

Math 165: Honors Calculus I

Name: _____

Quiz 8 *November 4, 1999*

1. Let n be a positive integer and define $f(x) = \int_0^x \frac{1}{t^{2n} + 1} dt$. Using the definition of continuity, prove that $f(x)$ is continuous at any real number p . [Hint: $\frac{1}{t^{2n} + 1} \leq 1$.]

2. a) State BOLZANO'S THEOREM.

b) State the INTERMEDIATE VALUE THEOREM.

3. Prove that the function $f(x) = 1 + \sin(x)$ has a fixed point, (i.e., there is a number c such that $f(c) = c$).