

= 1.65cm = 5.5pt

I have not violated the Honor Code in any way with regard to this work.

Math 105-Test III April 12, 1994 =2

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The slope of the curve  $x^3 + y^3 = 9xy$  at  $(2, 4)$  is

$$\frac{4}{5} \cdot 3 - 4 - \frac{2}{5} \cdot \frac{5}{3}$$

Let  $f(x) = \sqrt{x+1} \ln(x+1)$ . Then  $f'(x) =$

$$\frac{2+\ln(x+1)}{2\sqrt{x+1}} \cdot \frac{1}{\sqrt{x+1}} + \frac{\ln(x+1)}{2\sqrt{x+1}} + \frac{\sqrt{x+1}}{\ln(x+1)} \cdot \frac{\ln(x+1)}{\sqrt{x+1}} - \frac{1}{\sqrt{x+1}} \cdot \frac{1}{2\sqrt{x+1}} \cdot \frac{1}{x+1}$$

The solution of the differential equation  $y' + y = 0, y(0) = 1$  is

$$y = e^{-x} \quad y = e^{-x} + e^x \quad y = e^x \quad y = 2e^{-x} \quad y = 1$$

Find  $x$  such that  $\ln 10^x = 10x$

$$x = 0 \quad x = 1 \quad x = \ln 10 \quad x = e \quad x = 10$$

The solution of the equation  $e^{x^2-x} = e^2$  is

$$x = 2 \text{ or } x = -1 \quad x = -2 \quad x = 0 \quad x = 1 \text{ or } x = -2 \text{ no solution}$$

The derivative of  $y = (xe^x + 1)^{-1}$  is

$$-(xe^x + 1)^{-2}(e^x + xe^x) \quad -(xe^x + 1)^{-2} + (e^x + xe^x) \quad (xe^x + 1)^{-1}(e^x + xe^x) \quad -(e^x + xe^x) - 2$$

The function  $y = (4x - 1)e^{3x-2}$  has one relative extremum point. This point is a minimum at  $x = -\frac{1}{12}$  minimum at  $x = \frac{1}{4}$  maximum at  $x = -\frac{1}{12}$  maximum at  $x = \frac{1}{4}$  minimum at  $x = \frac{2}{3}$

Solve the equation  $\ln(\ln(x+1)) = 1$

$$x = e^e - 1 \quad x = e - 1 \quad x = e^{e-1} \quad x = 0 \text{ no solution}$$

The equation of the tangent line to the graph of  $y = \ln(x^2 + 1)$  at  $x = 0$  is

$$y = 0 \quad y = x + 1 \quad x = -1 \quad y = -1 \quad y = 2x$$

Use logarithmic differentiation to find the derivative of  $f(x) = (x+1)^{(x+1)}$ .

$$[\ln(x+1) + 1](x+1)^{(x+1)} \quad (x+1)(x+1)^x \quad (x+1) \ln(x+1) \quad \frac{1}{x+1} \ln(x+1) \quad (x+1) [\ln(x+1) + 1]$$

From 1990 to 1993 the population of a town grew exponentially from 8000 to 16000. How large will the population be in the year 1996?

$$8000e^{2 \ln 2} \quad 16000 \frac{e^{2 \ln 2}}{8000} \quad 32000e^{\ln 2} \quad 8000e^{\ln 2}$$

The half life of an radioactive element is 3 days. Its decay constant is (assume  $\ln 2 = 0.69$ )

$$\lambda = 0.23 \quad \lambda = 0.069 \quad \lambda = 0.0023 \quad \lambda = 0.69 \quad \lambda = 0.023$$

$$\frac{d}{dx} [x^2 \ln \sqrt{x}] =$$

$$x \ln x + \frac{x}{2} \quad 2x \ln \sqrt{x} \quad 2x \frac{1}{\sqrt{x}} \quad 2x \frac{1}{\ln \sqrt{x}} \quad 2x \ln \frac{1}{2\sqrt{x}}$$

$$\frac{d}{dx} [(x+1)^2 e^{x^3-2}] =$$

$$2(x+1)e^{x^3-2} + 3x^2(x+1)^2 e^{x^3-2} \quad 2(x+1)e^{x^3-2} + (x+1)^2 e^{x^3-2} \quad 2(x+1) + e^{3x^2} \quad 2(x+1)e^{3x^2} \quad 2(x+1) + 3x^2 e^{x^3-2}$$

If \$50 is deposited in an account with 10% compounded continuously, how much money will be in the account after 10 years? (assume  $e=2.7$ )

135 125 75 155 100

If  $f(x) = \ln [(x^2 + 1)^{-3}(x^3 - 1)^4]$ , then  $f'(x)$  is

$$-\frac{6x}{x^2+1} + \frac{12x^2}{x^3-1} - 3 \ln (x^2 + 1)^{-4} + 4 \ln (x^3 - 1) - 6x \ln (x^2 + 1)^{-3} + 12x^2 \ln (x^3 - 1)^4$$

$$\frac{1}{(x^2+1)^3(x^3-1)^4} \frac{6x}{x^2+1} - 12x^2(x^3-1) \frac{d}{dx} [x^{e+\ln 2}] =$$

$$(e + \ln 2)x^{e+\ln 2-1} (e + \ln 2)x^{e+\ln 2} x^{e+\ln 2} \frac{1}{e+\ln 2} x^{e+\ln 2} e x^{e-1} + \ln 2 x^{\ln 2-1}$$

$$e^{2 \ln x^3 - \ln 4 + \ln x} =$$

$$\frac{x^7}{4} \frac{x^4}{2} 2x^3 - 4 + x \frac{2}{x^3} - \frac{1}{4} + \frac{1}{x} - \frac{1}{2x^4}$$

The derivative of  $f(x) = \ln(1 + e^x)^2$  is

$$\frac{2e^x}{1+e^x} 2 \frac{e^x}{(1+e^x)^2} 2e^x \ln(1 + e^x) 2(1 + e^x) \ln(1 + e^x)$$

If  $x^{\frac{2}{3}} + y^{\frac{2}{3}} = 8$ , then  $y' =$

$$-\left(\frac{y}{x}\right)^{\frac{1}{3}} - y^{-\frac{1}{3}} - x^{-\frac{1}{3}} \left(\frac{x}{y}\right)^{\frac{1}{3}} y^{\frac{1}{3}} + x^{\frac{1}{3}} y^{\frac{1}{3}} - x^{\frac{1}{3}}$$