

1. Which one of the following is true?

(A) If f is not continuous at c , then $\lim_{x \rightarrow c} f(x)$ does not exist

(B) If f is not continuous at c , then $\lim_{x \rightarrow c^+} f(x) \neq \lim_{x \rightarrow c^-} f(x)$

(C) If $\lim_{x \rightarrow c} f(x) = L$, then $f(c) = L$

(D) If f is continuous at c , then $\lim_{x \rightarrow c^+} f(x) = \lim_{x \rightarrow c^-} f(x)$

(E) If $f(c) = L$, then $\lim_{x \rightarrow c} f(x) = L$

2. $\lim_{x \rightarrow 1} (x^2 - 1) \csc(x - 1) =$

(A) $-\infty$

(B) ∞

(C) 0

(D) 1 (E) 2

3. $\lim_{x \rightarrow 1} \frac{x-1}{\sqrt{x+3}-2} =$

- (A) 0 (B) ∞ (C) 4 (D) 2 (E) $\frac{1}{2}$

4. The function

$$f(x) = \begin{cases} \cos x, & x \leq 0 \\ \frac{\sin x}{x}, & 0 < x \leq \frac{\pi}{2} \\ \frac{2x - \frac{\pi}{2} + 1}{4x - 2\frac{\pi}{2} + 1}, & x > \frac{\pi}{2} \end{cases}$$

- (A) is continuous only when $0 < x < \frac{\pi}{2}$
 (B) is continuous for all values of x
 (C) is discontinuous only at $x = \frac{\pi}{2}$
 (D) is discontinuous only at $x = 0$
 (E) is discontinuous at both $x = 0$ and $x = \frac{\pi}{2}$

5. $\lim_{h \rightarrow 0} \frac{(\sqrt{2} + h)^5 - (\sqrt{2})^5}{h} =$

(A) $20\sqrt{2}$

(B) 20

(C) $10\sqrt{2}$

(D) 10

(E) $5\sqrt{2}$

6.

From the graphs, which one of the following appears to be true?

(A) h is the derivative of f

(B) g is the derivative of f

(C) h is the derivative of g

(D) g is the derivative of h

(E) f is the derivative of g

7. Suppose $f(x)$ is a function for which $f(1) = 2$ and $f'(1) = 3$. If

$$g(x) = \frac{x+1}{f(x)},$$

then $g'(1) =$

- (A) -1 (B) $\frac{1}{3}$ (C) 1 (D) $\frac{2}{3}$ (E) $-\frac{1}{3}$

8. If $f(x) = \frac{3x+8}{x+2}$, then $f''(0) =$

- (A) $\frac{1}{4}$ (B) $-\frac{1}{2}$ (C) $\frac{1}{2}$ (D) $-\frac{1}{4}$ (E) 0

9. The equation of the tangent line to the curve $y = \cot x$ at the point $\left(\frac{\pi}{4}, 1\right)$ is

- (A) $y = -x + \frac{\pi}{4} + 1$ (B) $y = -\frac{1}{2}x + \frac{\pi}{8} + 1$
(C) $y = -\frac{1}{2}x + \frac{\pi}{4} + 1$ (D) $y = -2x + \frac{\pi}{4} + 1$
(E) $y = -2x + \frac{\pi}{2} + 1$

10. If $f(x) = x^2 \cos x$, then $f'\left(\frac{\pi}{2}\right) =$

- (A) $\frac{\pi^2}{4}$ (B) $-\pi$ (C) 0 (D) $-\frac{\pi^2}{4}$ (E) π

11. The position of a body moving along a coordinate line is given by the equation

$$s = t^4 - 4t^3 + 8t^2 - 2t + 1.$$

At a certain time, the acceleration of the body happens to be 4, and then the position of the body is given by $s =$

- (A) -2 (B) 4 (C) 1 (D) 3 (E) 0

12. If $f(x) = \left(x^2 - x - \frac{2}{x}\right)^{10}$, then $f'(2) =$

- (A) 35 (B) $10\left(\frac{7}{2}\right)^9$ (C) 10 (D) $\left(\frac{7}{2}\right)^{10}$ (E) 70

13. If $f(x) = \tan^2\left(2x + \frac{\pi}{4}\right)$, then $f'(0) =$

- (A) 2 (B) $\sqrt{2}$ (C) $2\sqrt{2}$ (D) 8 (E) 4

14. The tangent line to the curve

$$x^2 y^2 - 3x + 6y + 8 = 0$$

at the point (2, -1) has equation

- (A) $y = -\frac{1}{2}x$ (B) $y = -2x + 3$ (C) $y = x - 3$
(D) $y = \frac{1}{2}x - 2$ (E) $y = 2x - 5$

15. Suppose $f(x) = x^3 - 3x^2 + 10$. Let M be the largest value of $f(x)$, and m the smallest value of $f(x)$, where the values of x lie in the interval $[-2, 3]$. Then

- (A) $M = 6$ and $m = -10$ (B) $M = 6$ and $m = -6$
(C) $M = 6$ and $m = 0$ (D) $M = 10$ and $m = -10$
(E) $M = 10$ and $m = 6$

16. A certain function $f(x)$ has derivative given by

$$f'(x) = x(x-1)^2(x-2)^3.$$

The function $f(x)$ is increasing on the intervals

- (A) $(1, 2)$ and $(2, \infty)$
- (B) $(-\infty, 0)$ and $(2, \infty)$
- (C) $(0, 1)$ and $(2, \infty)$
- (D) $(0, 1)$ and $(1, 2)$
- (E) $(-\infty, 0)$ and $(1, 2)$

17. Suppose $f(x)$ is a differentiable function for which $f(-1) = -1$ and $f(1) = 2$. Then the mean value theorem or Rolle's theorem implies

- (A) There is a value of c between -1 and 1 for which $f'(c) = \frac{3}{2}$.
- (B) There is exactly one value of x between -1 and 1 where $f(x) = 0$.
- (C) There is at least one value of x between -1 and 1 where $f(x)$ has either a local maximum or a local minimum.
- (D) There is a value of c between -1 and 1 for which $f'(c) = 0$.
- (E) $f(x)$ is never decreasing anywhere within the interval $(-1, 1)$.