Chris Bendel and Peter Cholak Math 222 - Quiz 7 Wednesday, March 17
Be sure to carefully write up your answers. It is suggested that you first write out a draft of your proposed questions and then carefully rewrite that draft to get your final version. You do not have to write the answers on this sheet of paper.

Problem 4 from Section 6.3.
Consider the Galois Field $F \equiv \operatorname{GF}\left(3, x^{2}+x+2\right)$. Let $\alpha$ be the associated Galois imaginary.
(a) Compute all powers of $\alpha$, i.e. $\alpha, \alpha^{2}, \alpha^{3}, \ldots$ What is the least power for which $\alpha^{k}=1$ ?
(b) Find the inverse of each nonzero element in $F$. Hint: Use part (a).
(c) By definition $\alpha$ is one solution to $x^{2}+x+2=0$ over $\mathbb{Z}_{3}$. There should of course be another solution. It is also an element of $F$. Find this element. Is it a power of $\alpha$ ? Hint: Use long division.

