## Mathematics 214: Introduction to Statistics Review for Exam 3, April 1999

The following table is to be used for the questions 1) - 4).

|  |  | $X_{1}$ |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- |
|  |  |  |  |  |  |
|  |  | 0 | 1 | 2 |  |
| $X_{2}$ | -1 | 0.2 | 0.15 | 0.1 |  |
|  | 0 | 0.1 | 0.05 | 0.05 |  |
|  | 1 | 0.2 | 0.1 | 0 |  |
|  | 2 | 0.05 | 0 | 0 |  |
|  |  |  |  |  |  |

1. Find $P\left(X_{1} \geq 1\right)$.
a) 0.55
b) 0.35
c) 0.45
d) 0.25
e) 0.3
2. Find $E\left(X_{2}\right)$.
a) 1
b) -0.05
c) 0.6
d) -0.1
e) .15
3. Find $E\left(X_{1} X_{2}\right)$.
a) 0
b) 1
c) -0.25
d) -0.15
e) 0.6
4. Find $P\left(X_{1}=2 \mid X_{2}=0\right)$.
a) 0.03
b) 0.05
c) $\frac{1}{3}$
d) $\frac{1}{11}$
e) $\frac{1}{4}$
5. The fracture strengths of a certain type of glass average 14 (in thousands of pounds per square inch) and have a standard deviation of 2 . What is the probability that the average fracture strength for 100 pieces of this glass exceeds 14.5 ?
a) 0.0202
b) 0.4938
c) 0.9938
d) 0.0062
e) 0.4013
6. A fair die is tossed 600 times. What is the approximate probability that at most 90 times a "six" comes up? (You may use a calculator.)
a) $\frac{9}{60}$
b) 0.3508
c) 0.1492
d) $\frac{9}{10}$
e) 0.8508
7. Let $X$ and $Y$ be random variables with variances $V(X)=1$ and $V(Y)=9$ respectively. Assume $\operatorname{Cov}(X, Y)$, the covariance of $X$ and $Y$, is 2 . Then the correlation coefficient $\rho$ between $X$ and $Y$ is
a) $\frac{2}{3}$
b) $\frac{4}{3}$
c) $\frac{2}{9}$
d) $\frac{4}{9}$
e) $\frac{2}{\sqrt{3}}$
8. Let $X$ and $Y$ be random variables with

$$
E(X)=3, E(Y)=6, V(X)=9, V(Y)=1, E(X Y)=20
$$

Then the covariance $\operatorname{Cov}(X, Y)$ of $X$ and $Y$ is
a) 2
b) -2
c) $\frac{2}{3}$
d) 11
e) $-\frac{2}{3}$
9. The times to failure of four turbine blades in jet engines, in $10^{3}$ hours, were as follows:

$$
3.2,1.8,2.6,4.4
$$

The sample mean of these data is
a) $\frac{3}{4}$
b) 3
c) 12
d) 4
e) $\frac{11}{4}$
10. The times in minutes between eruptions for three of the eruptions of the geyser Old Faithful on August 1,1985 were $77,80,80$. The sample mean of these data is 79 . Find the sample variance.
a) 3
b) 2
c) 6
d) 6244
e) 3123.5
11. The diameter measurements of an electric cable, taken at 100 points along the cable, yield a sample mean of 2.1 centimeters and a sample standard deviation of 0.3 centimeter. Construct a $90 \%$ confidence interval for the average diameter of the cable.
a) $0.3 \pm 1.645 \frac{2.1}{10}$
b) $2.1 \pm 1.96 \frac{0.09}{10}$
c) $2.1 \pm 1.645 \frac{0.3}{100}$
d) $2.1 \pm 1.645 \frac{0.3}{10}$
e) $2.1 \pm 1.96 \frac{0.3}{10}$
12. Suppose that a random sample of only 15 black cherry trees has been taken to estimate the average volume of a black cherry tree in the Allegheny National Forest. Assume that the sample mean for the volumes (in cubic feet) of the 15 trees is $\bar{x}=30.2$ and the sample variance is $s^{2}=268.96\left(=16.4^{2}\right)$. If we assume further that the distribution of the volumes of all the black cherry trees is normal, then a confidence interval for the average volume of a tree in this forest with confidence coefficient 0.98 is:
a) $\quad 30.2 \pm 1.345 \frac{16.4}{\sqrt{15}}$
b) $\quad 30.2 \pm 2.33 \frac{16.4}{\sqrt{15}}$
c) $\quad 30.2 \pm 29.1413 \frac{16.4}{\sqrt{15}}$
d) $30.2 \pm 2.624 \frac{16.4}{\sqrt{14}}$
e) $\quad 30.2 \pm 2.624 \frac{16.4}{\sqrt{15}}$
13. Suppose $n=13$ observations are taken on normally distributed measurements. The sample variance is $s^{2}=5$. A confidence interval for the variance $\sigma^{2}$ with confidence coefficient 0.99 is approximately given by
a) $\left(\frac{60}{21.03}, \frac{60}{5.23}\right)$
b) $\left(\frac{60}{28.3}, \frac{60}{3.07}\right)$
c) $\left(-\frac{60}{28.3}, \frac{60}{28.3}\right)$
d) $\left(\frac{60}{29.82}, \frac{60}{3.57}\right)$
e) $\left(-\frac{60}{3.07}, \frac{60}{28.3}\right)$
14. Let $X, Y$ be independent random variables with $E(X)=3, E(Y)=4$ and $V(X)=9, V(Y)=25$. Then the covariance $\operatorname{Cov}(X, Y)$ is
a) 3
b) -3
c) 0
d) 27
e) 15
15. For an aptitude test for a certain job history shows scores to be normally distributed with a variance of 225.20 applicants are to take the test. Find the approximate probability that the sample variance of the test scores will be less than 138. (You may use a calculator.)
a) 0.1
b) 0.9
c) 0.975
d) 0.025
e) 0.05
16. One-hour carbon monoxide concentrations in air samples from a large city average 10 ppm , with a standard deviation of 9 ppm . Find the probability that the average concentration in 100 samples selected randomly will exceed 12 ppm .
a) 0.4129
b) 0.0132
c) 0.4868
d) 0.0871
e) 0.2514

| 1. | (a) | (b) | (c) | (d) | (e) | 9. | (a) | (b) | (c) | (d) | (e) |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 2. | (a) | (b) | (c) | (d) | (e) | 10. | (a) | (b) | (c) | (d) | (e) |
| 3. | (a) | (b) | (c) | (d) | (e) | 11. | (a) | (b) | (c) | (d) | (e) |
| 4. | (a) | (b) | (c) | (d) | (e) | 12. | (a) | (b) | (c) | (d) | (e) |
| 5. | (a) | (b) | (c) | (d) | (e) | 13. | (a) | (b) | (c) | (d) | (e) |
| 6. | (a) | (b) | (c) | (d) | (e) | (e). | (a) | (b) | (c) | (d) | (e) |
| 7. | (a) | (b) | (c) | (d) | (e) | (e) | (a) | (b) | (c) | (d) | (e) |
| 8. | (a) | (b) | (c) | (d) | (e) | (e. | (a) | (b) | (c) | (d) | (e) |

