

Math 166: Honors Calculus II

Name: _____

Quiz 7 *March 23, 2000*

1. Define precisely $\lim_{x \rightarrow \infty} f(x) = L$.

2. Prove that if $\lim_{x \rightarrow a} \frac{f(x)}{g(x)} = \infty$ then $\lim_{x \rightarrow a} \frac{g(x)}{f(x)} = 0$.

3. Compute the limits:

a) $\lim_{x \rightarrow 0} \frac{x \cos(x) - \sin(x)}{x^3}$

b) $\lim_{x \rightarrow \infty} x^4(e^{1/x^2} - 1) - x^2$

c) $\lim_{x \rightarrow \infty} \left(\frac{x+1}{x-1}\right)^x$