

1. Determine which of the following statements are true or false.

a) If  $a_n > 0$  and  $\sum_{n=1}^{\infty} a_n$  converges then  $\lim_{n \rightarrow \infty} a_n = 0$ .

b) If  $a_n > 0$  and  $\lim_{n \rightarrow \infty} a_n = 0$  then  $\sum_{n=1}^{\infty} a_n$  converges.

c) If  $a_n > 0$  and  $\sum_{n=1}^{\infty} a_n$  converges then  $\lim_{n \rightarrow \infty} a_n^{1/n} = 0$ .

d) If  $a_n > 0$  and  $\lim_{n \rightarrow \infty} a_n^{1/n} = 0$  then  $\sum_{n=1}^{\infty} a_n$  converges.

e) If  $a_n > 0$  and  $\lim_{n \rightarrow \infty} a_n = 0$ , then  $\sum_{n=1}^{\infty} (-1)^n a_n$  converges.

f) If  $a_n > 0$ ,  $b_n > 0$  and  $\lim_{n \rightarrow \infty} \frac{a_n}{b_n} = 0$  then  $\sum_{n=1}^{\infty} a_n$  converges whenever  $\sum_{n=1}^{\infty} b_n$  converges.

g) If  $a_n > 0$ ,  $b_n > 0$  and  $\lim_{n \rightarrow \infty} \frac{a_n}{b_n} = 1$  then  $\sum_{n=1}^{\infty} a_n$  converges if and only if  $\sum_{n=1}^{\infty} b_n$  converges.

h) If  $\sum_{n=1}^{\infty} a_n$  converges, then  $\sum_{n=1}^{\infty} |a_n|$  converges.

i) If  $\sum_{n=1}^{\infty} |a_n|$  converges then  $\sum_{n=1}^{\infty} a_n$  converges.

j) If  $\sum_{n=1}^{\infty} a_n$  is conditionally convergent, then  $\sum_{n=1}^{\infty} (-1)^n a_n$  converges.

2. Determine whether the series  $\sum_{n=1}^{\infty} \frac{(-1)^n n}{(n+1)^2}$  is absolutely convergent, conditionally convergent, or divergent.

3. Compute the integral, if possible, or test it for convergence.

a)  $\int_1^{\infty} \frac{\log(x)}{x^2} dx$  [Hint:  $u = \log(x)$ ]

b)  $\int_0^{\infty} e^{-x^2} dx$