

1. In the Maclaurin expansion of

$$e^{-2x} + (1 + 3x)^2 + \cos(2x^2)$$

the coefficient of  $x^4$  is

- (A)  $\frac{1}{3}$       (B)  $\frac{3}{2}$       (C)  $-\frac{4}{3}$       (D) 0      (E)  $-\frac{1}{2}$

2. The degree 5 term of the Maclaurin series for  $\sin x \cos x$  is

- (A)  $x^5$       (B)  $\frac{2}{15} x^5$       (C)  $-\frac{x^5}{10}$       (D)  $\frac{3}{20} x^5$       (E)  $\frac{8}{5}$   
 $x^5$

3. Suppose that we compute an approximate value for  $(1.2)^{9/4}$  by using the 2nd order Taylor polynomial for  $f(x) = x^{9/4}$  at  $a = 1$ . According to Taylor's theorem, the error in the approximation is

- (A)  $\frac{45}{64} \cdot c^{9/4}$ , where  $1 < c < 1.2$
- (B)  $\frac{1}{1600} \cdot \frac{1}{c^{3/4}}$ , where  $0 < c < 0.2$
- (C)  $\frac{45}{64} c^3$ , where  $0 < c < 0.2$
- (D)  $\frac{3}{3200} \cdot \frac{1}{c^{3/4}}$ , where  $1 < c < 1.2$
- (E)  $\frac{1}{3200} c^3$ , where  $1 < c < 1.2$

4. The number  $\int_0^1 \cos \sqrt{t} \, dt$  is equal to which of the following infinite series?

- (A)  $\sum_{n=0}^{\infty} (-1)^n \frac{1}{n[(2n)!]}$
- (B)  $\sum_{n=0}^{\infty} (-1)^n \frac{1}{(n+1)[(2n)!]}$
- (C)  $\sum_{n=0}^{\infty} (-1)^n \frac{1}{n[(2n-1)!]}$
- (D)  $\sum_{n=0}^{\infty} (-1)^n \frac{1}{2n[(2n)!]}$
- (E)  $\sum_{n=0}^{\infty} (-1)^n \frac{1}{2n[(2n-1)!]}$

5. The curve C is given parametrically by

$$\begin{aligned}x &= e^{-t} \\ y &= e^t\end{aligned}\quad \text{for all } t$$

Which of the following curves most clearly resembles C?

(A)

(B)

(C)

(D)

(E)

6. The curve C is described by the parametric equations

$$x = \sec^2 t - 1$$

$$y = \tan t$$

The equation of the tangent line to C at  $t = \frac{-\pi}{4}$  is

- (A)  $x - 2y + 3 = 0$                       (B)  $y = 2x - 3$   
(C)  $x + 2y + 1 = 0$                       (D)  $2x + y - 1 = 0$   
(E)  $y = -\frac{x}{2} - \frac{1}{2}$

7. The length of the curve given by parametric equations

$$\begin{aligned} x &= 2(\cos t + t \sin t) \\ y &= 2(\sin t - t \cos t) \end{aligned} \quad \text{for } 0 \leq t \leq \pi$$

is

- (A)  $6\sqrt{2}$                       (B)  $2\pi$                       (C) 8                      (D)  $\pi^2$                       (E)  $4\sqrt{\pi}$

8. The polar equation of the circle of radius 5, whose center has Cartesian coordinates  $(4, -3)$  is given by

(A)  $r = 5 \sin\theta$

(B)  $r^2 = 4 \cos\theta - 3 \sin\theta$

(C)  $r = 2 \cos\theta - \sqrt{3} \sin\theta$

(D)  $r^2 = -3 \cos\theta + 4 \sin\theta$

(E)  $r = 8 \cos\theta - 6 \sin\theta$

9. The polar equation  $r = 2 \sin\theta \tan\theta$  represents a curve whose Cartesian equation is

(A)  $x^2 y^2 + x^4 = y^3$

(B)  $\sqrt{x^2 + y^2} = 2 y^2/x$

(C)  $x^3 + xy^2 = 2y^2$

(D)  $x^2 y^2 + y^4 = x^2$

(E)  $\sqrt{x^2 + y^2} = y$

10. The graph of the polar equation  $r = \cos 2\theta$  most closely resembles

(A)

(B)

(C)

(D)

(E)

11. The area of the region that is bounded by the curve

$$r = 4 \cos \theta$$

is

(A)  $8\sqrt{2}$

(B) 12

(C)  $2\pi^2$

(D)  $2\pi + 4\sqrt{2}$

(E)  $4\pi$