- In a 10-team soccer conference, each team plays every other team 1. exactly once. How many games must be played?
- a. 45
- b. 90
- c. 99 d. 100
- e. 10!

- 2. A class of 100 students is split into 3 groups: group 1 is to have 20 students, group 2 is to have 30 students and group 3 is to have 50 students. How many ways are there to do this?

- a. $\binom{100}{20}\binom{80}{30}$ b. $\binom{100}{20}\binom{100}{30}\binom{100}{50}$ c. $\binom{100}{20}+\binom{100}{30}+\binom{100}{50}$
- d. 20 · 30 · 50
- e. 20 + 30 + 50

- At Smith College, 260 mathematics majors are surveyed about 3 courses: 3. finite math (F), Calculus (C), and Algebra (A). It is found that 52 students take all 3 courses and that 100 take A, 200 take C, 165 take F, 57 take A and C, 125 take C and F, 82 take A and F. How many students take none of the 3 courses?
- a. 5
- b. 7
- c. 10
- d. 13
- e. 25

- A fast food place offers a pancake combo, consisting of a basic pancake 4. with a choice of up to 3 extras from a list of 8. How many different pancake combos are possible?
- a. 56
- b. 93 c. 100
- d. 336
- e. 256
- 5. How many 5-digit numbers can be made with the digits 1 through 8 if no digit is repeated?
- a. 8⁵
- b. $\frac{8!}{5! \ 3!}$ c. $\frac{8!}{5!}$ d. $\frac{8!}{3!}$ e. 2^5

- 6. An urn contains 8 green balls and 6 red balls. Five balls are selected at random. Find the probability that exactly 3 of the balls are red.
- a. $\frac{\binom{6}{3}}{\binom{14}{5}}$

b. $1 - \frac{\binom{6}{3}}{\binom{14}{5}}$

c. $\frac{\binom{6}{3}\binom{8}{2}}{\binom{14}{5}}$

d. $1 - \frac{\binom{8}{2}}{\binom{14}{5}}$

- e. $\frac{\binom{6}{3}}{\binom{14}{5}} + \frac{\binom{8}{2}}{\binom{14}{5}}$
- 7. Suppose that, in a certain experiment, the events E and F are independent. If $Pr(E) = Pr(F) = \frac{1}{7}$, what is $Pr(E \cup F)$?

- a. $\frac{2}{3}$ b. $\frac{3}{4}$ c. 1 d. $\frac{7}{8}$ e. not enough information

- 8. A study finds that 20% of all inhabitants of the western part of Scotland suffer from heart disease, but only 10% of the inhabitants of the eastern part of Scotland do. 30% of the people of Scotland live in the western part, and 70% live in the eastern part. Suppose a Scottish citizen is chosen at random and is found to have heart disease. What is the probability that he/she comes from the western part of Scotland?

- a. $\frac{2}{3}$ b. $\frac{3}{10}$ c. $\frac{6}{13}$ d. $\frac{6}{70}$ e. $\frac{6}{7}$

- 9. Two cards are drawn from a standard deck of 52 cards. What is the probability that the first card is an ace and the second is a King if the first card is replaced before the second is drawn?
- a. $\frac{4}{52} + \frac{3}{52}$ $\left(\frac{4}{52}\right)^2$

b. $\frac{4}{52} + \frac{3}{51}$

C.

d. $\left(\frac{4}{52}\right)\left(\frac{5}{51}\right)$

- e. $\binom{4}{52} \binom{3}{51}$
- Suppose that E and F are events in an experiment, and $Pr(E) = \frac{1}{4}$, Pr(F) =10. $\frac{1}{2}$, $Pr(E \cup F) = \frac{3}{4}$. What is Pr(E|F)?
- a. 1 b. $\frac{1}{2}$ c. $\frac{1}{4}$

- d. 0
- e. १

- An urn contains 5 red balls and 5 white balls. 3 balls are drawn from the urn at random, one at a time and without replacement. What is the probability that the first ball drawn is red and the second and third are white?

- a. $\frac{1}{9}$ b. $\frac{1}{8}$ c. $\frac{5}{12}$ d. $\frac{2}{25}$ e. $\frac{5}{36}$

- A pair of fair dice is rolled 3 times. Find the probability that the dice add 12. up to 7 each time.

- a. $\frac{1}{12}$ b. $\frac{1}{6}$ c. $(\frac{1}{12})$ d. $(\frac{1}{6})^3$ e. $\frac{1}{2}$
- In a certain factory, an old machine produces bolts of which 10% are 13. defective. What is the probability that, in a random sample of 80 bolts produced by the machine, at least 3 are defective?
- a. $1 (.9)^{80} {80 \choose 1} (.1) (.9)^{79} {80 \choose 2} (.1)^{2} (.9)^{78}$
- b. $1 (.9)^{80} (.1) (.9)^{79} (.1)^2 (.9)^{78}$
- c. $\binom{80}{3}$ (.1) ³ (.9)⁷⁷
- d. $(.1)^3 (.9)^{77}$
- e. $(.9)^{80} + {80 \choose 1} (.1) (.9)^{79} + {80 \choose 2} (.1)^{2} (.9)^{78} + {80 \choose 3} (.1)^{3} (.9)^{77}$

- 14. The weight of a certain type of car (when it leaves the factory) is normally distributed with mean 998 kg and standard deviation .8 kg. Find the probability that a new car of this type chosen at random weighs between 997 kg and 999 kg.
- a. .8944
- b. .7698 c. .7888 d. .9876
- e. .9938
- Five fair coins are tossed simultaneously and the number X of heads is 15. observed. What is the variance of the random variable X?

- a. $\sqrt{\frac{5}{4}}$ b. $\frac{5}{2}$ c. $\frac{5}{4}$ d. $\frac{55}{25} \frac{4}{25}$ e. 1
- 16. The probability that a certain surgical operation is successful is 0.8 (it is a binomial distribution). If the operation is performed on 100 people, find the probability that 70 or more operations are successful (use normal distribution to approximate the binomial distribution):
- a. .9938

- b. .0062 c. .5 d. .8944 e. .1056
- 17. A bag contains three \$1 bills, two \$5 bills, and one \$10 bill. One bill is selected at random. If X denotes the denomination of the selected bill, find the expected value E(X).

- a. $\frac{1}{2} + \frac{1}{3} + \frac{1}{6}$ b. $\frac{1}{2} \cdot \frac{1}{3} \cdot \frac{1}{6}$ c. $(\frac{1}{2})^3 (\frac{1}{3})^2 (\frac{1}{6})$
- d. $\left(\frac{1}{2}\right)^3 + \left(\frac{1}{3}\right)^2 + \left(\frac{1}{6}\right)$ e. $1 \cdot \frac{1}{2} + 5 \cdot \frac{1}{3} + 10 \cdot \frac{1}{6}$

A random variable X has the following probability distribution: 18.

k
$$Pr(X = k)$$
-10 1/3
0 1/3
1 1/6
2 1/6

What is the expected value E(X)?

a.
$$-\frac{13}{4}$$
 b. $-\frac{7}{4}$ c. $-\frac{17}{6}$ d. $\frac{1}{4}$ e. $-\frac{7}{3}$

b.
$$-\frac{7}{4}$$

c.
$$-\frac{17}{6}$$

d.
$$\frac{1}{4}$$

e.
$$-\frac{7}{3}$$

The stable matrix of the absorbing stochastic matrix $\begin{bmatrix}
1 & 0 & 0 & \frac{1}{2} \\
0 & 1 & \frac{1}{4} & 0 \\
0 & 0 & \frac{1}{2} & 0 \\
0 & 0 & 1 & 1
\end{bmatrix}$ is 19.

$$\begin{bmatrix} 1 & 0 & 0 & \frac{1}{2} \\ 0 & 1 & \frac{1}{4} & 0 \\ 0 & 0 & \frac{1}{2} & 0 \\ 0 & 0 & \frac{1}{4} & \frac{1}{2} \end{bmatrix}$$
 is

a.
$$\begin{bmatrix} 1 & 0 & 1 & \frac{1}{2} \\ 0 & 1 & 0 & \frac{1}{2} \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix}$$

b.
$$\begin{bmatrix} 1 & 0 & \frac{1}{2} & 1 \\ 0 & 1 & \frac{1}{2} & \frac{1}{2} \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix}$$

c.
$$\begin{bmatrix} 1 & 0 & \frac{1}{2} & \frac{1}{2} \\ 0 & 1 & 1 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix}$$

d.
$$\begin{bmatrix} 1 & 0 & \frac{1}{2} & 1 \\ 0 & 1 & \frac{1}{2} & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix}$$

e.
$$\begin{bmatrix} 1 & 0 & 0 & \frac{1}{2} \\ 0 & 1 & 1 & \frac{1}{2} \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix}$$

- 20. The transition matrix of a Markov Process is given by the matrix $\begin{bmatrix} .7 & .1 \\ .3 & .9 \end{bmatrix}$. The stable distribution of this process is:
- a. $\begin{bmatrix} 1\\2\\1\\2 \end{bmatrix}$ b. $\begin{bmatrix} 1\\3\\2\\3 \end{bmatrix}$ c. $\begin{bmatrix} 2\\3\\1\\3 \end{bmatrix}$ d. $\begin{bmatrix} 2\\5\\3\\5 \end{bmatrix}$

- e.

21. The transition matrix of a Markov process is given by the matrix.

$$A = \begin{bmatrix} .1 & 0 & 0 \\ .2 & .5 & 0 \\ .7 & .5 & 1 \end{bmatrix}$$

The matrix A is

- a. regular
- b. absorbing c. regular and absorbing
- d. regular but not absorbing
- e. neither regular nor absorbing
- Calculate the amount at the end of 5 years if \$2,000 is invested at 22. 5% simple interest.

- a. 2,500 b. 2,250 c. 2,025 d. 2,750 e. 3,000

- 23. Let $A = \begin{bmatrix} \frac{1}{2} & \frac{1}{2} \\ \frac{1}{2} & \frac{1}{2} \end{bmatrix}$ be the transition matrix of a Markov Process. If the distribution of the current generation is $\begin{bmatrix} \frac{1}{2} \\ \frac{1}{2} \end{bmatrix}$. Then the distribution of the next generation is
- a. $\begin{bmatrix} 1 \\ 0 \end{bmatrix}$ b. $\begin{bmatrix} 0 \\ 1 \end{bmatrix}$ c. $\begin{bmatrix} \frac{1}{2} \\ \frac{1}{2} \end{bmatrix}$ d. $\begin{bmatrix} \frac{1}{4} \\ \frac{1}{4} \end{bmatrix}$ e. $\begin{bmatrix} \frac{1}{8} \\ \frac{1}{8} \end{bmatrix}$
- 27. Ted needs \$10,000 four years from now. How much should he invest now (one lump sum) in a savings account paying 6% annual interest compounded monthly?
- a. \$7,870.99
- b. \$1,633.39
- c. \$2,488.51

- d. \$2,633.39
- e. \$8,356.45
- 28. Mr. Rich takes out a 30-year \$300,000 mortgage at 9% annual interest, compounded monthly, with payments made monthly. What is the unpaid balance at the end of twenty years?
- a. \$2413.87
- b. \$190,555.72 c. \$109,444.28
- d. \$100,000
- e. \$290,000.15

- 29. Sue needs \$10,000 four years from now in order to pay off a loan. How much must she save each quarter for the next four years if interest rates are 8% compounded quarterly?
- a. \$490.22 b. \$386.53 c. \$326.02
- d. \$536.50 e. \$192.32
- 30. Mr. Smart purchased a car for \$1000 down payment plus monthly payments of \$300 for 3 years, at the annual interest rate of 18% compounded monthly. What is the purchase price (present value) of the car?
- a. \$108,000 b. \$118,000 c. \$97,000 d. \$8298.21 e. \$9298.21