

Syllabus for Math 165 (Fall 1997)

Chapter 1 Some Basic Concepts

- (1) Integers, Rational Numbers, Real Numbers
- (2) Mathematical Induction
- (3) Supremum and Infimum
- (4) Absolute Values and The triangle Inequality

Chapter 2 Integral Calculus

- (1) Functions
- (2) Partitions and Step Functions
- (3) Integral of Step Functions
- (4) Upper and Lower Integrals
- (5) The Concept of Integrable Functions
- (6) Integrability of Piecewise Monotonic Functions
- (7) Basic Properties of Integrals
- (8) Application of Integrals
- (9) Trigonometric Functions
- (10) Polar Coordinates
- (11) Area and Volume

Chapter 3 Continuous Functions

- (1) The Concept of Limit
- (2) Basic Properties of Limit
- (3) The Concept of Continuity
- (4) Basic Properties of Continuous Functions
- (5) Bolzano's Theorem, Intermediate-Value Theorems and The Extreme-Value Theorem
- (6) Integrability of Continuous Functions

Chapter 4 Differentiable Functions

- (1) The Concept of Differentiability
- (2) Derivative and Tangents
- (3) Differentiability implies Continuity

- (4) Basic Rules of Differentiation
- (5) Chain Rule
- (6) Applications: Maxima and Minima (First and Second Derivative Tests)
- (7) The Mean-Value Theorem

Chapter 4 The relationship between Integration and Differentiation

- (1) Primitive Functions
- (2) The Fundamental Theorem of Calculus
- (3) Techniques of Integrations (Substitution, by Parts, Partial Fractions)

Chapter 5 Inverse Functions The Logarithmic and Exponential Functions, Inverse Trigonometric Functions

- (1) Derivative of Inverse functions
- (2) The Logarithmic and Exponential Functions
- (3) Inverse Trigonometric Functions
- (4) More on Differentiation and Integrations of Functions