the region, we check if the deletion  
 215 splits the region by performing connected component labeling upon the region. If  
 216 the labeling shows two or more regions, we register it as a strong candidate for crease  
 217 edge. Then the dilation of edge points is performed only in this area until it gets a  
 218 split of the region. In the worst situation of the edge detection, we are given no edge  
 219 point at all in this extreme area. Then the forced split will erode the region inwards  
 220 from the boundary until the region is split. Fig. 6 shows the results both from the  
 221 baseline and the improved algorithm.

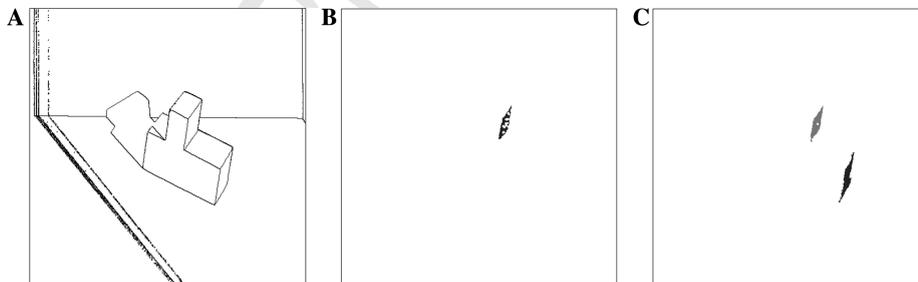


Fig. 6. Comparison of blind edge linking and forced split at the intermediate step (before post-processing). Only the regions of interest are shown. (A) Ground truth. (B) The baseline result. A small region at the rightmost side of the block is missing as result of excessive erosion of the region. Another region at the other right face of the block is eroded excessively. (C) The forced split result. The forced split has been applied. No region is missing and no region is eroded seriously.

### 222 3.4. Selective linking of edges

223 If the surface fit error map does not show any of the special patterns described  
224 above, or splitting the region is not completed even after applying the actions above,  
225 a selective dilation of edges is performed. This is similar to the original edge dilation  
226 scheme of the baseline, except that not all the edge pixels inside the region are se-  
227 lected for dilation. A typical surface fit error map of an under-segmented region  
228 has various areas of different fit errors. It is intuitive that edge points around the area  
229 with high surface fit error, regardless of the sign, are more likely—although not al-  
230 ways true—to be near the true edges than ones with low surface fit error.

231 We divide the surface fitting errors into three groups, i.e., high (greater than two  
232 times of the average), medium (greater than the average), and low (less than the aver-  
233 age), according to the relative value to the average fit error of the region. At the first step  
234 of dilation, edge points with high surface fitting error are dilated. If it succeeds in link-  
235 ing some edges and in splitting the region, then the dilation stops. Otherwise, dilating is  
236 performed on the edge pixels with medium surface fitting error. If it succeeds, then the  
237 same action will be taken. Otherwise, all the remaining edge pixels are dilated and per-  
238 forming this final step will have the same effect as the baseline algorithm. At worst, the  
239 algorithm with the new dilation approach does the same action as the baseline.

240 Both the baseline and the improved algorithm assume that a sufficient amount of  
241 edge pixels are provided along true edge contours. This assumption is more crucial to  
242 the baseline algorithm. Moreover, the baseline algorithm also assumes that false edge  
243 pixels are not dense in order to avoid over-segmentation. The second requirement is  
244 not crucial to the improved approach, therefore we can lower the edge thresholds  
245 without worrying about over-segmentation.

### 246 3.5. Training

247 We apply a different order of significance of the parameters to the baseline and the  
248 improved algorithms because they work differently. For example, for the ABW im-  
249 age set, the improved algorithm shows no performance improvement between 1-pa-  
250 rameter and 2-parameter tuning when  $T_j$  is set for the second significant parameter as  
251 we did for the baseline algorithm. A new order of parameter significance was deter-  
252 mined in a trial-and-error manner, as was done in the baseline algorithm.

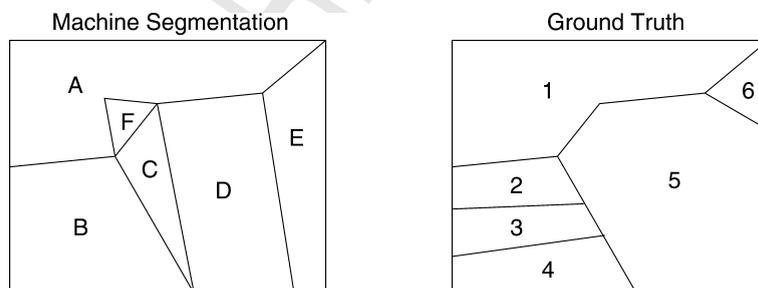
253 We selected a set of parameters ( $T_g$ ,  $T_r$ ,  $T_j$ , and  $T_a^p$ ) for the training on the ABW  
254 images, and another set of parameters ( $T_g$ ,  $T_c$ ,  $T_a^c$ , and  $T_j$ ) for the training on the  
255 Cyberware images. A total of 76,446 executions of the improved algorithm (156 h  
256 on a Sun Fire 880) were performed in training the algorithm over the 10 ABW train-  
257 ing sets and 76,428 executions (73 h on a Sun Fire 880) in training the algorithm over  
258 the 10 Cyberware training sets. The increased training time of the improved algo-  
259 rithm was expected because of several reasons. First, whenever a failed surface  
260 hypothesis is found, the algorithm tries to find surface fit patterns on which the direct  
261 split and/or the forced split operations are applicable. The baseline algorithm does  
262 not have this stage. Second, the pixels to be eroded by the selective erosion are a sub-  
263 set of the pixels to be eroded by the baseline algorithm. Therefore, the baseline algo-

264 rithm finishes the region split much faster than the improved algorithm does, regard-  
 265 less of the segmentation performances.

#### 266 4. Evaluation framework

267 The definition of the performance metrics for the segmentation is the same as used  
 268 by Hoover et al. [7]. A machine segmentation (MS) of an image compares to the  
 269 ground truth (GT) specification for that image to count instances of correct segmen-  
 270 tation, under-segmentation, over-segmentation, missed regions, and noise regions.  
 271 The definitions of these metrics are based on the degree of mutual overlap required  
 272 between a region in the MS and a corresponding region in the GT. An instance of  
 273 “correct segmentation” is recorded if and only if an MS region and its corresponding  
 274 GT region have greater than the required threshold of mutual overlap. Multiple MS  
 275 regions that correspond to one GT region constitute an instance of over-segmenta-  
 276 tion. One MS region that corresponds to several GT regions constitutes an instance  
 277 of under-segmentation. A GT region that has no corresponding MS region consti-  
 278 tutes an instance of a missed region. A MS region that has no corresponding GT re-  
 279 gion constitutes an instance of a noise region. Fig. 7 illustrates these definitions of the  
 280 performance metrics. For the statistical test for significance, we use the number of  
 281 instances of correct segmentation.

282 The performance evaluation framework [14] that we employ uses separate sets of  
 283 images for train, validation, and test. The training step searches for the “best”  
 284 parameter settings. The validation step decides how many of the segmenter’s param-  
 285 eters should have their value learned through training versus left at the default value.  
 286 The test step determines performance curves to be used in comparing different seg-  
 287 menters. Because the selected parameter settings may vary based on the particular  
 288 set of training images, we create multiple different training sets by random sampling  
 289 from a larger pool of training images. This applies to the validation and test sets, too.



MS A corresponds to GT 1 as an instance of correct segmentation.  
 GT 5 corresponds to MS C, D, and E as an instance of over-segmentation.  
 MS B corresponds to GT 2, 3, and 4 as an instance of under-segmentation.  
 GT 6 is an instance of a missed region.  
 MS F is an instance of a noise region.

Fig. 7. Illustration of definitions for scoring region segmentation results.

290 In general, typical algorithms have a number of parameters that control their  
291 operation and the default values for the parameters. This introduces the question  
292 of how many of the available parameters should be trained. After training on a given  
293 number of parameters, the parameter values for each training set are run on each  
294 validation set. If there are  $T_{tr}$  training sets and  $V$  validation sets, then  $T_{tr} \times V$  perfor-  
295 mance curves are produced. If the improvement of the validation in going from  
296  $N - 1$  to  $N$  parameters is statistically significant, then training is repeated using  
297  $N + 1$  parameters. If there was no improvement in going to  $N$  parameters, then  
298 the  $(N - 1)$ -parameter training result is kept.

299 The final trained parameter values from each training set are run on each test set,  
300 resulting in  $T_{tr} \times T_{te}$  performance curves. The areas under these curves are used as  
301 the basis of a test for statistical significance of an observed difference in performance  
302 between segmenters. The performance is compared quantitatively and statistically by  
303 using the paired differences in the areas under the performance curves.

304 Assume that we are comparing a “challenger” algorithm to a “baseline” algo-  
305 rithm. The test statistic will be the difference between the areas under the perfor-  
306 mance curves. The sign test can be used to check for statistical significance  
307 without requiring the assumption that the differences follow a normal distribution.  
308 The null hypothesis is that there is no true difference in average performance between  
309 the algorithms. Under the null hypothesis, each algorithm has a 0.5 probability of  
310 generating the larger area under the performance curve on any given trial. The num-  
311 ber of trials for which one algorithm generates a larger area than the other should  
312 follow a binomial distribution. Our framework implementation automatically re-  
313 ports the results of a sign test.

## 314 5. Experimental results

315 In Sections 2 and 3, both the baseline and the improved algorithm are trained  
316 using validation steps and 10 sets of trained parameters were applied to each of  
317 the 10 test sets. For each algorithm over each range data type, we got 100 (10 train  
318 sets  $\times$  10 test sets) performances of five different metrics (correct classification, under-  
319 segmentation, over-segmentation, missed region, and noise region) in the form of  
320 values of area under the performance curve. A paired sign test was performed on  
321 these 100 pairs of quantitative values to determine statistical significance. As is  
322 shown in subsequent subsections below, the improvement obtained by using the  
323 new algorithm is small but statistically significant (at the  $\alpha = 0.05$  level) for both data  
324 sets.

### 325 5.1. Results on planar-surface image sets

326 The paired comparison of 100 performance values (correct classification) between  
327 two algorithms is shown in Fig. 8. The new algorithm produced slightly better per-  
328 formance than the baseline in 67 out of 100 instances. The improvement in correct  
329 classification mostly came from reduction of missed regions (Fig. 9), which, in the

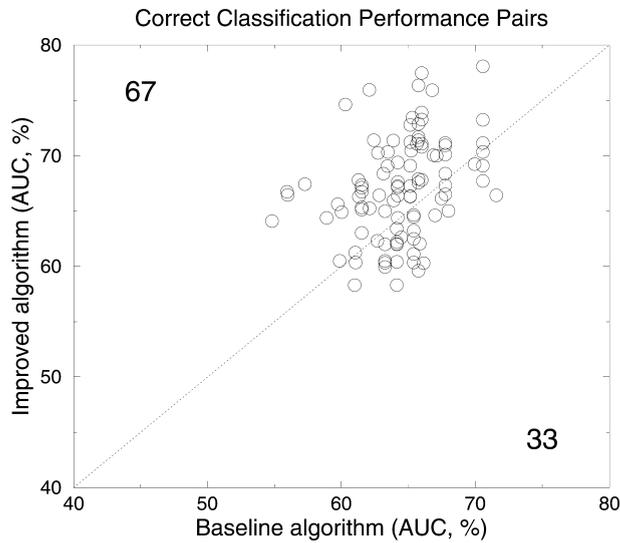


Fig. 8. Comparison of performance between the baseline and the improved algorithm on ABW test sets.

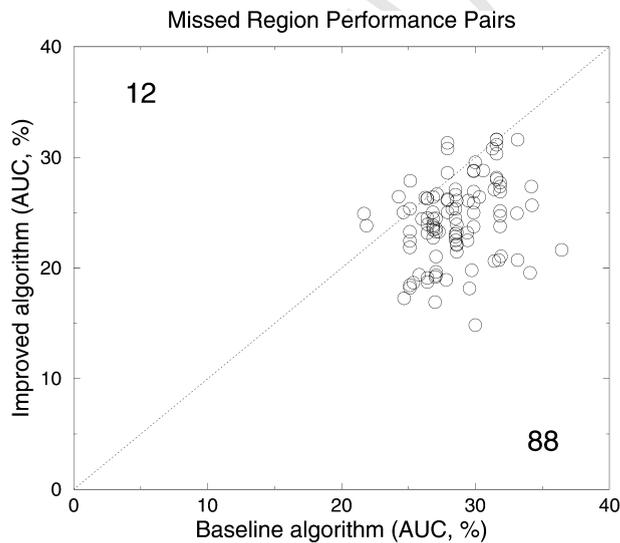


Fig. 9. Comparison of incorrect segmentations (missed regions) between the baseline and the improved algorithm on ABW test sets.

330 baseline algorithm, occurred mainly due to the excessive erosion of small regions.  
 331 There was a small decrease in over-segmentations and a small increase in noise re-  
 332 gions that in effect cancel each other out, and therefore did not influence the overall  
 333 performance. The new algorithm produced more under-segmentations in 96 out of  
 334 100 cases, but the amounts were so small that it did not make difference.

335 Fig. 10 shows machine segmentation samples from both algorithms. Note that  
 336 setting different overlap thresholds produces different interpretations of the same  
 337 segmentation result. For example, an instance of correct classification at a lower  
 338 threshold switches to an error metric at a higher threshold. And an instance of  
 339 over-segmentation at a lower overlap threshold (e.g., 51%) switches to an instance  
 340 of missed region *plus* multiple instances of noise region at a higher overlap threshold  
 341 (e.g., 95%). In the figure, we counted the number of instances of each performance  
 342 metric at the fixed overlap threshold of 85%.

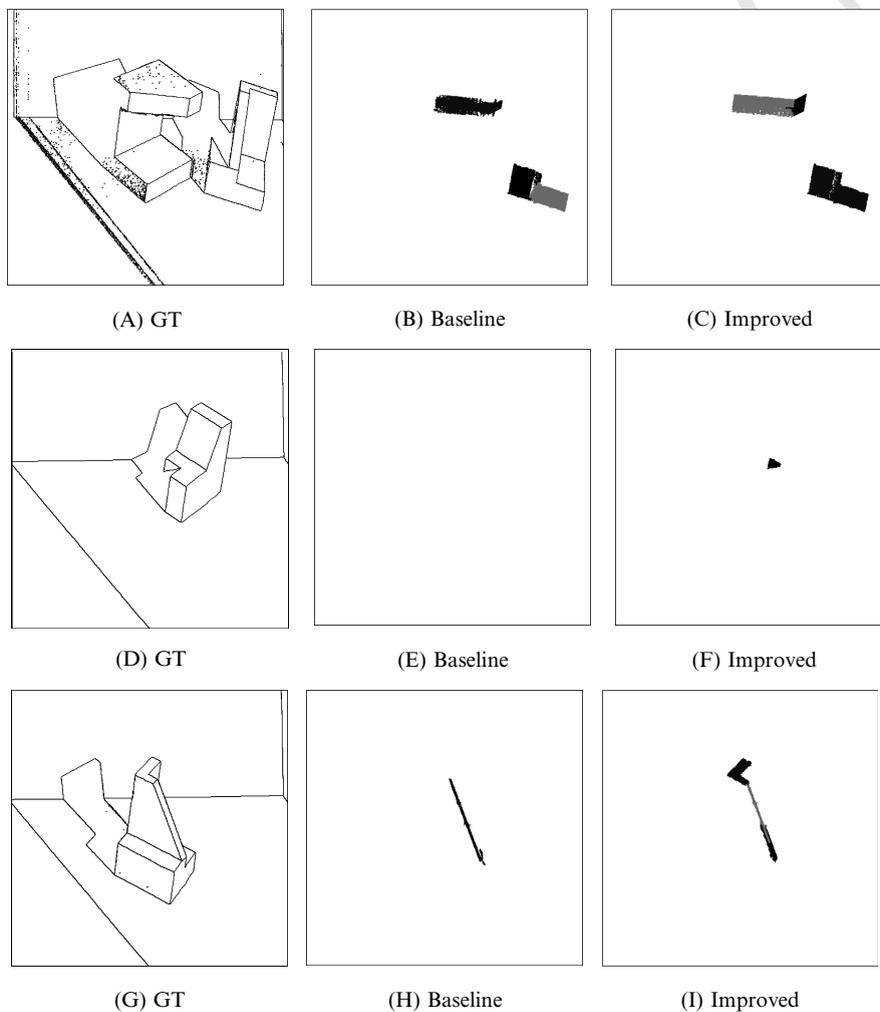


Fig. 10. Segmentation comparison on ABW images at 85% overlap threshold. (A–C) Test image “abw.18.” Two over-segmentations, two missed regions, and one noise region are recovered. (D–F) Test image “abw.28.” One missed region is recovered. (G–I) Test image “abw.25.” One missed region is recovered, but another missed region and additional two noise regions are created.

343 We can conclude that the new algorithm applied to the planar surface scenes im-  
344 proved the correct segmentation performance by relieving the excessive erosion  
345 problem of the baseline algorithm. The ABW data set contains many small planar  
346 regions which can be easily rejected from region acceptance due to small size after  
347 excessive erosion of the baseline algorithm. As all of the surfaces are planar, the  
348 new algorithm benefits from the forced split and selective erosion approaches be-  
349 cause the boundaries of adjoining planar surfaces are more likely having extreme  
350 fit errors.

### 351 5.2. Results on curved-surface image sets

352 The paired comparison of 100 performance values between two algorithms is dis-  
353 played in Fig. 11. The new algorithm produced better performance than the baseline  
354 in a statistically significant fraction of the results (72 out of 100 in the paired sign  
355 test).

356 By analyzing the performance of the baseline algorithm, we knew that its correct  
357 classification performance was largely influenced by its level of under-segmentation;  
358 on a curved surface, the algorithm tends to satisfy the fit error threshold by eroding  
359 the outer area of the under-segmented region. On the contrary, the improved algo-  
360 rithm is more likely to erode the inner area, which has high fit error. Thus, the new  
361 algorithm generally reduced the level of under-segmentation but did not have major  
362 effects on other performance metrics. An increase in the level of noise regions de-  
363 graded performance on some images but this was often outweighed by the decrease  
364 in under-segmentation. There is no remaining predominant error tendency in the  
365 new algorithm. Fig. 12 shows machine segmentation samples from both algorithms.

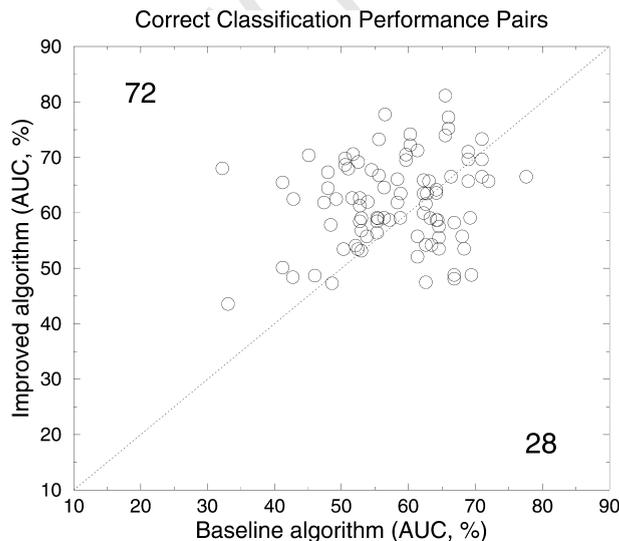


Fig. 11. Comparison of performance between the baseline and the improved algorithm on Cyberware test sets.

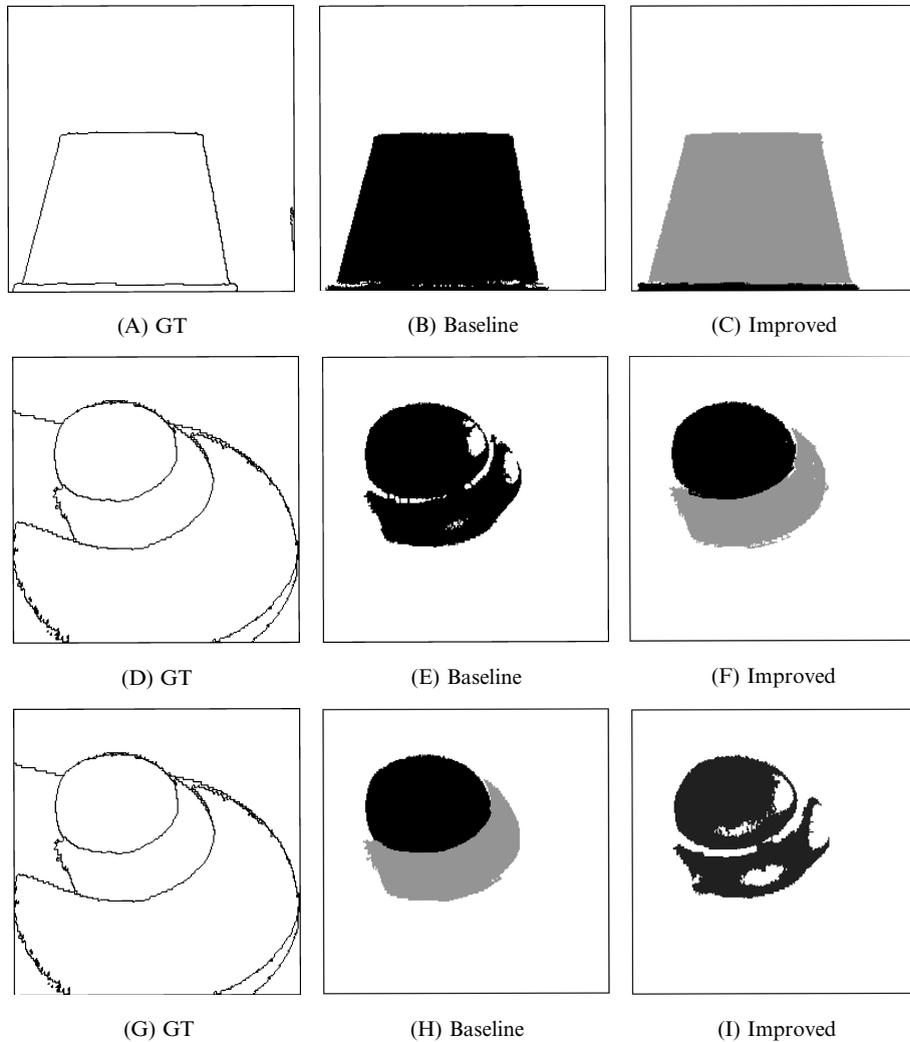


Fig. 12. Segmentation comparison on Cyberware images at 85% overlap threshold. (A–C) Test image “cone1.” One under-segmentation is recovered. (D–F) Test image “snowman.” Two missed regions and one noise region are recovered. (G–I) Test image “snowman” (with another parameter setting). Two missed regions and one noise region are created.

## 366 6. Summary and conclusions

367 An improvement in range image segmentation has been achieved by applying a  
368 new approach to handling failed surface hypothesis. Instead of linking edges blindly  
369 the new algorithm analyzes the surface fit patterns of the failed surface hypothesis.  
370 The improvement was verified by using a range image segmentation evaluation  
371 framework with sets of planar and curved surface scene images.

372 With image sets of uniform complexity, the produced edge maps may be of rea-  
373 sonable quality, so the baseline algorithm will perform well and be faster than the  
374 new approach. However, images with a wide variety in sizes of objects and/or in  
375 scene complexity will let the edge images be of low quality, so the baseline algorithm  
376 that only looks at the edge map would have difficulties in achieving a successful seg-  
377 mentation. By applying our novel approach, we were able to design an improved  
378 algorithm that is less sensitive to the edge extraction results.

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