

Math 166: Honors Calculus II

Name: _____

Quiz 9 *Apr. 6, 1995*

1. a) Prove that $\sum_{n=0}^{\infty} x^n$ converges to $\frac{1}{1-x}$ if $|x| < 1$.

b) Prove that $\sum_{n=1}^{\infty} \frac{1}{n}$ diverges.

2. Prove that the series converges to the indicated sum.

$$\text{a) } \sum_{n=1}^{\infty} \frac{2^{n-1} + 3^{n+1}}{4^n} = \frac{19}{2}.$$

$$\text{b) } \sum_{n=2}^{\infty} \log\left(1 - \frac{1}{n^2}\right) = -\log(2). \text{ (Hint: Use telescoping series).}$$