

1.

How many of the following statements about the function  $y = f(x)$  pictured above, are true?

- (i)  $\lim_{x \rightarrow 1} f(x)$  exists
- (ii)  $\lim_{x \rightarrow 2} f(x)$  exists
- (iii)  $\lim_{x \rightarrow 3^+} f(x)$  does not exist
- (iv)  $\lim_{x \rightarrow 3^-} f(x)$  does not exist

(A) 0      (B) 1      (C) 2   (D) 3      (E) 4

2.  $\lim_{x \rightarrow 1} \frac{x - \sqrt{3x - 2}}{x^2 - 1} = ?$

(A)  $\frac{1}{3}$       (B)  $-\frac{1}{4}$       (C)  $\frac{\sqrt{2}}{3}$       (D)  $-\frac{1}{2}$       (E)  $-\frac{3}{2}$

3.  $\lim_{t \rightarrow 0} \frac{t}{\sqrt{t}} = ?$

- (A)  $-\infty$       (B) 1      (C)  $\infty$       (D) 0 (E) -1

4.  $\lim_{h \rightarrow 0} \frac{\left(-\frac{1}{2} + h\right)^4 + \left(-\frac{1}{2}\right)^4}{h} = ?$

- (A) 2      (B)  $-\frac{1}{2}$       (C)  $\frac{1}{4}$       (D)  $-\frac{3}{4}$       (E)  $\frac{1}{8}$

5. Which of the following partial graphs shows the behavior of

$$f(x) = \frac{x-2}{(x+3)(x-1)^2} \quad \text{for } x \text{ near } 1?$$

(A)

(B)

(C)

(D)

(E)

6. Define  $g\left(\frac{1}{2}\right)$  in a way that extends

$$g(x) = \frac{2x - 1}{8x^2 - 4x}$$

to be continuous at  $x = \frac{1}{2}$ .

- (A) 2      (B)  $-\frac{1}{4}$       (C) 0      (D) -1      (E)  $\frac{1}{2}$

7. Let  $f(x) = x^3 - x^2 + x + 3$ . Which one of the following values must the function  $f$  take on at some point on the interval  $[0, 1]$ ?

- (A) -1      (B)  $\sqrt{2}$       (C)  $\frac{5}{2}$       (D)  $\pi$       (E) 7

8. The equation of the tangent line to the curve

$$y = 4 \cos x - 2 \sin x$$

at the point  $\left(\frac{\pi}{2}, -2\right)$  is

- (A)  $y = -4x + 2\pi - 2$       (B)  $y = 2x - 2\pi$   
(C)  $y = x - \frac{3}{2}\pi$       (D)  $y = -4x + \pi + 1$   
(E)  $y = -2x$

9.                       $y = f(x)$                        $y = g(x)$                        $y = h(x)$

From the graphs, which one of the following statements appears to be true?

- (A)  $f(x)$  is the derivative of  $h(x)$   
(B)  $g(x)$  is the derivative of  $f(x)$   
(C)  $g(x)$  is the derivative of  $h(x)$   
(D)  $h(x)$  is the derivative of  $f(x)$   
(E)  $h(x)$  is the derivative of  $g(x)$
10. If  $y = \frac{\tan x}{1 + \tan x}$ , then the slope of the curve at the point  $\left(\frac{\pi}{4}, \frac{1}{2}\right)$  is
- (A)  $\frac{\pi}{4}$       (B) 1      (C)  $\frac{1}{2}$       (D) 0      (E) 2

11. Suppose that  $f(x)$  is a function for which  $f(1) = -3$  and  $f'(1) = 1$ . If  $g(x) = (x + 1)f(x)$ , then  $g'(1) = ?$

- (A) 2      (B) 0      (C) -3      (D) 1      (E) -1

12. The position of a body at time  $t$  seconds is  $s = 2t^3 - 15t^2 + 54t - 12$  feet.

What is the body's velocity, in ft/sec, at the time the acceleration is 6 ft/sec<sup>2</sup>?

- (A) 12      (B) 0      (C) -9      (D) 18      (E) -15