14. (a) Calculate the following sums

$$1 = 1$$
 $1 + 3 =$
 $1 + 3 + 5 =$
 $1 + 3 + 5 + 7 =$
 $1 + 3 + 5 + 7 + 9 =$
 $1 + 3 + 5 + 7 + 9 + 11 =$

(b) Examine the results of part (a) to see if you can find a pattern which would enable you to find the sum

$$1 + 3 + 5 + 7 + 9 + 11 + 13 =$$

without actually adding these numbers.

- (c) Express the sum in each case of part (a) in terms of how many odd numbers are to be added.
- (d) Give a conjecture as to the sum of the first n odd numbers

$$1 + 3 + 5 + ... + (2n - 1) =$$