

2006

PHYSICS 10310 - Exam I

①

MC1

$$[F_{\text{air}}] = N = \text{kg m/s}^2$$

$$[A] = \text{m}^2$$

$$[v] = \text{m/s}$$

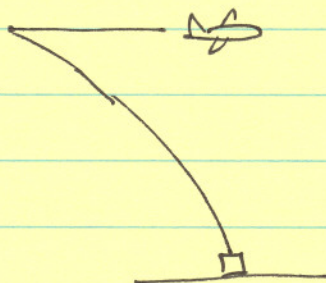
$$[C] = \frac{[F_{\text{air}}]}{[A][v^2]} = \frac{\text{kg m/s}^2}{\text{m}^2 \cdot \text{m}^2/\text{s}^2} = \text{kg/m}^3.$$

⑤

MC2 Car has non-zero initial velocity and constant positive acceleration

③

MC3



Horizontal velocity of plane & crate remains the same, so crate fall vertically down wrt plane.

⑧

MC4 Apparent weight $w = m(g+ a)$. In this case $a = -g$ so we get $w = 0$.

④

MC5 Only two forces present: (i) gravity and (ii) normal force.

③

(II)

a) Free fall acceleration: $v_y^2 - v_{0y}^2 = 2a(y - y_0)$

$$y - y_0 = \frac{-v_{0y}^2}{2(-g)} = \frac{(250 \text{ m/s} \cdot \sin 65^\circ)^2}{2 \cdot 9.81 \text{ m/s}^2} = \underline{\underline{2617 \text{ m}}}$$

b) "up" & "down" times are equal.

$$v_y - v_{0y} = at_{\text{up}} \Rightarrow -v_{0y} = -gt_{\text{up}} \Rightarrow t_{\text{up}} = \frac{v_{0y}}{g}$$

$$t = t_{\text{up}} + t_{\text{down}} = \frac{2v_{0y}}{g} = \frac{2 \cdot 250 \text{ m/s} \cdot \sin 65^\circ}{9.81 \text{ m/s}^2} = \underline{\underline{46.2 \text{ s}}}$$

c) Range:

$$R = \frac{v_0^2}{g} \sin 2\theta = \frac{(250 \text{ m/s})^2}{9.81 \text{ m/s}^2} \cdot \sin 130^\circ = \underline{\underline{488 \text{ m}}}$$

(III)

NI x 3:

$$T_1 - m_1 g = m_1 a$$

up positive

$$T_3 - T_1 = m_2 a$$

right positive

$$m_3 g - T_3 = m_3 a$$

down positive.

$$a) \quad m_3(g - a) - m_1(g + a) = m_2 a \Rightarrow (m_1 + m_2 + m_3)a = (m_3 - m_1)g$$

↓

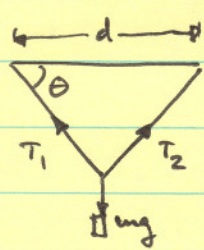
$$a = \frac{m_3 - m_1}{m_1 + m_2 + m_3} = \frac{2.5 - 1.5}{1.5 + 4.0 + 2.5} g = \frac{1}{8} g = \underline{\underline{1.23 \text{ m/s}^2}}$$

$$b) \quad T_1 = m_1(g + a) = 1.5 \text{ kg} (9.81 \text{ m/s}^2 + 1.23 \text{ m/s}^2) = \underline{\underline{16.6 \text{ N}}} \quad \frac{9}{8} m_1 g !$$

$$T_2 = m_2(g - a) = 2.5 \text{ kg} (9.81 \text{ m/s}^2 - 1.23 \text{ m/s}^2) = \underline{\underline{21.5 \text{ N}}} \quad \frac{7}{8} m_3 g.$$

IV

a)



$$\frac{d}{2} \cos \theta = \frac{d}{2}$$

⇓

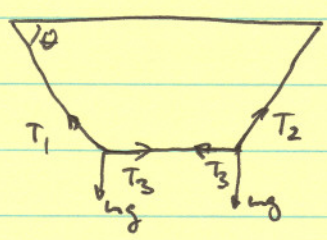
$$\theta = \text{Arccos } \frac{d}{e} = \text{Arccos } \frac{1}{1.2} = \underline{\underline{33.6^\circ}}$$

b)

NI @ knot: $2T_1 \sin \theta = mg$ ($T_1 = T_2$ by symmetry)

$$T_1 = \frac{mg}{2 \sin \theta} = \frac{0.5 \text{ kg} \cdot 9.8 \text{ m/s}^2}{2 \cdot \sin 33.6^\circ} = \underline{\underline{4.44 \text{ N}}}$$

c)



Angle θ : $2 \cdot 0.4 \text{ m} \cos \theta + 0.4 \text{ m} = 1 \text{ m}$

$$\theta = \text{Arccos } \left(\frac{1 - 0.4}{2 \cdot 0.4} \right) = 41.4^\circ$$

NI @ left mass:

x: $T_1 \cos \theta = T_3$

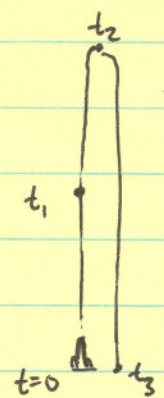
y: $T_1 \sin \theta = mg$

⇓

$$T_1 = \frac{mg}{\sin \theta} = \frac{0.25 \text{ kg} \cdot 9.8 \text{ m/s}^2}{\sin 41.4^\circ} = \underline{\underline{3.71 \text{ N}}}$$

$$T_3 = 3.71 \text{ N} \cdot \cos 41.4^\circ = \underline{\underline{2.78 \text{ N}}}$$

(V)



Part 1: $t=0 - t \leq t_1$ dg motor on.

$$y_1 = \frac{1}{2} a t_1^2$$

$$v_1 = a t_1$$

$$a = 20 \text{ m/s}^2$$

$$t_1 = 20 \text{ s.}$$

Part 2: moving towards highest point w/engine off.
free fall acceleration!

$$\begin{cases} (y_2 - y_1) = v_1 (t_2 - t_1) - \frac{1}{2} g (t_2 - t_1)^2 \\ v_2 = v_1 - g (t_2 - t_1) \Rightarrow t_2 - t_1 = \frac{v_1}{g} = t_1 \frac{a}{g} \quad (v_2 = 0). \end{cases}$$

$$y_2 - y_1 = a t_1 \frac{a t_1}{g} - \frac{1}{2} g \left(t_1 \frac{a}{g} \right)^2 = \frac{1}{2} a^2 t_1^2 / g$$

a) Total height:

$$y_2 = y_1 + (y_2 - y_1) = \frac{1}{2} a t_1^2 + \frac{1}{2} a^2 t_1^2 / g = \frac{1}{2} a t_1^2 \left(1 + \frac{a}{g} \right)$$

$$= \frac{1}{2} \cdot 20 \text{ m/s}^2 \cdot (20 \text{ s})^2 \left(1 + \frac{20 \text{ m/s}^2}{9.81 \text{ m/s}^2} \right) = \underline{\underline{12.2 \text{ km}}}$$

b) $t_2 = t_1 \left(1 + \frac{a}{g} \right)$

Free fall from height y_2 : $y_2 = \frac{1}{2} g (t_3 - t_2)^2 = \frac{1}{2} a t_1^2 \left(1 + \frac{a}{g} \right)$

$$t_3 - t_2 = t_1 \sqrt{\frac{a}{g} \left(1 + \frac{a}{g} \right)}$$

$$\text{Total time: } t_3 = t_2 + (t_3 - t_2) = t_1 \left[\left(1 + \frac{a}{g} \right) + \sqrt{\frac{a}{g} \left(1 + \frac{a}{g} \right)} \right]$$

$$= \underline{\underline{111 \text{ s}}}$$

$\frac{a}{g} = 2.04$

(v) cont'd

$$c) \quad v_3 = g(t_3 - t_2) = g t_1 \sqrt{\frac{a}{g} \left(1 + \frac{a}{g}\right)} = \cancel{dg(a+g)}$$

$$= t_1 \sqrt{a(a+g)} = \underline{\underline{488 \text{ m/s}}}$$