

Record your answers to the multiple choice problems by placing an \times through one letter for each problem on this answer sheet. There are 14 multiple choice questions worth 6 points each. You start with 16 points.

Find the limit $\lim_{(x,y) \rightarrow (0,0)} \left(\frac{x^2 - y^2}{x^2 + y^2} \right)^2$. *does not exist* 0 1 4 2

Let $f(x, y) = \cos(x^2y)$. Compute $f_{xy}(2, \pi)$. -16π 8π -4π π 0

A triangular sheet of glass is expanding. When the base is 2 inches and the height is 4 inches, the base is increasing at the rate of 0.25 in/hr and the height at 0.5 in/hr. At what rate is the area of the triangle increasing? $1.0 \text{ in}^2/\text{hr}$ $0.75 \text{ in}^2/\text{hr}$ $1.5 \text{ in}^2/\text{hr}$ $1.75 \text{ in}^2/\text{hr}$ $2.0 \text{ in}^2/\text{hr}$

Suppose that z is a function of u and v , and that $u = e^{xy}$ and $v = \frac{x}{y}$. If $z_u(e, 1) = 3$ and $z_v(e, 1) = 1$, find z/dy when $x = 1$ and $y = 1$. $3e - 1$ 1 0 $e - 3$ $-e$

Which of the following represents the graph of the function $f(x, y) = 12y - y^3 - 3x^2$?

Compute the derivative of $f(x, y) = x^2y - y^2 - 2$ in the direction $3\mathbf{i} + 4\mathbf{j}$ at the point $(2, 1)$. 4
 12 $\mathbf{i} + 8\mathbf{j}$ $4\mathbf{i} + 2\mathbf{j}$ 20 *does not exist*

Find the direction in which the function $f(x, y) = x^3 - 3xy^2$ increases most rapidly at the point $(1, -1)$.
 \mathbf{i} \mathbf{j} $3x^2\mathbf{i} - 2xy\mathbf{j}$ $(x^2 - y)\mathbf{i} - x\mathbf{j}$ $2\mathbf{i} - \mathbf{j}$

Determine the equation of the plane tangent to the paraboloid $z = 9 - 4x^2 - y^2$ at the point $(1, 1, 4)$.
 $8x + 2y + z = 14$ $x + y + 4z = 18$ $4x + 2y + z = 10$ $x + 8y + 4z = 25$ $x + 4y + z = 9$

Determine the critical points of the function $f(x, y) = 3x^2 - 3xy^2 + 2y^3$. $(0, 0)$, $(2, 2)$ $(0, 0)$, $(2, 0)$, $(2, 2)$
 $(0, 0)$, $(2, 0)$ $(0, 0)$, $(2, 2)$, $(-2, 2)$ $(0, 0)$, $(2, 0)$, $(2, 2)$, $(-2, 2)$

The function $f(x, y) = 2x^3 - 6x + 2y^3 - 3xy^2$ has a critical point at $(\sqrt{2}, \sqrt{2})$. Use the Second Partials Test to determine which of the following is true at this point: f has a relative minimum f has a relative maximum f has a saddle point *test is inconclusive* *none of the above*

Find the maximum of the function $f(x, y) = y^3 + 3x^2y$ in the region $x^2 + y^2 \leq 4$. $8\sqrt{2}$ 8 0 16 $16\sqrt{2}$

Determine which of the following sets of equations must be solved to find the extreme values of the function $f(x, y) = x^3y + y^2x + xy^4$ subject to the constraint $x^4 + 4xy + y^4 = 4$.

$$\begin{aligned} 3x^2y + y^2 + y^4 &= \lambda(4x^3 + 4y) \\ x^3 + 2xy + 4xy^3 &= \lambda(4x + 4y^3) \\ x^4 + 4xy + y^4 &= 4 \end{aligned}$$

$$\begin{aligned} 3x^2y + y^2 + y^4 &= \lambda(4x^3 + 4y^3) & 3x^2y + y^2 + y^4 &= \lambda(4x^3 + 4y + 4y^3) & 3x^2y + y^2 + y^4 &= \lambda(4x^3 + 4y^3) & 3x^2y + y^2 + y^4 &= \lambda(4x^3 + 4y^3) \\ x^3 + 2xy + 4xy^3 &= \lambda(4x^3 + 4y^3) & 3x^2 + 2y + 4y^3 &= \lambda(4x + 4y^3) & x^3 + 2xy + 4xy^3 &= \lambda(4x^3 + 4y^3) & x^3 + 2xy + 4xy^3 &= \lambda(4x^3 + 4y^3) \\ 4x^3 + 4y + 4y^3 &= 0 & x^4 + 4xy + y^4 &= 4 \end{aligned}$$

Let R be the triangle in the plane with vertices at the points $(0, 0)$, $(0, 1)$, and $(1, 1)$. Compute the double integral $\int_R x + y^2 dA$. $\frac{5}{12}$ $\frac{6}{15}$ $\frac{1}{4}$ $\frac{1}{3}$ $\frac{2}{5}$

Reverse the order of integration of the iterated integral $\int_0^1 \int_{\sqrt{y}}^1 f(x, y) dx dy$. $\int_0^1 \int_0^{x^2} f(x, y) dy dx$ $\int_1^{\sqrt{x}} \int_0^1 f(x, y) dy dx$

$$\int_0^1 \int_{\sqrt{x}}^1 f(x, y) dy dx \quad \int_{\sqrt{y}}^1 \int_0^1 f(x, y) dx dy \quad \int_0^1 \int_{x^2}^1 f(x, y) dy dx$$

Find the centroid of the region between the y -axis and $x = 1 - y^4$. $(\frac{4}{9}, 0)$ $(\frac{32}{45}, 0)$ $(\frac{5}{8}, 0)$ $(\frac{3}{8}, 0)$ $(\frac{4}{5}, 0)$