

Brief Article

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This exam is worth a total of 100 points. There are 11 problems – 8 multiple choice and 3 partial credit. Each multiple choice problem is worth 7 points. Point values are assigned next to the partial credit problems. Please show all work on the partial credit section of the test inside the test booklet. Use the front sheet to answer the multiple choice section by putting a in the appropriate box. You will have until 9:20am to complete the exam. Good luck!

Sign your name

$6=2.5\text{in}=0.8\text{cm}=1\text{cm}=0.4\text{cm}=1$ Evaluate $\int x^2 + \frac{1}{3}e^{-2} e^{-2} \infty 1 3e^{-2} 3 \sin(2x) dx$.

$$\frac{1}{3}x^3 - 3 \cos(2x) + C \quad \frac{1}{3}x^3 - \frac{3}{2} \cos(2x) + C \quad \frac{1}{3}x^3 + \frac{3}{2} \cos(2x) + C \quad 3x^3 - 3 \cos(2x) + C \quad 3x^3 + 6 \cos(2x) + C$$

Evaluate $\int \ln x dx$

$$x \ln x - x + C \quad \frac{1}{x} + C \quad \frac{1}{2}(\ln x)^2 + C \quad \frac{\ln x}{x} + C \quad \frac{e^x}{x} + C$$

The marginal cost function for a company is given by $MC(x) = 3x^2 - 17x + 2000$. If the fixed costs for the company are \$12,000, what is the total cost function $C(x)$?

$$x^3 - \frac{17}{2}x^2 + 2000x - 12,000 \quad 3x^3 - 17x^2 + 2000x - 12,000 \quad x^3 - \frac{17}{2}x^2 + 2000x + 12,000 \quad x^3 - \frac{17}{2}x^2 + 2000x$$

It cannot be determined from the information provided.

Consider the following graph of the supply curve, $S(q)$, and the demand curve, $D(q)$ for a certain item. Which region/regions denoted on the graph correspond to the consumer's surplus?

A+B B A A+B+C B+C

Determine the average value of the function $y = \cos x$ between $x = 0$ and $x = \frac{\pi}{2}$.

$$2 \quad 0 \quad 2\pi \quad \frac{\pi}{2} \quad \frac{2}{\pi}$$

Find the area underneath the curve $y = e^{-x/3}$ for $x \geq 6$.

How long will it take an amount of money to triple if interest is 10% compounded continuously? You may assume $\ln 3 \approx 1.1$.

5 12 7 The answer cannot be determined without knowing the initial amount invested. 11

Approximate the value of the definite integral of the function $f(x)$ from $x = 1$ to $x = 3$ using the table below and the left endpoint method.

x	1	1.5	2	2.5	3
f(x)	1	2	2	3	5

8 5 6 9 4

Suppose that a museum sells tickets for an exhibit and that the number of tickets sold (q) depends upon the price of the ticket (p) so that $q = -100p + 1000$. (Note that this means that for each \$1 decrease in price, 100 more people will buy a ticket.) The museum wants to know at what price they should sell their tickets so as to maximize their revenue. What price would this be, and how much revenue would the mu-

seum make at this price? (16 points)

b. What is the equilibrium price p_e ?

c. Compute the consumer surplus.

d. Compute the producer surplus.

Find the area between the curves $y = x^2e^{2x}$ and $y = 0$ from $x = 0$ to $x = 1$. (Note that the first function always has a positive value, so it is

(16 points) Suppose that the demand curve for producing a quantity q of some item is given by:

$$D(q) = \frac{50}{q+1}$$

and the supply curve is given by:

$$S(q) = q + 6.$$

a. What is the equilibrium quantity q_e ?

always greater than or equal to 0.) (12 points)