Instructor: <u>Bullwinkle</u>

Exam I bruery 15, 200

- February 15, 2001
- The Honor Code is in effect for this examination. All work is to be your own.
- No calculators.
- The exam lasts for one hour.
- Be sure that your name is on every page in case pages become detached.
- Be sure that you have all 10 pages of the test.

Good Luck!							
PLE	ASE MARK	YOUR A	NSWERS	WITH AN X	, not a circle!		
1.	(a)	(b)	(c)	(d)	(e)		
2.	(a)	(b)	(c)	(d)	(e)		
3.	(a)	(b)	(c)	(d)	(e)		
4.	(a)	(b)	(c)	(d)	(e)		
5.	(a)	(b)	(c)	(d)	(e)		
6.	(a)	(b)	(c)	(d)	(e)		
7.	(a)	(b)	(c)	(d)	(e)		
8.	(a)	(b)	(c)	(d)	(e)		
9.	(a)	(b)	(c)	(d)	(e)		
10.	(a)	(b)	(c)	(d)	(e)		

DO NOT WRITE IN THIS BOX!					
Total multiple choice:					
11.					
12.					
13.					
14.					
Total:					

Multiple Choice

1.(5 pts.) The function x^x has a global minimum on the interval x > 0. (You need not check this.) This minimum value occurs at

(a)
$$x = \ln e - 1$$
 (b) $x = \frac{1}{2}$ (c) $x = \ln 2$ (d) $x = \frac{1}{e}$ (e) $x = e$
2.(5 pts.) $\frac{d}{dx} \ln(\ln x) = ?$
(a) $\frac{1}{\ln x}$ (b) $\frac{\ln x}{x}$ (c) $\frac{\ln x}{\ln(\ln x)}$ (d) $\frac{1}{x \ln x}$ (e) $\frac{x}{\ln x}$
3.(5 pts.) $\int_{0}^{\pi/3} \tan x \, dx =$
(a) 4 (b) 3 (c) $\ln \frac{1}{2}$ (d) $\sqrt{3}$ (e) $\ln 2$

4.(5 pts.) On the teeter-totter with weights as indicated you need to place one further mass of 2kg in such a way as to balance the beam. At what distance from the left-end is the correct location?

(e)

 $\ln 2$

teeter.eps

(a)

4

- (a)0.5(b) 1.0(c) 1.5(d) 2.0
- There is no such distance. (e)

5.(5 pts.) Suppose you know the following results about a differentiable function:

• its inverse function q exists

(b)

3

• f(2) = 4 and f'(2) = 3. Which of the following is certain to be true?

(a)
$$g'(4) = \frac{1}{3}$$
 (b) $g'(3) = \frac{1}{4}$ (c) $g'(4) = \frac{1}{2}$ (d) $g'(2) = \frac{3}{4}$ (e) $g'(2) = \frac{1}{3}$

6.(5 pts.) If
$$y = \frac{1}{2}(e^x + e^{-x})$$
, then $\int_{-2}^2 \sqrt{1 + \left(\frac{dy}{dx}\right)^2} dx =$
(a) e^2 (b) $e^2 - e^{-2}$ (c) $e^2 - 1$ (d) $e^2 + e^{-2}$ (e) $2e^2$

7.(5 pts.)
$$\frac{a}{dx} 4 \arctan e^x |_{x=0} =$$

(a) 0 (b) 1 (c) 2 (d) 3 (e) 4

8.(5 pts.) Which of the following is an integrating factor for the expression

 $y' + (\cot x)y$

i.e. which function v below satisfies $(vy)' = vy' + v(\cot x)y$.

(a) 1 (b) $\sin y$ (c) $e^{\sin x}$ (d) $\ln \sin x$ (e) $\sin x$

9.(5 pts.) Which of the following statements is true for general x > 0

(a) $10^{\ln x} = x^{\log_{10} e}$ (b) $10^{\ln x} = x^{\ln 10}$ (c) $10^{\ln x} = \ln 10^{x}$

(d)
$$10^{\ln x} = e^{\log_{10} x}$$
 (e) $10^{\ln x} = (\ln x)^{10}$

10.(5 pts.)

$$\frac{d}{dx}(\arccos x)^2 =$$

(a)
$$\frac{-2 \arccos x}{\sqrt{1-x^2}}$$
 (b) $\frac{-2x}{\sqrt{1-x^2}}$ (c) $\arccos \frac{x}{\sqrt{1-x^2}}$ (d) $\frac{\sin x}{\cos^2 x}$

(e) $\frac{-2x}{\sqrt{1-x^4}}$

Partial Credit

11.(13 pts.)

graph.eps

- (a) Find the area of the boomerang shaped (shaded) region.
- (b) Find the moment about the axis of your choice.
- (c) Use symmetry to find the coordinates of the center of mass.

Hint for (a) and (b): The integral for each answer will be in two pieces.

12.(13 pts.) Evaluate the integral
$$\int_{-1}^{0} \frac{1}{x^2 + 2x + 2} dx$$

13.(12 pts.) Find y(1) if y is the unique function which satisfies

$$y' = \sqrt{1 - y^2} \cdot x \quad , \quad y(0) = 0$$

14.(12 pts.) Find the general solution to the differential equation

$$y' = \frac{2y}{x} + x \quad (x > 0)$$

Instructor: ANSWERS

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