

[11pt]article graphicx amssymb epstopdf .tifpng.png'convert 1 'dirname 1'/'basename 1 .tif.png  
= 6.5 in = 9 in = 0.0 in = 0.0 in = 0.0 in = 0.0 in = 0.0 in

theoremTheorem corollary[theorem]Corollary definitionDefinition

Brief Article The Author document

minipage[c]6in 1. Please cross × the correct answers.

[-2mm]0mm8mm **Sign your name:6cm 6cm**10=2.2in =0.8cm =1cm =0.4cm=1 Compute the definite  
integral  $\int_0^1 xe^x dx =$

1 e - 1 e - e - 1

Assume a certain amount of money is in a bank account with an annual interest rate of 10% compounded  
continuously. Compute the number of years it takes until the amount triples.

10 ln 3 10 17 20 5 ln 3

Compute the improper integral

$$\int_2^{\infty} x^{-4} dx.$$

124 13 18 -112 -16

A company determines that its marginal profit function is  $MP(x) = -300x^2 + 600x + 400$ . If the company  
makes \$300 when it sells 2 items, what is the total profit function?

$-100x^3 + 300x^2 + 400x - 900$   $-100x^3 + 300x^2 + 400x$   $-100x^3 + 300x^2 + 400x + 300$   $-100x^3 + 300x^2 + 400x + 150$   
 $-100x^3 + 300x^2 + 400x - 750$

Solve the following differential equation with given initial condition:

$$y' = 13y - 1, \quad y(0) = 1.$$

$f(t) = 3 - 2e^{13t}$   $f(t) = 4 - 2e^{13t}$   $f(t) = 3 - 12e^{13t}$   $f(t) = 3 - e^{12t}$   $f(t) = 5 - e^{3t}$

Assume  $y' = t^3$  and  $y(0) = 1$ . Compute  $y(2)$ .

5 3 9 0 12

Find the equation of the plane through the points  $(3, 0, 0)$ ,  $(0, 4, 0)$  and  $(0, 0, 2)$ .

$4x + 3y + 6z = 12$   $x + 34y + 2z = 3$   $8x + 4y + 2z = 8$   $13x + 14y + 12z = 0$   $16x + 13y + 12z = 4$

For what value of  $k$  does the following system of equations have **no solution**?

$$\begin{array}{r} 9x - 6y = -31 \end{array}$$

$$k = 10 \quad k = -10 \quad k = 231 \quad k = 90 \quad k = 23$$

Determine which of the following functions is a solution of the differential equation  $y'' - 6y' + 8y = 0$ .

$$e^{4t} \quad e^{8t} \quad e^{5t} \quad e^{6t} \quad e^{-5t}$$

A continuous random variable  $X$  has a probability density function  $f(x) = 38x^2$  for  $0 \leq x \leq 2$ . What is the expected value  $E(X)$ ?

$$32 \quad 316 \quad 1 \quad 52 \quad 43$$

Find the line of least squares  $y = ax + b$  which best fits the data points  $(-3, -5)$ ,  $(1, 3)$  and  $(2, 5)$ .

$$y = 2x + 1 \quad y = 3x + 2 \quad y = x + 1 \quad y = 5x + 4 \quad y = 3x$$

Consider the function  $f(x, y) = -6x^2 - 7xy - 2y^2$ . Then one has:

$(0, 0)$  is a saddle point.  $(0, 0)$  is a relative minimum.  $(0, 0)$  is a relative maximum. The second derivative test is inconclusive. There are no critical points.

Let  $X$  be a discrete random variable whose distribution is given by

$$\text{array}{c|c|c|c|c|c|c|x} 2468101214$$

Compute the Variance  $\text{Var}(X)$ .

$$485 \quad 275 \quad 365 \quad 125 \quad 325$$

Let  $Z$  have the standard normal distribution. Compute  $\Pr(1 \leq Z)$ .

$$0.3413 \quad 0.500 \quad 0.1587 \quad 0.8413 \quad 0.6742$$

(13 pts) The demand curve of a certain item is  $p = D(q) = 100q + 1$  and its supply curve is  $p = S(q) = q + 1$ .

(6 pts) Find the equilibrium price  $p_e$  and equilibrium quantity  $q_e$ . \*8cm

(6 pts) Compute the producer surplus.

\*8cm

(13 pts) A person opens an Individual Retirement Account (IRA) with the initial amount of \$50,000. Then \$6,000 per year is deposited in this IRA in a uniform and continuous manner. Assume that the interest rate is 7.5% compounded continuously.

(4 pts) Model this problem as a Calculus problem by finding a **differential equation** and an **initial condition** describing the amount of money,  $M(t)$ , in the IRA at any time  $t$ .

\*4cm

(5 pts) Solve the obtained differential equation, i.e. find  $M(t)$  at any time  $t$ .

\*8cm

(4 pts) Compute the balance in the IRA after 20 years. (If you do not have a calculator you can approximate  $e^{1.5}$  with 4.5).

\*4cm

(13 pts) The Cobb-Douglas production function for a certain product is given by  $f(x, y) = 5x^{35}y^{25}$  where  $f(x, y)$  is the quantity produced,  $x$  denotes units of labor force and  $y$  denotes units of capital. Assume that each unit of labor costs \$400, each unit of capital costs \$100, and the total budget is \$20,000. Find the amounts of labor and capital which will maximize the company's production while keeping within the constraints of the budget.

\*15cm

**Answer:**  $x = 2$   $y = 2$

(13 pts) A bank has 1,000,000 credit card holders. During the preceding year the average billing to each card holder was \$195 and the standard deviation was \$60. It is assumed that the billings are normally distributed. Compute the number of customers whose bill exceeds \$300.

\*18cm

**Answer:** Number = 2