

Name: \_\_\_\_\_

Instructor: \_\_\_\_\_

Exam II - 126 2000S

March 21, 2000

- The Honor Code is in effect for this examination. All work is to be your own.
- No calculators.
- The exam lasts for one hour.
- Be sure that your name is on every page in case pages become detached.
- Be sure that you have all 11 pages of the test.

Good Luck!

PLEASE MARK YOUR ANSWERS WITH AN X, not a circle!

- |     |     |     |     |     |     |
|-----|-----|-----|-----|-----|-----|
| 1.  | (a) | (b) | (c) | (d) | (e) |
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Total multiple choice: \_\_\_\_\_

11. \_\_\_\_\_

12. \_\_\_\_\_

13. \_\_\_\_\_

14. \_\_\_\_\_

15. \_\_\_\_\_

**Total:** \_\_\_\_\_

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**Multiple Choice**

1.(5 pts.) Solve the initial value problem  $\frac{dy}{dx} = \frac{3x^2 - 1}{e^y}$ ,  $y(1) = 1$ .

(a)  $y = \ln(x^3 + x) + \ln(e/2)$

(b)  $y = e^{x^3-x}$

(c)  $y = e^{x^3-2x+1}$

(d)  $y = \arctan\left(\frac{1}{\sqrt{3}}\right) + \frac{\pi}{4}$

(e)  $y = \ln(x^3 - x + e)$

2.(5 pts.)

$$\int \frac{x^2}{1+x^2} dx =$$

(a)  $\sec x \tan x + c$

(b)  $\arctan \frac{1}{x} + c$

(c)  $\frac{x}{2} \ln |1+x^2| + c$

(d)  $x - \arctan x + c$

(e)  $\frac{1}{2} \ln |1+x^2| + c$

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3.(5 pts.)

$$\int_4^5 \frac{1}{x^2 - 5x + 6} dx =$$

- (a)  $\ln \frac{4}{3}$       (b) divergent      (c)  $\ln \frac{5}{4}$       (d)  $\ln 20 - \ln 3$       (e)  $\ln 5 - \ln 3$

4.(5 pts.)

$$\int (2x + 1)e^x dx =$$

- (a)  $(x^2 + x + c)e^x$       (b)  $(x^2 + x)e^x + c$       (c)  $2xe^x - e^x + c$   
(d) divergent      (e)  $\frac{1}{2}xe^{x^2+1} + c$

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5.(5 pts.)

$$\int \ln(1-x) dx =$$

(a)  $\frac{-2x}{1-x^2} + c$

(b)  $x \ln(1-x) - x + c$

(c)  $(x-1) \ln(1-x) - x + c$

(d)  $(1-x) \ln(1-x) - (1-x) + c$

(e)  $\ln(\arctan x^2) + c$

6.(5 pts.)

$$\int_0^1 \frac{2x dx}{\sqrt{1-x^2}} =$$

(a)  $1/2$

(b)  $2$

(c) divergent

(d)  $1$

(e)  $-4$

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7.(5 pts.) If  $a_1 = -1$ ,  $a_2 = 2$ , and  $a_{n+2} = a_{n+1} + a_n$  for  $n \geq 1$  what is  $a_5$ ?

- (a) 4                      (b) -5                      (c) 2                      (d) 5                      (e) -1

8.(5 pts.) Determine  $\lim_{k \rightarrow \infty} 1 + \frac{2^k}{k!}$

- (a)  $\infty$                       (b) 0                      (c) 1                      (d)  $1/k!$                       (e)  $3/2$

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9.(5 pts.) List all values of  $x$  for which  $\sum_{n=1}^{\infty} \left( \frac{1}{x^2 + 3/4} \right)^n$  converges.

- (a)  $x > \sqrt{3/4}$     (b)  $|x| > 1/2$     (c)  $|x| \geq 1$     (d)  $|x| \geq \sqrt{3}/2$     (e)  $x \neq 0$

10.(5 pts.) Determine  $\sum_{n=1}^{\infty} ((1/2)^n + (1/4)^n)$

- (a)  $3/2$     (b)  $9/4$     (c)  $3/4$     (d)  $4/3$     (e)  $3$

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**Partial Credit**

**11.**(10 pts.) Solve the equation

$$t \frac{dy}{dt} + 2y = 5t^3$$

with initial condition  $y(1) = 0$ .

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**12.**(10 pts.) Find just the partial fraction decomposition (not the integral) of

$$\frac{2x^2 - 4x + 1}{(x - 1)^2(x - 2)} =$$

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**13.**(10 pts.) Using substitution, and then a trig substitution, find

$$\int_1^e \frac{dy}{y\sqrt{1+(\ln y)^2}} =$$

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14.(10 pts.) Does  $\int_1^{\infty} \frac{(1 + \sin x)}{x^{4/3}} dx$  converge or diverge? Why?

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**15.**(10 pts.) Determine the convergence of the sequence  $\{a_n\}$  with  $a_n = \frac{1}{n^2} \int_1^n x \, dx$ .

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